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Water in star-forming regions with *Herschel* (WISH)

VI. Constraints on UV and X-ray irradiation from a survey of hydrides in low- to high-mass young stellar objects[★]

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ABSTRACT

Context. Hydrides are simple compounds containing one or a few hydrogen atoms bonded to a heavier atom. They are fundamental precursor molecules in cosmic chemistry and many hydride ions have become observable in high quality for the first time thanks to the *Herschel* Space Observatory. Ionized hydrides such as CH⁺ and OH⁺ (and also HCO⁺), which affect the chemistry of molecules such as water, provide complementary information on irradiation by far-UV (FUV) or X-rays and gas temperature.

Aims. We explore hydrides of the most abundant heavier elements in an observational survey covering young stellar objects (YSOs) with different mass and evolutionary state. The focus is on hydrides associated with the dense protostellar envelope and outflows, contrary to previous work that focused on hydrides in diffuse foreground clouds.

Methods. Twelve YSOs were observed with HIFI on *Herschel* in six spectral settings providing fully velocity-resolved line profiles as part of the Water in star-forming regions with *Herschel* (WISH) program. The YSOs include objects of low (Class 0 and I), intermediate, and high mass, with luminosities ranging from 4 $L_{\odot}$ to $2 \times 10^5 L_{\odot}$.

Results. The targeted lines of CH⁺, OH⁺, H₂O⁺, C⁺, and CH are detected mostly in blue-shifted absorption. H₃O⁺ and SH⁺ are detected in emission and only toward some high-mass objects. The observed line parameters and correlations suggest two different origins related to gas entrained by the outflows and to the circumstellar envelope. The derived column densities correlate with bolometric luminosity and envelope mass for all molecules, best for CH, CH⁺, and HCO⁺. The column density ratios of CH⁺/OH⁺ are estimated from chemical slab models, assuming that the H₂ density is given by the specific density model of each object at the beam radius. For the low-mass YSOs the observed ratio can be reproduced for an FUV flux of 2–400 times the interstellar radiation field (ISRF) at the location of the molecules. In two high-mass objects, the UV flux is 20–200 times the ISRF derived from absorption lines, and 300–600 ISRF using emission lines. Upper limits for the X-ray luminosity can be derived from H₃O⁺ observations for some low-mass objects.

Conclusions. If the FUV flux required for low-mass objects originates at the central protostar, a substantial FUV luminosity, up to 1.5 $L_{\odot}$, is required. There is no molecular evidence for X-ray induced chemistry in the low-mass objects on the observed scales of a few 1000 AU. For high-mass regions, the FUV flux required to produce the observed molecular ratios is smaller than the unattenuated flux expected from the central object(s) at the *Herschel* beam radius. This is consistent with an FUV flux reduced by circumstellar extinction or by bloating of the protostar.

Key words. stars: formation – stars: low-mass – stars: massive – ISM: molecules – ultraviolet: ISM – astrochemistry

1. Introduction

The physics and chemistry of the inner few thousand AU of star-forming regions are poorly constrained. *Herschel* (Pilbratt et al. 2010) has opened up the opportunity for high-quality observations of species that cannot (or only with great difficulties) be observed from the ground. Water is a key molecule, but to fully understand its chemistry related molecules such as hydrides and HCO⁺ must be characterized as well. Moreover, compared to cold cores, the chemistry in protostellar envelopes is affected by Far-UV (FUV) and X-rays from the central source. Some hydrides are particularly good diagnostics of this energetic radiation, which cannot be observed directly in the most deeply embedded phases of star formation.

Specifically, gaseous H₂O is destroyed by high levels of FUV (6.2–13.6 eV) or X-rays, both through photodissociation and through reactions with ionized species whose abundances are enhanced by irradiation (van der Tak & van Dishoeck 2000; Aalto et al. 2011). On the other hand, H₂O in the gas reduces the abundance of species like CH⁺, OH⁺, H₂O⁺, and HCO⁺. Thus their abundances and that of H₂O cannot be high at the same location. Stäuber et al. (2006) have analyzed the water abundance under various conditions in star-forming regions. At temperatures $T < 100$ K, irradiation induces the formation of water through ion-molecule reactions. For $100 < T < 250$ K, irradiation decreases the H₂O abundance through reactions with H₃⁺ and HCO⁺ and local UV emission of excited H₂. In the regime $T > 250$ K, endothermic neutral-neutral reactions produce H₂O efficiently, but a high X-ray flux at low densities ($n_{\text{H}} = 10^4$ – 10^5 cm^{−3}) destroys water and reduces its abundance by orders of magnitude. Constraining the amount of FUV and

[★] *Herschel* is an ESA space observatory with science instruments provided by a European-led Principal Investigator consortia and with important participation from NASA.

X-rays across the protostellar envelope is therefore important in tracing the full water chemistry.

Ionizing radiation may have several origins. If the surface temperature of a protostar exceeds 10^4 K, the emission of FUV becomes significant and is proportional to the radiating hot surface area. Accretion and jets produce shocked gas capable of emitting both FUV and X-rays. Finally, protostellar coronae are powerful emitters of both X-rays and high-energy UV radiation. When the envelopes of low-mass young stellar objects (YSOs) become transparent in the Class I phase, a median X-ray luminosity of more than 10^{30} erg s $^{-1}$ is observed that decreases with age (Feigelson & Montmerle 1999; Güdel 2004). Temperatures exceeding 10^7 K and occasional flares suggest a process in the stellar corona or the star-disk interface releasing magnetic energy (Benz & Güdel 2010). The average X-ray luminosity may reach a few times $10^{-3} L_{\text{bol}}$ or 10^{32} erg s $^{-1}$ (Güdel 2004), limited by the stellar magnetic field strength (few kGauss) and by the finite volume of the reconnection region.

