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Cosmological bounds on the field content of asymptotically safe gravity–matter models

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ABSTRACT

We use the non-Gaussian fixed points (NGFPs) appearing in the renormalization group flow of gravity and gravity–matter systems to construct models of NGFP-driven inflation via a renormalization group improvement scheme. The cosmological predictions of these models depend sensitively on the characteristic properties of the NGFPs, including their position and stability coefficients, which in turn are determined by the field content of the underlying matter sector. We demonstrate that the NGFPs appearing in gravity–matter systems where the matter content is close to the one of the standard model of particle physics are the ones compatible with cosmological data. Somewhat counterintuitively, the negative fixed point value of the dimensionless cosmological constant is essential for these findings.

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1. Introduction

The Planck and WMAP satellite missions have measured the fluctuation spectrum of the cosmic microwave background (CMB) at an hitherto unprecedented precision [1,2]. Combined with other cosmological observations like baryon acoustic oscillations obtained from large scale galaxy surveys this data allows to determine cosmic parameters describing the evolution of the early universe rather accurately. In particular the spectral index $n_s = 0.968 \pm 0.006$, the normalization of the scalar power spectrum $\ln 10^{10} \mathcal{A}_* = 3.062 \pm 0.029$, and the bound on the tensor-to-scalar ratio $r < 0.11$ (95% CL), reported in [3], are determined with a precision where one can actually discriminate between (and also rule out) various inflationary models [4].

A quite surprising outcome of these investigations is that data seems to favor simplicity. Inflationary models based on a single scalar field or modified gravity theories based on an R^2 -Lagrangian (Starobinsky-inflation) are quite successful in explaining the observation. In particular, the rather simple action

$$S = \frac{M_{\text{Pl}}^2}{2} \int d^4x \sqrt{-g} \left(R + \frac{1}{6m^2} R^2 \right) \quad (1)$$

predicts a scalar spectral index n_s and a scalar-to-tensor ratio r

$$n_s \simeq 1 - \frac{2}{N}, \quad r \simeq \frac{12}{N^2} \quad (2)$$

where N is the number of e -folds of expansion between the creation of the fluctuation spectrum and the end of inflation. For typical values of N between 50 and 60, this is in striking agreement with observations [4]. Moreover, the normalization of the scalar power spectrum indicates that the scalaron mass m should be of the order $m^2 \sim 10^{-10} M_{\text{Pl}}^2$ [2,5].

In this work we study a close relative of Starobinsky inflation, the so-called NGFP-driven inflation. This scenario is motivated by the idea of Weinberg [6,7] that the short distance behavior of gravity may be controlled by a non-Gaussian fixed point (NGFP) of the gravitational renormalization group flow. In this framework coupling constants like Newton's constant G or the cosmological constant Λ become energy-scale dependent. At energies above the Planck scale the “running” of these couplings is controlled by the NGFP which ensures that their dimensionless counterparts $g_k = G_k k^2$, $\lambda_k = \Lambda_k k^{-2}$, ... approach constant values as the energy scale k goes to infinity. In this way the quantum theory is free from unphysical UV-divergences or, synonymously, “asymptotically safe”. Starting from the seminal work [8] this scenario has been widely explored for pure gravity [8–45] and, more recently, also in

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Table 1

Fixed point structure arising from gravity–matter systems on foliated spacetimes [43] (foliated columns) and the $f(R)$ -computation [63] (covariant columns). In the foliated case the gravitational degrees of freedom are carried by the fields appearing in the Arnowitt–Deser–Misner formalism [83] while the covariant computation considers fluctuations of a graviton $h_{\mu\nu}$ in a fixed background. Despite the different ways of encoding the gravitational degrees of freedom, both settings give rise to remarkably similar values for the critical exponents θ_i . The Standard Model (SM), its minor modifications, and the Minimal Supersymmetric Standard Model (MSSM) induce a gravity–matter NGFP with $\lambda_* g_* < 0$. The difference in the fixed point structure found for GUT-type models can be traced back to the different gauge-fixing procedures employed by the computations (see [63] for a detailed discussion of this point). The eigenvectors $\mathbf{e}_{1,2}$ are normalized such that $e_1^1 = e_2^2 = 1$.

Model	Field content			Foliated						Covariant					
	N_S	N_D	N_V	g_*	λ_*	θ_1	θ_2	e_1^2	e_1^1	g_*	λ_*	θ_1	θ_2	e_1^2	e_1^1
Pure gravity	0	0	0	0.78	+0.32	$0.503 \pm 5.387i$		0	0	2.53	0.18	4	2.775	0	0.22
Standard Model (SM)	4	$\frac{45}{2}$	12	0.75	−0.93	3.871	2.057	−0.06	−1.26	0.54	−0.63	4	2.127	0	−1.09
SM, dark matter (dm)	5	$\frac{45}{2}$	12	0.76	−0.94	3.869	2.058	−0.07	−1.24	0.55	−0.63	4	2.129	0	−1.07
SM, 3ν	4	24	12	0.72	−0.99	3.884	2.057	−0.06	−1.38	0.52	−0.66	4	2.121	0	−1.21
SM, 3ν , dm, axion	6	24	12	0.75	−1.00	3.882	2.059	−0.05	−1.34	0.54	−0.66	4	2.126	0	−1.16
MSSM (SM Higgs)	49	$\frac{61}{2}$	12	2.26	−2.30	3.911	2.154	−0.16	−1.01	1.27	−1.15	4	2.327	0	−0.81
MSSM (Higgs doublet)	53	$\frac{63}{2}$	12	2.66	−2.72	3.924	2.162	−0.16	−1.01	1.41	−1.28	4	2.370	0	−0.81
SU(5) GUT	124	24	24	0.17	+0.41	25.26	6.008	−0.05	1.48	–	–	–	–	–	–
SO(10) GUT	97	24	45	0.15	+0.40	19.20	6.010	−0.27	1.80	–	–	–	–	–	–

the context of gravity–matter systems [46–63]. This led to the key insight that gravity as well as many phenomenologically interesting gravity–matter systems possess a NGFP suitable for realizing asymptotic safety.

While this scenario is quite attractive from a quantum field theory point of view, since it allows for a consistent quantization of the gravitational force along the same lines of the other fundamental interactions, it also comes with the technical challenge that the action describing the gravitational interactions in the high-energy phase is quite complicated and not well understood. It is clear, however, that it contains higher curvature terms similar to the ones encountered in (1). Moreover, one expects that the set of asymptotically safe theories can be parameterized by a finite number of free parameters which need to be fixed based on experimental input.

Our present work then builds on two recent observations: First, it has been shown in [64] that, at the level of pure gravity, the class of Asymptotically Safe actions can be tested using cosmological data.¹ In particular it has been found that Starobinsky-type actions appear quite naturally, indicating that one may obtain interesting cosmologies within this set of models. Second, it has been understood that the addition of matter fields may give rise to NGFPs whose properties differ from the one found in the case of pure gravity. In particular their position projected to the g – λ -plane and the value of the stability coefficients, governing the scale-dependence of the couplings in the high-energy regime, depend on the precise matter content of the system. In [43] it was demonstrated that one can distinguish three broad classes of gravity–matter fixed points according to their stability properties: Class I, represented by pure gravity, has a spiraling attractor, Class II, containing the standard model of particle physics, has real critical exponents and a negative product $g_* \lambda_*$ while Class III, comprising GUT-type models, comes with real critical exponents and a positive product $g_* \lambda_*$, see Table 1.²

In this work we construct NGFP-driven inflationary models based on the three characteristic classes of non-Gaussian gravity–

matter fixed point and compare the resulting cosmological predictions. It thereby turns out that the inflationary models based on the Class II fixed points are highly favored. Counterintuitively, it is the negative value of the dimensionless cosmological constant at the NGFP which makes these models viable.³ In this way the interplay between cosmological measurements and NGFP-driven inflation puts (rather mild) bounds on the matter fields present in Nature.

The rest of the work is organized as follows. In Section 2 we briefly review the properties of the NGFPs encountered in gravity–matter systems following [43,63]. The inflationary models arising from these fixed points are constructed in Section 3 and the resulting cosmological signatures are derived in Section 4. The consequences of our findings are discussed in Section 5.

2. Asymptotic safety in a nutshell

A general feature of a quantum field theory is that its coupling constants u^α depend on the energy scale k . In the vicinity of a fixed point, located at u_*^α , the full RG flow is captured by the linearized beta functions

$$k \partial_k u^\alpha = \sum_\gamma B^\alpha_\gamma (u^\gamma_k - u_*^\gamma) \quad (3)$$

where the components of the stability matrix B are given by $B^\alpha_\gamma \equiv \partial_{u^\gamma} \beta^\alpha|_{u=u_*}$. Denoting the right-eigenvectors of B by $e_i^\alpha = (\mathbf{e}_i)^\alpha$ the stability coefficients θ_i of the system are defined as minus the eigenvalues of B , i.e. $\sum_\gamma B^\alpha_\gamma e_i^\gamma = -\theta_i e_i^\alpha$. The solution of the linearized equation (3) is then given by

$$u^\alpha(k) = u_*^\alpha + \sum_i c_i e_i^\alpha \left(\frac{k}{k_0} \right)^{-\theta_i}, \quad (4)$$

where c_i are free integration constants and k_0 is an arbitrary renormalization scale. The asymptotic safety condition, stating that the solution is attracted to the fixed point as $k \rightarrow \infty$, then entails that the coefficients c_i associated to the stability coefficients with $\text{Re } \theta_i < 0$ must be fixed to zero. Based on the construction of the

¹ For other works connecting Asymptotic Safety to cosmology see the original works [9,64–81] and [82] for a review.