X-rays and FUV radiation are absorbed differently in molecular gas. X-rays beyond 10 keV penetrate a half-power hydrogen column density of some 10^{24} cm $^{-2}$ (Maloney et al. 1996; Stäuber et al. 2005). The penetration depth of FUV photons is three orders of magnitude less, thus they are absorbed mainly at irradiated surfaces. For the distant massive objects, the sphere of influence of X-ray emission (if present) is geometrically limited to a small fraction of the *Herschel* beam and may be overwhelmed by FUV (Bruderer et al. 2010a). However, the accreting protostars may bloat and have a low surface temperature (Behrend & Maeder 2001). Significant populations of massive stars without HII regions have been reported (e.g., Lumsden et al. 2013). On the other hand, massive YSOs known to have ultra-compact HII regions indicate that their UV emission has significantly changed their circumstellar environment. The situation is different for the nearby low-mass objects studied here, where the X-ray dominated region (XDR) may exceed the size of the *Herschel* beam. Excess FUV emission has been inferred from observed mid-*J* CO isotopolog observations interpreted to originate from irradiated cavity walls created by the outflows (van Kempen et al. 2009; Yıldız et al. 2012, 2015). Here we provide independent tracers of the FUV and X-ray irradiation using observations of hydrides that are particularly sensitive to these radiations.

In addition to ionization, the high-energy photons heat the molecular gas and thus further enhance the abundances of those hydrides whose formation requires extra energy, such as CH $^+$ (Sternberg & Dalgarno 1995). Ionized hydrides are chemically active and can drive substantial chemical evolution. When formed, they generally react fast and without activation energy. Once their chemistry and excitation is understood, they will become tracers of warm and ionized gas in deeply embedded phases of star and planet formation.

Absorption lines of hydrides have been found in diffuse interstellar clouds both at optical and mm wavelengths (e.g., Liszt & Lucas 2002; Snow & McCall 2006) and were extensively observed by *Herschel*/HIFI (Falgarone et al. 2010; Gerin et al. 2010b; Monje et al. 2013; Flagey et al. 2013, and others). Relevant for this work are also ground-based SH $^+$ observations by Menten et al. (2011), HIFI CH $^+$ and SH $^+$ observations by Godard et al. (2012). The lines of this diffuse gas are also seen in our data at velocities substantially offset from the YSO.

Here we report on hydrides and their relation to H $_2$ O in star-forming regions, where the gas is denser, hotter, and strongly irradiated by the nearby protostar. In the environments of newly

forming stars, H $_2$ O has been found in various places including disks (e.g., Pontoppidan et al. 2010; Hogerheijde et al. 2011), shocked gas (Kristensen et al. 2013; Mottram et al. 2014), outflow lobes (Nisini et al. 2010, 2013; Lefloch et al. 2010; Kristensen et al. 2012; Busquet et al. 2014), and the envelope (e.g., Coutens et al. 2012; Kristensen et al. 2012; Mottram et al. 2013; van der Tak et al. 2013). The origin is generally inferred from line widths and Doppler shifts. Water observations were compared to CH $^+$, OH $^+$, and C $^+$ toward low-mass sources by Kristensen et al. (2013). The ratio of H $_2$ O $^+$ to H $_2$ O was measured in high-mass YSOs by Wyrowski et al. (2010).

We present results of the subprogram “Radiation Diagnostics” (Benz et al. 2013) of the *Herschel* guaranteed time key program “Water in Star-forming regions with *Herschel*” (WISH, van Dishoeck et al. 2011). Here the focus is on possibilities of identifying FUV and X-ray emission through chemistry in deeply embedded objects, where UV and X-rays cannot be observed directly due to a high attenuating column density, but can affect the chemistry of water.

Hydrides and ion molecules in dense star-forming regions are also of interest in red-shifted galaxies of the early Universe, where these species can be observed from the ground. The analysis and observational characteristics of these species in nearby objects are important for future observations.

In the following section and in Appendix A, where the details are given, we present the observations. Section 3 describes the method to derive column densities. Its quantitative results are tabulated in Appendix B. In Sect. 4 the results are analyzed and correlated in various ways; some details are available in Appendix C. Section 5 presents the discussion of the resulting constraints on FUV and X-ray irradiation. Three scenarios on the origin of the ionized molecules are discussed in Sect. 6. The conclusions can be found in Sect. 7. The correlation of HCO $^+$ with L_{bol} is interpreted in Appendix D.

2. Observations

A selection of 12 star-forming objects was observed with the Heterodyne Instrument for the Far Infrared (HIFI, de Graauw et al. 2010) on *Herschel*. The YSOs were selected from the list of the WISH key program (van Dishoeck et al. 2011) and are listed in Table 1. The low-mass sample contains mostly deeply embedded Class 0 sources and one more evolved Class I source. The high-mass sources were chosen to represent different stages of evolution, but the classification is too uncertain and the number is too small to expect clear evolutionary trends. The observed transitions were selected according to their expected intensity based on model calculations by Stäuber et al. (2005), Bruderer (2006) and Bruderer et al. (2010a). They are listed in Table 2 together with molecular and atomic parameters.

The objects are observed in six 4 GHz spectral settings for a total of typically 950 s each (including on and off source plus overhead) in the low frequency bands. In Band 4 (960–1120 GHz) the observing times are typically 1800 s for OH $^+$ and H $_3$ O $^+$, and 2400 s for H $_2$ O $^+$. The data are taken in dual beam switching (DBS) mode. In the DBS mode, the telescope is centered at the object coordinates given in Table 1 within a few arcsec, and the reference positions are offset by 3' on either side of the object. The only exception is S 140, observed in the framework of the WADI key program, where the C $^+$ observation is in on-the-fly (OTF) mode, and HCO $^+$, CH $^+$ (1–0) and CH in frequency switching mode (Dedes et al. 2010). Table C.1 contains the observing log.

Table 1. Observed objects and their parameters.

Object	RA [h m s]	Dec [° ' "]	Class	d [pc]	V_{LSR} [km s ⁻¹]	L_{bol} [$L_{\odot}$]	T_{bol} [K]	M_{env} [$M_{\odot}$]	References
NGC 1333 I2A	03:28:55.6	+31:14:37.1	LM 0	235	+7.7	35.7	50	5.1	1, 2, 10, 11
NGC 1333 I4A	03:29:10.5	+31:13:30.9	LM 0	235	+7.2	9.1	33	5.6	1, 2, 10, 11
NGC 1333 I4B	03:29:12.0	+31:13:08.1	LM 0	235	+7.4	4.4	28	3.0	1, 2, 10, 11
Ser SMM1	18:29:49.8	+01:15:20.5	LM 0	415	+8.5	99.0	39	52.1	1, 2, 10, 11, 12
L 1489	04:04:43.0	+26:18:57.0	LM I	140	+7.2	3.8	200	0.2	1, 2, 11, 10
NGC 7129 FIRS2	21:43:01.7	+66:03:24.0	IM	1250	-9.8	430	40	50	1, 3
W3 IRS5	02:25:40.6	+62:05:51.0	mIRb	2000	-38.4	1.7×10^5	370	424	1, 4, 7
NGC 6334 I	17:20:53.3	-35:47:00.0	HMC	1700	-7.7	2.6×10^5	100	500	1, 4, 8
NGC 6334 I(N)	17:20:55.2	-35:45:04.0	mIRq	1700	-3.3	1.9×10^3	30	3826	1, 4, 8
AFGL 2591	20:29:24.9	+40:11:19.5	mIRb	3300	-5.5	2.2×10^5	325	320	1, 4
S 140 IRS1	22:19:18.2	+63:18:46.9	mIRb	910	-7.1	1.0×10^4	85	100	1, 5, 6
NGC 7538 IRS1	23:13:45.3	+61:28:10.0	UCHII	2800	-56.2	1.3×10^5	40	433	1, 4, 9

Notes. Reference position chosen in J2000, distance d , systemic velocity V_{LSR} in the Local Standard of Rest, bolometric luminosity L_{bol} , bolometric temperature T_{bol} , and envelope mass M_{env} . The evolutionary stage is abbreviated for low-mass objects as LM 0 and LM I for Class 0 and I. IM stands for intermediate mass objects. High-mass objects are classified according to [van der Tak et al. \(2013\)](#), based on the scheme presented by [Molinari et al. \(2008\)](#): mIRq for mid-infrared quiet high-mass protostellar object (HMPO), mIRb for mid-infrared bright HMPO, HMC for hot molecular cores, and UCHII for objects reported to contain an ultra-compact HII region.

References. (1) [van Dishoeck et al. \(2011\)](#), confusion between NGC 6334 I and I(N) corrected; (2) [Kristensen et al. \(2012\)](#) and references therein; (3) [Crimier et al. \(2010\)](#); (4) [van der Tak et al. \(2013\)](#); (5) [Harvey et al. \(2012\)](#); (6) [Dedes et al. \(2010\)](#); (7) [van der Tak et al. \(2005\)](#); (8) [Sandell \(2000\)](#); (9) [Sandell & Sievers \(2004\)](#); (10) [San José-García et al. \(2013\)](#); (11) [Yildiz et al. \(2013\)](#); (12) [Dzib et al. \(2010\)](#).

Most of the lines in this exploratory survey are published for the first time. For the two high-mass regions AFGL 2591 and W3 IRS5, first results on CH⁺, OH⁺, H₂O⁺, CH, CH⁺, and H₃O⁺ were published before ([Bruderer et al. 2010b](#); [Benz et al. 2010](#)), but are reanalyzed and included here. C⁺ and HCO⁺ toward S 140 were studied by [Dedes et al. \(2010\)](#). The detection of SH⁺ toward W3 IRS5 was reported in [Benz et al. \(2010\)](#). Fore-ground clouds of some high-mass objects in this selection at velocities offset from the YSO were analyzed by [Indriolo et al. \(2015\)](#).

We used primarily the Wide Band Spectrometer, having a spectral resolution of 1.1 MHz, yielding a velocity resolution better than 0.7 km s⁻¹ over the entire HIFI range. The *Herschel* interactive processing environment (HIPE) 4.4 ([Ott 2010](#)) and higher was used for the pipeline and version 11.0 for data analysis. We resampled all spectra to 1 km s⁻¹, sufficient to resolve most observed lines. Some of the narrow CH and HCO⁺ lines were analyzed more precisely with the High Resolution Spectrometer yielding a resolution better than 0.36 MHz (0.2 km s⁻¹). The accuracy of the velocity calibration is estimated to be better than 0.1 km s⁻¹ ([Roelfsema et al. 2012](#)).