² The link between the number of matter fields and the corresponding fixed point classification actually depends on the regularization scheme. Depending on the computational details like, e.g. the parameterization of the fluctuation fields, not all classes may be realized within a given setting. The conclusions of this work can then be drawn at the level of the fixed point properties, independently of the precise set of matter fields realizing the corresponding class.

³ Note that a negative cosmological constant in the NGFP-regime is not in conflict with the positive value of Λ observed at cosmological scales: the NGFP-regime and the classical regimes are connected through a crossover in which the sign of Λ_k changes at energies around the Planck scale.

complete phase diagram [13,84], one concludes that the linearized solution (4) provides a good approximation at energies $k^2 \gtrsim M_{\text{Pl}}^2$.

For the gravity–matter flows projected to the Einstein–Hilbert action, where $u_k^\alpha = \{\lambda_k, g_k\}$, it is actually useful to distinguish between the two cases where θ_1 and θ_2 are real (Classes II and III) or form a complex conjugate pair (Class I). In the first case (4) entails

$$\lambda_k = \lambda_* + c_1 e_1^1 \left(\frac{k}{k_0}\right)^{-\theta_1} + c_2 e_2^1 \left(\frac{k}{k_0}\right)^{-\theta_2}, \quad (5a)$$

$$g_k = g_* + c_1 e_1^2 \left(\frac{k}{k_0}\right)^{-\theta_1} + c_2 e_2^2 \left(\frac{k}{k_0}\right)^{-\theta_2}. \quad (5b)$$

The only free parameters are the dimensionless variables c_1 and c_2 which allow to select a particular RG trajectory and can be determined by comparing physical observables, e.g. physical couplings in the effective Lagrangian, with observations.

For complex stability coefficients, $\theta_{1,2} = \theta' \pm i\theta''$, the eigenvectors $\mathbf{e}_{1,2}$ are complex conjugates of each other. Redefining $\mathbf{e}_1 = \text{Re } \mathbf{e}_1$ and $\mathbf{e}_2 = \text{Im } \mathbf{e}_2$ and similarly for $c_{1,2}$ the general solution can be written as

$$\lambda_k = \lambda_* + \left((c_1 \cos(\theta''t) + c_2 \sin(\theta''t)) e_1^1 + (c_1 \sin(\theta''t) - c_2 \cos(\theta''t)) e_2^1 \right) \left(\frac{k}{k_0}\right)^{-\theta'}, \quad (6a)$$

$$g_k = g_* + \left((c_1 \cos(\theta''t) + c_2 \sin(\theta''t)) e_1^2 + (c_1 \sin(\theta''t) - c_2 \cos(\theta''t)) e_2^2 \right) \left(\frac{k}{k_0}\right)^{-\theta'}. \quad (6b)$$

Here $t \equiv \ln(k/k_0)$.

For later reference, we note the inversion formula for g_k . Employing the geometric series expansion, eq. (5b) gives

$$\frac{1}{g_k} = \frac{1}{g_*} \sum_{n=0}^{\infty} (-1)^n \left[\frac{c_1}{g_*} e_1^2 \left(\frac{k}{k_0}\right)^{-\theta_1} + \frac{c_2}{g_*} e_2^2 \left(\frac{k}{k_0}\right)^{-\theta_2} \right]^n. \quad (7)$$

Ordering the stability coefficients according to $\theta_1 \geq \theta_2 > 0$, and assuming that $k/k_0 \gg 1$, the leading terms in this expansion are

$$\frac{1}{g_k} \simeq \frac{1}{g_*} \left[1 - \frac{c_2}{g_*} e_2^2 \left(\frac{k}{k_0}\right)^{-\theta_2} + \text{subleading} \right]. \quad (8)$$

Analogously, the case of complex critical exponents (6b) leads to

$$\frac{1}{g_k} = \frac{1}{g_*} \sum_{n=0}^{\infty} (-1)^n \left[\frac{1}{g_*} (\dots) \left(\frac{k}{k_0}\right)^{-\theta'} \right]^n, \quad (9)$$

where the dots represent the expression in the round bracket.

We close the section by introducing “reference models” for each of the three classes represented in Table 1.

$$\begin{array}{ll} \text{Class I:} & \begin{array}{ll} \theta' = 0.5, & \mathbf{e}_1 = \{1, 0\} \\ \theta'' = 5, & \mathbf{e}_2 = \{0, 1\} \end{array} \end{array} \quad (10a)$$

$$\begin{array}{ll} \text{Class IIa:} & \begin{array}{ll} \theta_1 = 4, & \mathbf{e}_1 = \{1, 0\} \\ \theta_2 = 2, & \mathbf{e}_2 = \{-1, 1\} \end{array} \end{array} \quad (10b)$$

$$\begin{array}{ll} \text{Class IIb:} & \begin{array}{ll} \theta_1 = 4, & \mathbf{e}_1 = \{1, 0\} \\ \theta_2 = 3, & \mathbf{e}_2 = \{0.2, 1\} \end{array} \end{array} \quad (10c)$$

$$\begin{array}{ll} \text{Class III:} & \begin{array}{ll} \theta_1 = 25, & \mathbf{e}_1 = \{1, 0\} \\ \theta_2 = 6, & \mathbf{e}_2 = \{1.5, 1\} \end{array} \end{array} \quad (10d)$$

These reference models mainly serve the purpose of highlighting the qualitatively different cosmological dynamics which results from the RG improved actions constructed below. Apart from the critical exponents listed for pure gravity (Class I), the values for θ_i correspond to “typical values” for critical exponents obtained in the corresponding setting.⁴ In the case of pure gravity, a detailed comparison [42] of critical exponents obtained from different computations shows that $\theta' \simeq 1.5$ and $\theta'' \simeq 3$ may be a better approximation to the exact value. Notably, the cosmological analysis carried out below is actually independent of the way the critical exponents are computed and the cosmological constraints remain valid independently of the gravity–matter system which realizes the corresponding critical exponents.

At this stage the following remark is in order. The linearized approximation of the RG flow (3) holds in the vicinity of a RG fixed point only. The full phase diagrams for selected gravity–matter models have been constructed in [43]. These show that even in the case where $\lambda_* \leq 0$, there are RG trajectories which undergo a crossover to $\lambda_k > 0$ at observable scales. Thus $\lambda_* \leq 0$ is not in tension with the positive value of the cosmological constant observed at cosmic scales.

3. Effective Lagrangians for quantum gravity–matter systems

In the present discussion we restrict the gravitational sector to the Einstein–Hilbert truncation. The corresponding scale-dependent Lagrangian reads

$$\mathcal{L}_k = \frac{k^2}{16\pi g_k} (R - 2\lambda_k k^2). \quad (11)$$

Throughout the study, we assume that inflation is driven by quantum gravitational effects so that the dynamics of the matter sector can be neglected.

A RG-improved Lagrangian can be obtained by substituting the running couplings (5) into eq. (11) [68,69,72,73,77,85–87]. The resulting analytical expression strongly depends on the critical exponents θ_i . In particular, following the discussion in [43], these stability coefficients are complex conjugate in the case of pure gravity case, positive and real for gravity–matter systems such as the Standard Model (SM) and its modifications (see Table 1).

In order to close the system, the infrared cutoff k must be related to a diffeomorphism-invariant quantity such that the resulting semi-classical model is described by an effective diffeomorphism-invariant Lagrangian.⁵ The simplest scale-setting satisfying these requirements is [32,77,94,95]

$$k^2 = \xi R. \quad (12)$$

Here ξ is an a priori undetermined, positive constant whose value may be fixed by comparing to a one-loop computation [96] or imposing other physical requirements. The cutoff identification (12) generates an effective $f(R)$ -type Lagrangian in a natural way. Notably, evaluating eq. (11) at the fixed point, where $g_k = g_*$ and $\lambda_k = \lambda_*$, the scale-setting (12) gives rise to the R^2 -type action identified in [20,97,98] as the RG fixed point of $f_k(R)$ -gravity.

⁴ The precise values for the critical exponents associated with the NGFPs appearing in pure gravity and gravity–matter systems are currently not known. The values listed above reflect current “best estimates” which may vary slightly depending on the precise form of the approximations made when evaluating the functional renormalization group equation, choice of regularization procedure, or spacetime signature [41].

⁵ In the case of scalar-field theory a similar cutoff-identification allows to retrieve the Coleman–Weinberg potential in a rather straightforward manner [88–93].

Starting from the scale-dependent Lagrangian (11), substituting the scale-dependent couplings from eqs. (5a) and (7) (truncating the geometric expansions at $n = 1$) and applying the scale-setting procedure (12) results in the following RG-improved Lagrangian

$$\mathcal{L}_{\text{eff}} = a_0 R^2 + b_1 R^{\frac{4-\theta_1}{2}} + b_2 R^{\frac{4-\theta_1}{2}} + b_3 R^{\frac{4-\theta_2}{2}} + b_4 R^{2-\theta_1} + b_5 R^{2-\theta_2}. \quad (13)$$

The coefficient of the R^2 -term is given by

$$a_0 = \frac{\xi(1 - 2\xi\lambda_*)}{16\pi g_*}, \quad (14)$$

while the b_i 's read

$$b_1 = \frac{c_1 c_2 (e_1^2 e_2^2 + e_1^2 e_2^2) \xi^{\frac{4-\theta_1-\theta_2}{2}} k_0^{\theta_1+\theta_2}}{8\pi g_*^2}, \quad (15a)$$

$$b_2 = \frac{c_1 (2e_1^2 \xi \lambda_* - 2e_1^2 \xi g_* - e_1^2) \xi^{\frac{2-\theta_1}{2}} k_0^{\theta_1}}{16\pi g_*^2}, \quad (15b)$$

$$b_3 = \frac{c_2 (2e_2^2 \xi \lambda_* - 2e_2^2 \xi g_* - e_2^2) \xi^{\frac{2-\theta_2}{2}} k_0^{\theta_2}}{16\pi g_*^2}, \quad (15c)$$

$$b_4 = \frac{c_1^2 (e_1^1 e_1^2) \xi^{2-\theta_1} k_0^{2\theta_1}}{8\pi g_*^2}, \quad (15d)$$

$$b_5 = \frac{c_2^2 (e_2^1 e_2^2) \xi^{2-\theta_2} k_0^{2\theta_2}}{8\pi g_*^2}. \quad (15e)$$