The antenna temperature was converted to main beam temperature, using the beam efficiencies of [Roelfsema et al. \(2012\)](#) and the forward efficiency of 0.96 for observations after 2011/01/01. A newer calibration of the data came out recently (HIFI memo Oct. 1, 2014), which increases the main beam intensities by around 13%. The analysis was not repeated since the conclusions would not change significantly as they depend mostly on relative intensities.

After visual inspection and defringing, the two polarizations were averaged. The continuum level was corrected for single sideband by halving the measured value. The calibration uncertainty is $\approx 10\%$ and limited to $<15\%$ in all bands ([Roelfsema et al. 2012](#)). For some sources in each band, a second

observation of equal length was made, using a local oscillator frequency shifted by 10 km s⁻¹ to identify interfering lines from the other sideband. All lines of interest could be attributed to a sideband without ambiguity.

Emission at the off-positions can interfere with the background elimination. This is mostly a problem for C⁺, which is abundant, has a low critical density, and thus is easily excited. All of the C⁺ detections were checked by comparing the spectra at the reference positions. For the C⁺ observation of S 140 the reference position was at a distance of 6.57 arcmin from IRS1 in an HII region in the direction of the illuminating star. Some questionable cases of CH⁺ and OH⁺ absorptions were also tested with no indications for off-source contamination.

3. Derivation of column density

The column density N_i of molecule i is calculated from the velocity integrated molecular line emission or absorption. For optically thin emission, the column density of the upper level of the transition, N_i^u , is

$$N_i^u = \frac{8\pi k \nu^2}{hc^3 A_{ul}} \int T_{\text{MB}} dV, \quad (1)$$

where A_{ul} is the Einstein-A coefficient, ν the frequency of the line and k the Boltzmann constant. For absorption, the column density N_i^l of the lower level l of the transition ($l \rightarrow u$) is

$$N_i^l = \frac{8\pi \nu^3 g_l}{c^3 A_{ul} g_u} \int \tau dV, \quad (2)$$

where g_u and g_l are the statistical weights of the upper and lower level. The optical depth is $\tau = \ln(T_{\text{cont}}/T_{\text{line}})$. T_{cont} is the single sideband continuum main-beam temperature. The contributions

Table 2. Frequency, upper level energy, E_u , and Einstein coefficient A_{ul} of observed lines.

Species	Transition	Frequency [GHz]	E_u [K]	A_{ul} [s ⁻¹]
CH ⁺	1–0	835.1375	40.08	6.4(–3)
CH ⁺	2–1	1669.2813	120.19	6.1(–2)
OH ⁺	1 _{1/2} –0 _{1/2}	1032.9979	49.58	1.4(–2)
	1 _{1/2} –0 _{1/2}	1033.0044	49.58	3.5(–3)
	1 _{1/2} –0 _{1/2}	1033.1118	49.58	7.0(–3)
	1 _{1/2} –0 _{1/2}	1033.1186*	49.58	1.8(–2)
o-H ₂ O ⁺	1 _{11/2} –0 _{00 1/2}	1115.1507	53.51	1.7(–2)
	1 _{11/2} –0 _{00 1/2}	1115.1862	53.51	2.8(–2)
	1 _{11/2} –0 _{00 1/2}	1115.2041*	53.51	3.1(–2)
	1 _{11/2} –0 _{00 1/2}	1115.2629	53.51	1.4(–2)
	1 _{11/2} –0 _{00 1/2}	1115.2983	53.51	3.5(–3)
o-H ₃ O ⁺	4 ₃ –3 ₃	1031.2995	232.2	5.1(–3)
SH ⁺	1 _{2(3/2)} –0 _{1(1/2)}	526.0387	25.25	8.0(–4)
	1 _{2(3/2)} –0 _{1(3/2)}	526.0479*	25.25	9.7(–4)
	1 _{2(3/2)} –0 _{1(3/2)}	526.1250	25.25	1.6(–4)
HCO ⁺	6–5	535.0616	89.9	1.3(–2)
CH	(³ / ₂) ₂ –(¹ / ₂) ₁₊	536.7611*	25.76	6.4(–4)
	(³ / ₂) ₁ –(¹ / ₂) ₁₊	536.7820	25.76	2.3(–4)
	(³ / ₂) ₂ –(¹ / ₂) ₀₊	536.7956	25.76	4.6(–4)
C ⁺	² P _{3/2} – ² P _{1/2}	1900.5369	91.21	2.3(–6)

Notes. The strongest (hyper)fine transition is labeled with an asterisk (*) symbol and used to set the velocity scale in Figs. A.1–A.8. The numbers in parentheses give the decimal power. Molecular and atomic data are taken from CDMS (Müller et al. 2001).

of different fine or hyperfine transitions are summed up according to their statistical weight. For a ground state line in absorption, the total column density, N_i , of a molecule i can be derived from

$$N_i = \frac{N_i^0 Q}{g_0}. \quad (3)$$

N_i^0 is the column density of the ground state, and g_0 its degeneracy. Q denotes the partition function at the excitation temperature T_{ex} . In the case of line emission from an upper level u , the total column density is

$$N_i = \frac{N_i^u Q(T_{\text{ex}})}{g_u} \exp\left(\frac{E_u}{kT_{\text{ex}}}\right), \quad (4)$$

where E_u is the upper energy level.