Notably, the scale-setting procedure always produces an R^2 -term whose coefficient is determined by (λ_*, g_*, ξ) . The occurrence of this term is universal in the sense that it does not depend on the field content of the model and solely relies on the presence of a NGFP. The information about the stability coefficients θ_i and the chosen RG trajectory (c_i -coefficients) is carried by the b_i -terms. As it will turn out, it is these terms that encode the subleading corrections to the scale-free fluctuation spectrum. Also note that negative stability coefficients $\theta_i < 0$, which would naively dominate (13) in the large curvature regime, do not enter $\mathcal{L}_{\text{eff}}$. From eq. (4) one sees that such terms come with positive powers of k , so that the corresponding coefficients c_i must be set to zero to ensure that the flow approaches the fixed point as $k \rightarrow \infty$.

Following the same steps for a NGFP with complex critical exponents results in a class of improved Lagrangians studied in [77]

$$\begin{aligned} \mathcal{L}_{\text{eff}} = & a_0 R^2 + \tilde{b}_1 R^{\frac{4-\theta'}{2}} \cos\left(\frac{1}{2}\theta'' \ln\left(\frac{\xi R}{k_0^2}\right)\right) \\ & + \tilde{b}_2 R^{\frac{4-\theta'}{2}} \sin\left(\frac{1}{2}\theta'' \ln\left(\frac{\xi R}{k_0^2}\right)\right) \\ & + \tilde{b}_3 R^{2-\theta'} + \tilde{b}_4 R^{2-\theta'} \cos\left(\theta'' \ln\left(\frac{\xi R}{k_0^2}\right)\right) \\ & + \tilde{b}_5 R^{2-\theta'} \sin\left(\theta'' \ln\left(\frac{\xi R}{k_0^2}\right)\right) \end{aligned} \quad (16)$$

where

$$\tilde{b}_1 = \frac{(2\xi\lambda_* - 1)(c_1 e_1^2 - c_2 e_2^2) - 2\xi g_*(c_1 e_1^1 - c_2 e_2^1) \xi^{\frac{2-\theta'}{2}} k_0^{\theta'}}{16\pi g_*^2}, \quad (17a)$$

$$\tilde{b}_2 = \frac{(2\xi\lambda_* - 1)(c_2 e_1^2 + c_1 e_2^2) - 2\xi g_*(c_2 e_1^1 + c_1 e_2^1) \xi^{\frac{2-\theta'}{2}} k_0^{\theta'}}{16\pi g_*^2}, \quad (17b)$$

$$\tilde{b}_3 = \frac{(c_1^2 + c_2^2)(e_1^1 e_1^2 + e_2^1 e_2^2) \xi^{2-\theta'} k_0^{2\theta'}}{16\pi g_*^2}, \quad (17c)$$

$$\tilde{b}_4 = \frac{((c_1^2 - c_2^2)(e_1^1 e_1^2 - e_2^1 e_2^2) - 2c_1 c_2 (e_1^1 e_2^2 + e_2^1 e_1^2)) \xi^{2-\theta'} k_0^{2\theta'}}{16\pi g_*^2}, \quad (17d)$$

$$\tilde{b}_5 = \frac{((c_1^2 - c_2^2)(e_1^1 e_2^2 + e_2^1 e_1^2) + 2c_1 c_2 (e_1^1 e_1^2 - e_2^1 e_2^2)) \xi^{2-\theta'} k_0^{2\theta'}}{16\pi g_*^2}. \quad (17e)$$

At this stage, it is instructive to give the explicit form of $\mathcal{L}_{\text{eff}}$ arising from the prototypical fixed point of Class IIa associated to a typical standard model like matter content. Evaluating the general Lagrangian (13) for the fixed point characteristics (10b) leads to a Starobinsky-type action of the form⁶

$$\mathcal{L}_{\text{eff}} = \frac{1}{16\pi G_N} \left(R + \frac{1}{6m^2} R^2 - 2\Lambda_{\text{eff}} \right). \quad (18)$$

The effective couplings G_N, m^2 and Λ_{eff} in this Lagrangian are determined by the fixed point data g_*, λ_* and the specific RG trajectory underlying the improvement procedure c_1, c_2, ξ . Explicitly,

$$G_N = \frac{g_*^2}{c_2 (2g_* \xi + 2\lambda_* \xi - 1) k_0^2}, \quad (19a)$$

$$m^2 = \frac{g_*}{6\xi(1 - 2\lambda_* \xi) G_N}, \quad (19b)$$

$$\Lambda_{\text{eff}} = \frac{k_0^4 (c_2^2 + c_1 g_*) G_N}{g_*^2}. \quad (19c)$$

4. Cosmic parameters

We are now in the position to verify if and under which conditions NGFP-driven inflation gives rise to an inflationary scenario in agreement with the Planck data [1,2]. Depending on the critical exponents, some of the b_i -contributions to the Lagrangian (13) could be in the form R^{-p} , with p positive: these terms are suppressed when R is large and become important only on cosmic scales [99], where the linearized approximation of the RG flow, eq. (4), is no longer valid. In particular, if all critical exponents satisfy the condition $\theta_i > 4$ then all b_i -terms are suppressed [99] and the resulting Lagrangian $\mathcal{L} \sim R^2$ gives rise to a scale invariant scalar power spectrum, $n_s = 1$. Therefore, in order to obtain a phenomenologically interesting inflationary scenario compatible with observational data, at least one critical exponent must be $\theta_i < 4$. As $\theta_1 > \theta_2$ is assumed, the first constraint we find reads

$$\theta_2 < 4. \quad (20)$$

The prototypical NGFPs satisfying this requirement are the ones summarized in Class II. Following Table 1 these comprise gravity coupled to Standard Model matter and some of its frequently studied beyond the Standard Model extensions. Thus we start by analyzing this class. In practice this analysis is performed by converting the $f(R)$ -type Lagrangian to a scalar-tensor theory by adding suitable Lagrange multipliers (see [100,101] for a pedagogical account). The resulting scalar potential is illustrated in Fig. 2. The results obtained in this way are conveniently summarized in Fig. 1.

NGFPs of Class IIa: The effective Lagrangian for Class IIa is given in (18) with the relation between the NGFP and the effective couplings provided by (19). Neglecting Λ_{eff} for a moment, the model reduces to the $R + R^2$ -Lagrangian (1). The value of the mass m is fixed by the CMB normalization of the power spectrum, $\mathcal{A}_s \sim 10^{-10}$, and for a Starobinsky-like model this implies

⁶ Here we drop terms containing inverse powers of R since they do not affect the inflationary dynamics arising from actions of the type (18).

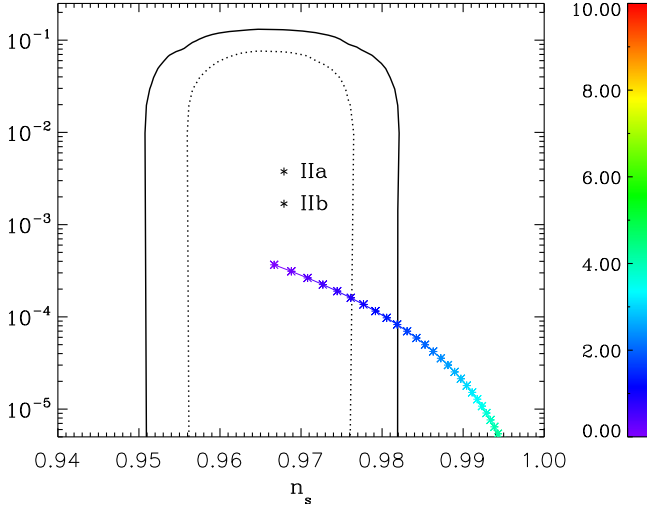


Fig. 1. Spectral index and tensor-to-scalar ratio induced by the class of theory (24) as a function of the power index p for $N = 60$ e-folds. Dashed and solid lines represents 1σ and 2σ level respectively. The data corresponding to Class IIa and Class IIb models are also displayed with a *. The values for the cosmic parameters obtained from Class I model are outside the range covered by the figure and therefore not shown. Note that the models IIa and IIb give rise to r -values which could be tested by future CMB experiments like CORE [102], LiteBIRD [103], PIXIE [104], or CMB S4 [105].

$m \simeq 10^{13}$ GeV (see [5] for details). Investigating (19b), treating ξ as a free parameter, one finds that this condition can only be met if

$$\lambda_* \leq 0. \quad (21)$$

Taking g_*, λ_* of order unity, the observational constraint $G_{\text{NM}}^2 \sim 10^{-11}$ fixes $\xi \sim 10^5$. The values of c_1 and c_2 can then be obtained by requiring that the RG trajectory underlying the construction reproduces the values for Newton's constant and the cosmological constant observed at large distances, see [87] for a detailed discussion. All parameters appearing in our model are thus completely fixed by observations. Inspecting Table 1, it is quite remarkable that there are indeed gravity-matter fixed points fulfilling the whole set of conditions $\theta_2 < 4$ and $\lambda_* \leq 0$. Even more remarkable, the NGFP found for the matter content of the standard model of particle physics is one representative of this class.