In some cases T_{MB} seems to reach values slightly below zero (such as for CH⁺ in NGC 6334 I, AFGL 2591, and NGC 6334 I(N)). For C⁺ toward W3 IRS 5 (Fig. A.7, third row, middle), the negative value exceeds the 15% calibration uncertainty of the continuum. Most likely it is an effect of an incomplete sideband correction (in all cases the continuum increases with frequency and the line was observed in the upper sideband). In these cases the integral $\int \tau dV$ cannot be determined. Its column density is given as a lower limit by assuming $\tau = 3$ in the region where the data would suggest $\tau > 3$. The limit on τ is necessary because the accuracy in the background continuum determines the accuracy of large τ . At $\tau = 3$ the background is reduced to 5%. Since the bottom of the absorption still has a

sharp peak in all cases, we infer that the absorption is not extremely saturated. Note that complete absorption requires that the absorbing region has equal or larger spatial extent than the background emission region behind it.

All column densities given in Table B.1 are beam-averaged values and are not corrected for a beam filling factor. There are two cases of column densities derived from absorption lines: (i) if the absorbing region is larger than the continuum source, the derived column density refers to the average along the line of sight through which the continuum is observed. (ii) If the absorbing region is smaller than the continuum emitting region and does not fill the beam, the derived column density underestimates the true value.

There are also two cases of lines in emission: (i) If the emitting regions are larger than the beam, the derived values refer to the sampled part of that region. (ii) If the source regions are smaller than the beam, the average column densities are beam diluted and depend on the ratios of the beam size to the source size. The absolute beam size (in AU) is given by the source distance and the frequency. When column densities are compared for species whose emission does not fill the beam, we may correct the column density for the difference in beam size, but not for the usually unknown source size. Equivalently, the line intensities in such comparisons may be normalized to a given distance (we use 1 pc), i.e., multiplied by the square of the distance. Note that this correction if applied to case (i) would spuriously introduce or enhance a correlation due to the relation between YSO luminosity and distance (to be discussed later, see Fig. C.3, bottom right). In reality, the distribution of the emission over the beam area is heterogeneous and is between the extreme cases of homogeneous and point-like. In the following, we refrain from corrections in general and indicate the exceptions.

4. Results and analysis

Figure 1 presents an overview of the detection of the observed lines. Most of the lines are detected in several sources; SH⁺ is found only toward one object. Only lines centered within $\pm 12 \text{ km s}^{-1}$ of the systemic velocity were considered. The range excludes gas at high velocity (“bullets”) associated with jets and most of the absorption lines caused by the diffuse interstellar clouds in the foreground. The analyzed lines are assumed to be associated with the YSO; exceptions are discussed. The observed line spectra are individually shown in Figs. A.1–A.8, where details on individual observations, such as line identification, significance of the detection, and line confusion are discussed. The line shapes are fitted with Gaussians. The results are given in Table B.1.

The accuracy of the reported column density is limited by the calibration error (<15%) of the line flux at low frequencies (for CH⁺ and HCO⁺) and by the background determination for the other lines. Similar error margins arise from the assumed excitation temperature T_{ex} , which is estimated from various sources with multiple transitions detected. The excitation temperature of CH⁺ in AFGL 2591, W3 IRS5, and NGC 6334 I was determined from a 1D slab model solving the radiative transfer equation along the line of sight and fitting the $J = 2-1$ and $J = 1-0$ lines for the same T_{ex} . The other fitted parameters were column density, velocity and line width (Bruderer et al. 2010b; Benz et al. 2013). The inferred values, 38 K for emission and 9 K for absorption, were subsequently assumed for the other sources. For OH⁺, the upper limit of T_{ex} derived from the non-detection of the (2–1) line in absorption is 40 K. We assumed 9 K. Analogously, we assumed 9 K for the H₂O⁺ absorption lines of the

	NGC 1333 2A	NGC 1333 4A	NGC 1333 4B	Ser SMM 1	L 1489	NGC 7129 FIR2	W3 IRS5	NGC 6334 I	NGC 6334 I(N)	AFGL 2591	S 140	NGC 7538 IRS1
CH ⁺	N blue	M blue	M blue	M blue		M red	M pcyg	M red	N red	M pcyg	N blue	M ipcyg
OH ⁺		M blue	M blue	M blue		M red	M pcyg	M b+r	M red	M pcyg	M red	M red
H ₂ O ⁺				M blue			M blue			M blue		N blue
H ₃ O ⁺							M red	N blue	M red	M red	N red	
SH ⁺							M blue					
HCO ⁺	M blue	M blue	M blue	M blue	M blue	M red	M red	M blue	M red	M blue	M red	M blue
C ⁺	M blue	M blue		M blue			M pcyg			M pcyg	M blue	
CH	N ipcyg	N ipcyg	N ipcyg	M+N ipcyg		M red	N red	N ipcyg	N red	N red	N red	N blue

Fig. 1. Overview of observed properties of the main line component. Color code: yellow=emission, green=absorption, beige=non-detection, white=not observed. “M” and “N” refer to medium-broad (5–20 km s^{−1}) and narrow (<5 km s^{−1}) line width; “blue”, “red” to the line shift, “b+r” to components in both directions, “pcyg” to P-Cygni, and “ipcyg” to inverse P-Cygni profiles. The quantitative values are reported in Tables A.1–A.3; line transitions and frequencies are given in Table 2.

Table 3. Assumed T_{ex} for reported column density, expected range of T_{ex} , and total error margins (factor) of the reported column density at the lower/upper limits of the expected T_{ex} range.

Species	Line mode	Assumed T_{ex} [K]	Expected T_{ex} [K]	Error factors col. density
CH ⁺	emission	38–44	19–75	1.8 1.2
CH ⁺	absorption	3–9	5–19	0.8 1.4
OH ⁺	emission	38	9–75	0.8 2.5
OH ⁺	absorption	3–9	3–19	0.8 1.4
H ₂ O ⁺	absorption	3–9	3–19	0.8 1.5
H ₃ O ⁺	emission	225	75–225	1.6 0.8
SH ⁺	emission	38	19–75	0.8 1.5
HCO ⁺	emission	38	19–75	5.7 0.5
C ⁺	emission	38	19–75	1.3 0.4
CH	emission	38	19–75	0.8 1.4
CH	absorption	6	3–9	0.85 1.2

ground-state. For the emission lines of SH⁺, HCO⁺, C⁺, and CH we assumed 38 K. The reasons are: SH⁺ in analogy to CH⁺; HCO⁺ (6–5) as reported by Morales Ortiz et al. (2014) toward the outer regions of NGC 6334 I; CH similar to the envelope component of OH as derived by Wampfler et al. (2011) for W3 IRS5. The adopted T_{ex} is given in Table B.1 for each case. For the error introduced by the assumption of T_{ex} , we explored a range of expected values. Table 3 summarizes the T_{ex} values, gives the expected T_{ex} range for each species and reports the resulting uncertainty in the column density at the range limits. In conclusion, the total error margin of the inferred column densities is typically

factors of 0.8–2 for emission lines, and factors of 0.8–1.5 for lines in absorption.

Figure 1 also gives a rough overview of line widths and line shifts. The line widths are classified according to Kristensen et al. (2012) for H₂O lines in low-mass objects. No broad line widths (>20 km s^{−1}) were observed in the lines selected here. More useful are average values for each species and class based on the Table B.1. They are given in Table 3. The indicated range does not represent the uncertainty but rather the spread of the distribution around the average. The line widths of intermediate and high-mass mass objects are on average larger than for low-mass objects (Figs. C.4–C.9, top). This trend holds for all lines and was noted by San José-García et al. (2013) also for C¹⁸O ($J = 10-9$ and $3-2$) (Table 3). The only exception is C⁺, for which the line width does not increase with luminosity or envelope mass (see also Fig. C.8, top row). Furthermore, the scatter in line width increases generally from low- to high-mass objects, again with the exception of C⁺.

4.1. Line classification

Based on Fig. 1 and Table 4, two classes of lines can be identified that generally comply with the following trends:

- The CH⁺, OH⁺, H₂O⁺, and C⁺ lines are mostly in absorption, preferentially blue-shifted and occasionally P-Cygni. Their line widths are generally medium-broad.
- The H₃O⁺, SH⁺, HCO⁺, and CH lines are mostly in emission. Their shifts relative to the systemic velocity are small (<1 km s^{−1}); positive and negative values are equally frequent. The line widths are generally narrow or have a narrow

Table 4. Averages of line width, velocity shift, and standard deviation of their distributions.

Species	Line width [km s ⁻¹]	Velocity shift [km s ⁻¹]	Comment
Low-mass objects			
CH ⁺	6.0 ± 0.8	-2.0 ± 1.2	main abs. comp.
OH ⁺	4.1 ± 4.0	-3.9 ± 1.0	main abs. comp.
o-H ₂ O ⁺	5.5	-3.5	one object, abs.
C ⁺	6.0 ± 0.9	-5.8 ± 1.2	main abs. comp.
H ₃ O ⁺	–	–	not detected
HCO ⁺	2.5 ± 0.6	-0.12 ± 0.12	narrow em. comp.
HCO ⁺	8.5 ± 3.3	0.20 ± 0.86	broad em. comp.
CH	1.0 ± 0.5	-0.35 ± 0.23	narrow em. comp.
	9.4	0.5	broad em. comp.
¹³ CO(10–9)	3.9 ± 3.0		narrow em. comp.
Intermediate and high-mass objects			
CH ⁺	8.2 ± 4.3	-0.1 ± 4.9	main abs. comp.
OH ⁺	8.7 ± 2.9	2.8 ± 7.1	main abs. comp.
o-H ₂ O ⁺	9.4 ± 4.1	-7.6 ± 3.3	blue abs. comp.
C ⁺	5.7 ± 1.0	1.5 ± 2.5	main em. comp.
H ₃ O ⁺	6.4 ± 2.7	1.2 ± 1.2	em. comp.
HCO ⁺	4.1 ± 1.1	-0.01 ± 0.46	narrow em. comp.
HCO ⁺	12.9 ± 8.0	0.59 ± 1.5	broad em. comp.
CH	3.9 ± 0.8	1.2 ± 2.0	narrow em. comp.
¹³ CO(10–9)	4.3 ± 0.8		narrow em. comp.

Notes. The accuracy of individual line widths and line shifts are better than 1 km s⁻¹. *First four lines:* blue-shifted molecules in absorption; *second group:* molecules preferentially in emission and unshifted; *bottom line:* ¹³CO (10–9) from San José-García et al. (2013) for comparison.

component, except for some cases of H₃O⁺ and the wing component of HCO⁺. The line widths of CH are extremely narrow and show inverse P-Cygni profiles in about half of the objects.