We now reinstall the cosmological constant and compute the spectral index n_s and tensor-to-scalar ratio r associated with the class of theories (18). These parameters can be easily computed within the slow-roll approximation [5]. A straightforward calculation gives

$$n_s = 1 - \frac{2}{N} + \frac{24 \Lambda_{\text{eff}} M_{\text{Pl}}^{-2} + \sqrt{3} - 3}{N^2} + O\left(\frac{1}{N^3}\right) \quad (22a)$$

$$r = \frac{12}{N^2} - \frac{144 \Lambda_{\text{eff}} M_{\text{Pl}}^{-2} + 12\sqrt{3}}{N^3} + O\left(\frac{1}{N^4}\right) \quad (22b)$$

where N is the number of e-folds. Assuming that Λ_{eff} is the cosmological constant observed today, the combination $\Lambda_{\text{eff}} M_{\text{Pl}}^{-2}$ is much less than one. Thus the Λ_{eff} -terms do not affect the cosmic fluctuation spectrum and can safely be neglected. The leading contribution to n_s and r are then in agreement with the Planck observational data provided $N \sim 50$ – 60 . In particular $n_s \sim 0.966$ and $r \sim 0.00324$ for $N = 60$.

NGFPs of Class IIb: The case of pure gravity with real critical exponents ($\theta_1 \sim 4$ and $\theta_2 \sim 3$) is covered by the Class IIb given in

eq. (10c). Using the slow-roll approximation and neglecting Λ_{eff} , the spectral index and tensor-to-scalar ratio are approximately given by

$$n_s = 1 - \frac{2}{N} - \frac{0.85}{N^2} + O\left(\frac{1}{N^{7/3}}\right) \quad (23a)$$

$$r = \frac{5.33}{N^2} - \frac{6.15}{N^3} + O\left(\frac{1}{N^4}\right) \quad (23b)$$

Notably the change in θ_2 and the corresponding eigenvector does not affect the leading $1/N$ -term in n_s and appears at order $1/N^2$ only. Setting $N = 60$ leads again to values for (n_s, r) compatible with the Planck data: the value of n_s is identical to the one produced by the Class IIa model, $n_s \sim 0.966$, but in this case the tensor-to-scalar ratio is much lower, $r \sim 0.00145$ (see Fig. 1).

NGFPs of Class III: The grand unified type models are characterized by critical exponents $\theta_i > 4$. In this case the leading terms appearing in (13) are

$$S = \frac{M_{\text{Pl}}^2}{2} \int d^4x \sqrt{-g} \left(\frac{R^2}{6m^2} + \frac{1}{R^p} \right) \quad (24)$$

where $p = (\theta_2 - 2)/2 \sim 2$. Although this type of theories do not reproduce General Relativity at long distances, it is interesting to study the corresponding cosmic parameters. The values of spectral index and tensor-to-scalar ratio depend on the number of e-folds N and power index p . Fixing the number of e-folds to $N = 60$, we obtained the functions $n_s(p)$ and $r(p)$ (see Fig. 1). As it can be seen in Fig. 1, for $p \gtrsim 1$ these models give rise to a power spectrum which is too close to scale-invariance and therefore not compatible with the Planck data. Moreover, the tensor-to-scalar ratio rapidly approaches zero as p increases.

NGFPs of Class I: The inflationary dynamics resulting from the family of effective Lagrangians (16) is rather complex. Comparing the coefficients $\tilde{b}_1, \tilde{b}_2$ and $\tilde{b}_3, \tilde{b}_4, \tilde{b}_5$ one first observes that the latter are suppressed by (inverse) powers of ξ . As the cutoff identification $k^2 = \xi R$ does not depend on the particular gravity-matter configuration, we can use the constraint $\xi \sim 10^5$ obtained before. The contribution of $\tilde{b}_3, \tilde{b}_4, \tilde{b}_5$ can then be neglected and we set $\tilde{b}_3 = \tilde{b}_4 = \tilde{b}_5 = 0$. Fixing $\tilde{b}_1 = \tilde{b}_2 = 1$ all models with $\theta' \lesssim 3$ lead to an oscillatory scalar potentials supporting an infinite number of meta-stable de Sitter vacua. A sufficiently pronounced inflationary phase leading to a sufficient number of e-folds may then be obtained by placing initial conditions for the scalar field close to a local maximum of the potential. The CMB fluctuations are then created when the field is very close to the local maximum, entailing $r \ll 1$. The value of the spectral index n_s is then essentially determined by the second slow-roll parameter η_V . Increasing θ' , the oscillations in the potential start smoothing out and the standard nearly-flat plateau is recovered when $\theta' \gtrsim 3$. In particular the values for (n_s, r) are not compatible with observations unless $\theta' \gtrsim 5$. For the specific model (10a), the Lagrangian (16) gives rise to the scalar potential shown in Fig. 2. The slow-roll conditions are fulfilled for all values $\phi \gtrsim 2.19 M_{\text{Pl}}$. An inflationary phase including an exit from the slow-roll condition can be realized by placing the starting value of ϕ close to the maximum at $\phi \simeq 4.23 M_{\text{Pl}}$. Evaluating the cosmic parameters for an inflationary scenario where the field rolls towards the minimum on the left yields $n_s = 0.423$ and $r \sim 10^{-16}$ which is clearly ruled out by observations. Thus one concludes that while some of the effective Lagrangians (16) give rise to a realistic inflationary dynamics, these models are not related to the critical exponents obtained from the renormalization group computations.