Figure 2 shows two examples of composites of the first class of lines. In the high-mass object (top) both the absorption line width and the line shift decrease from bottom to top, indicating a relation between mean velocity and turbulent velocity. The absorption feature of CH at -40 km s⁻¹ may also be related to the first group of molecules, but the dip in the CH spectrum at -46 km s⁻¹ is caused by another CH hyperfine absorption line (see Fig. A.8, bottom left). Absorption lines toward Ser SMM1 are superposed in Fig. 2 (bottom). We conclude that the absorption lines of our first molecular class are related to each other and originate in the same physical unit, but not at exactly the same place. Kristensen et al. (2013) report similar properties for the “offset component” of H₂O.

The second molecular class includes emission lines with narrow line width and a velocity shift that is small relative to the systemic velocity and unrelated to each other (as shown later in Fig. 4). Most of the shifts are within the accuracy of the measurements of molecular and systemic motions. The line width of H₃O⁺ is generally larger than that of the narrow component (peak) of HCO⁺, and CH in emission is even narrower than HCO⁺. An inverse P-Cygni profile as in the observed CH line toward some objects (see Fig. 1) was also reported

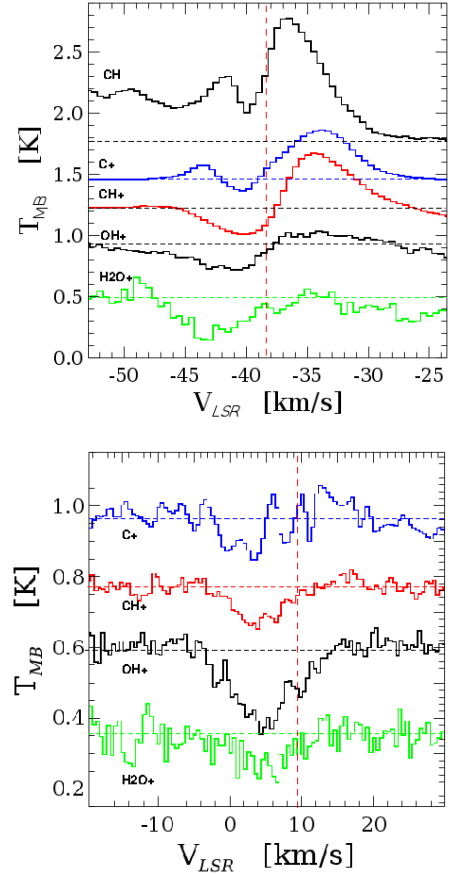


Fig. 2. *Top:* superposition of line profiles of various molecules of the first molecular class (see text) toward the high-mass object W3 IRS5. The line intensities are scaled and shifted to allow better comparison (CH: $T_{\text{MB}} + 1.5$ K; C⁺: $0.01T_{\text{MB}} + 1.4$ K; CH⁺: $0.25T_{\text{MB}} + 1.0$ K; OH⁺: $T_{\text{MB}} - 0.5$ K; H₂O⁺: $2T_{\text{MB}} - 3.7$ K). The systemic velocity of the YSO, -38.4 km s⁻¹, is indicated with a vertical red dashed line. *Bottom:* same as top for the low-mass object Ser SMM1 (C⁺: $0.5T_{\text{MB}} - 0.2$ K; CH⁺: $T_{\text{MB}} + 0.5$ K; OH⁺: $T_{\text{MB}} + 0.5$ K; H₂O⁺: $2T_{\text{MB}} - 0.45$ K).

for the narrow component of the H₂O ground-state lines in low-mass objects (Kristensen et al. 2012; Mottram et al. 2013; San José-García et al. 2016).

4.2. Correlations between different molecules

In the following, correlations are studied between line parameters of different molecules and objects with the aim to test the membership to the two classes defined above. We have used for analysis only the components likely to be associated with the YSO and omitted absorption components indicated with “DC” in Table B.1, for which confusion with diffuse clouds cannot be excluded. Where appropriate (column density, luminosity, mass, etc.), log-log scales are used for statistics to give equal weight to widely different objects. Quantitative studies use the Pearson correlation coefficient ρ to characterize the correlation and test its significance against the null hypothesis (applying the Student’s *t*-test at 99% confidence level). A linear fit (regression) quantifies the relation, and chi-square statistics is used to compare the scatter of different correlations. Correlation coefficients are only indicated in the figures where statistically significant.

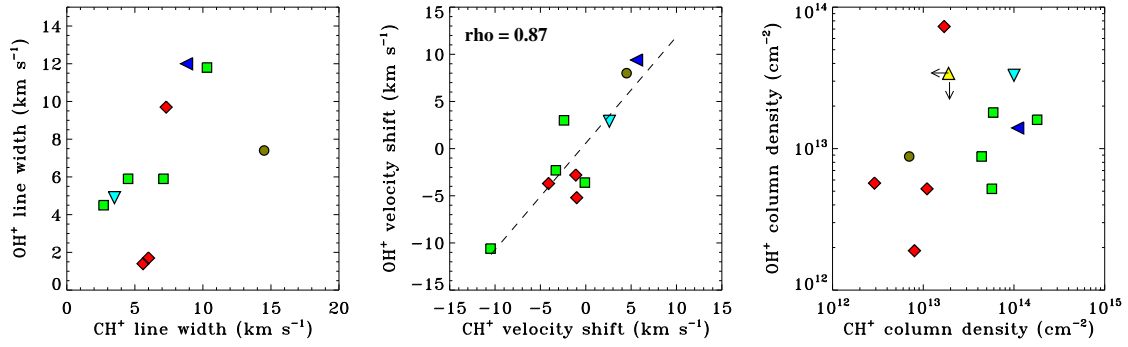


Fig. 3. Observed line parameters of OH⁺ (Table B.1) vs. observed line parameters of CH⁺. The symbols indicate different objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1). In this and subsequent figures uncertainties of individual points are typically the size of the symbols and up to a factor of two for column densities. The Pearson correlation coefficient ρ is given only for statistically significant relations.