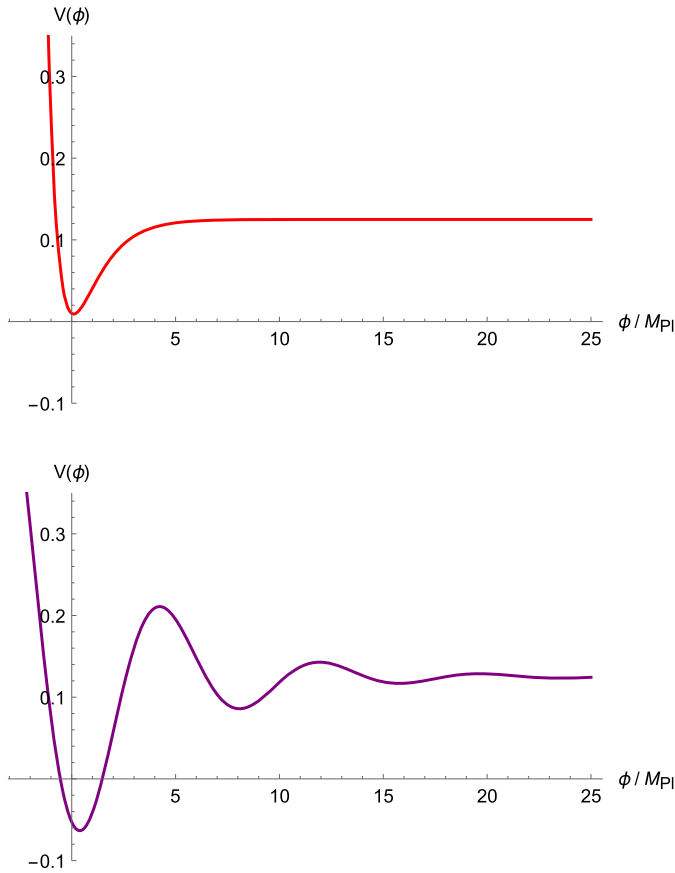


Fig. 2. Scalar potentials obtained from the action (18) (top) and (16) evaluated for the fixed point (10a) and coefficients $\tilde{b}_1 = \tilde{b}_2 = 1$ and $\tilde{b}_3 = \tilde{b}_4 = \tilde{b}_5 = 0$ (bottom). In the latter case the potential exhibits an infinite number of metastable de Sitter vacua. An inflationary phase including an exit from the slow roll conditions can be realized by starting close to the maximum at $\phi \simeq 4.23 M_{\text{Pl}}$ and rolling to the left.

5. Conclusions

The asymptotic safety mechanism provides a natural way for constructing consistent and predictive high-energy completions of gravity and gravity–matter systems. The characteristic properties of the NGFPs controlling the theories at trans-Planckian energy depend on the specific matter content of the model. Based on the Einstein–Hilbert approximation supplemented by minimally coupled matter fields one can distinguish three different classes of fixed points (see Table 1) according to their critical exponents and position. The effective models describing the evolution in the very early universe, eq. (13), sensitively depend on this data. The results are quite intuitive and corroborate the picture advocated in [73]: while the NGFP itself provides a scale-free scalar power spectrum and vanishing scalar-to-tensor ratio, flowing away from the fixed point induces (small) corrections to these values. Studying the resulting NGFP-driven inflationary scenarios and comparing the theoretical predictions with Planck data puts constraints on the fixed point properties.

Notably, cosmologies arising from RG-improvements have already undergone detailed investigations at the level of both pure gravity and dilaton-type actions [9,64–81]. The novel feature of this work consists in a RG-improvement procedure which takes the contribution of (standard model) matter fields into account in a rather systematic way. As a result, the resulting effective cosmological dynamics knows about the particle content of the universe. Quite remarkably, the models whose matter field content is close to the one of the standard model of particle physics are compatible

with the Planck data while fixed points associated with GUT-type models do not reproduce the observations. In particular, the discussion around eq. (21) shows that an acceptable normalization of scalar power spectrum requires $\lambda_* \leq 0$ and can not be achieved if $\lambda_* > 0$.

Remarkably, similar conclusions favoring a negative value of λ_* have been reached in [62] and [106] albeit based on very different considerations: in the former obtaining phenomenological viable particle physics models based on Asymptotic Safety mechanism required a negative fixed point value of the dimensionless cosmological constant, while in the latter $\lambda_* \leq 0$ was the key to a nonsingular cosmological evolution. It would be very interesting to see whether this feature can be corroborated by further studies.

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