Figure 3 displays the relations between the lines of the first class of molecules (medium width, blue-shifted absorptions). OH⁺ and CH⁺ correlate in line shift relative to the systemic velocity. The correlation extends from low-mass to high-mass objects. The scatter is within a few km s⁻¹. The apparent correlations between OH⁺ and CH⁺ in line width and column density are statistically not significant. The line parameters of C⁺ correlate less with CH⁺ than those of OH⁺, partly due to the P-Cygni line profiles of some sources.

The line shifts of OH⁺ and H₂O⁺ toward Ser SMM1, AFGL 2591 and W3 IRS5 correlate well (Table B.1). The averaged difference $\langle \delta V_{\text{H}_2\text{O}^+} - \delta V_{\text{OH}^+} \rangle$ is -0.27 km s⁻¹. The difference may result from the inaccuracy of the transition frequency of the H₂O⁺ line; it would amount to a correction of $+1.0$ MHz, to be added to the H₂O⁺ frequencies listed in Table 2. A correction was discussed by Neufeld et al. (2010) and Indriolo et al. (2015), who reported a value of $+5$ MHz.

The relations between the molecules of the second class are presented in Fig. 4. The line shifts of H₃O⁺ and HCO⁺ are correlated. Also the column densities of CH and HCO⁺ are well correlated. The relation between them is $N(\text{CH}) \propto N(\text{HCO}^+)^{1.7 \pm 0.3}$.

As expected, there is no correlation in line width and line shift of the second class of molecules with CH⁺ as representative of the first class (Fig. C.1). However, the column density of HCO⁺ (derived from an emission line) and the column density of CH⁺ (derived from absorption) are well correlated ($\rho = 0.83$). CH and CH⁺ are also correlated in column density. The relations are not linear, but power laws: $N(\text{HCO}^+) \propto N(\text{CH}^+)^{0.7 \pm 0.2}$, and $N(\text{CH}) \propto N(\text{CH}^+)^{1.5 \pm 0.3}$.

The HCO⁺(6–5) line was fitted by a broad and a narrow Gaussian, representing high and low turbulent velocities. The average line widths are 11.0 ± 1.0 km s⁻¹ and 3.4 ± 1.3 km s⁻¹ for the broad and narrow component, respectively. The distribution of the two components in line width can be fitted with the linear regression $\Delta V_{\text{broad}} = 3.1(\pm 0.5)\Delta V_{\text{narrow}}$ (Fig. C.2). There is no correlation of the line shifts, which scatter around zero. The column densities fitted to the line peak and the wings correlate well, the narrow one being two times higher on average, indicating that the narrow component amounts to two thirds of the total. Thus the two HCO⁺ components have many similarities and they seem to be physically related. Therefore the column densities are added in Table B.1 and the two components will not be distinguished in the following.

San José-García et al. (2013) have analyzed the ¹³CO ($J = 10-9$) line in a similar way. The average line widths towards the

objects in common are 4.1 ± 1.9 km s⁻¹ and 12.6 ± 7.1 km s⁻¹ for the narrow and broad component, respectively. Their average ratio is 3.1 ± 1.0 , the same as found for HCO⁺. The agreement in velocity dispersion between ¹³CO (10–9) and our HCO⁺(6–5) line (Table 3) suggests a common region of origin.

4.3. Relations between molecular lines and object parameters

Here we summarize the most prominent results on the relations between lines and objects. First, we note that the source parameters are not independent of each other. Already Bontemps et al. (1996) reported an observational relation between bolometric luminosity and envelope mass for Class 0 and Class I low-mass objects. The relation appears clearly in our sample, but now also includes intermediate and high-mass objects and covers five orders of magnitude (Fig. C.3 top left); the result is

$$M_{\text{env}} \approx 1.1(L_{\text{bol}})^{0.54(\pm 0.12)} \quad (5)$$

using solar units [$M_{\odot}$] and [$L_{\odot}$]. The largest deviations from the regression line are NGC 6334 I(N) (a mid-IR quiet object in early evolutionary phase) having the largest envelope mass in the sample, and L 1489, an evolved (Class 1) object with a small envelope mass. Both deviations are consistent with the evolutionary trend reported by Bontemps et al. (1996) and Molinari et al. (2008) of increasing $(L_{\text{bol}})^{0.6}/M_{\text{env}}$ with time.

The bolometric temperature is not related to either envelope mass, luminosity or distance (Fig. C.3). The correlation of luminosity (and thus envelope mass) with distance is conspicuous. It is clearly a selection effect and must be taken into account for the interpretation of column densities toward unresolved sources (see end of Sect. 3).

In general, the observed column density of all molecules increases with luminosity. This is the case for column densities based both on absorption and emission. The column density of CH⁺ has a correlation coefficient of $\rho = 0.87$ with luminosity (Fig. C.4, bottom left). The correlation of OH⁺ with luminosity is not statistically significant. Especially Ser SMM1, which shows exceedingly deep and broad absorptions (Fig. A.3, second row, left), is an outlier. As envelope mass correlates with luminosity (Fig. C.3, top left), it is not surprising that the column densities of all molecules (except H₃O⁺ and OH⁺) also correlate with envelope mass with comparable coefficients (Figs. C.4–C.9).

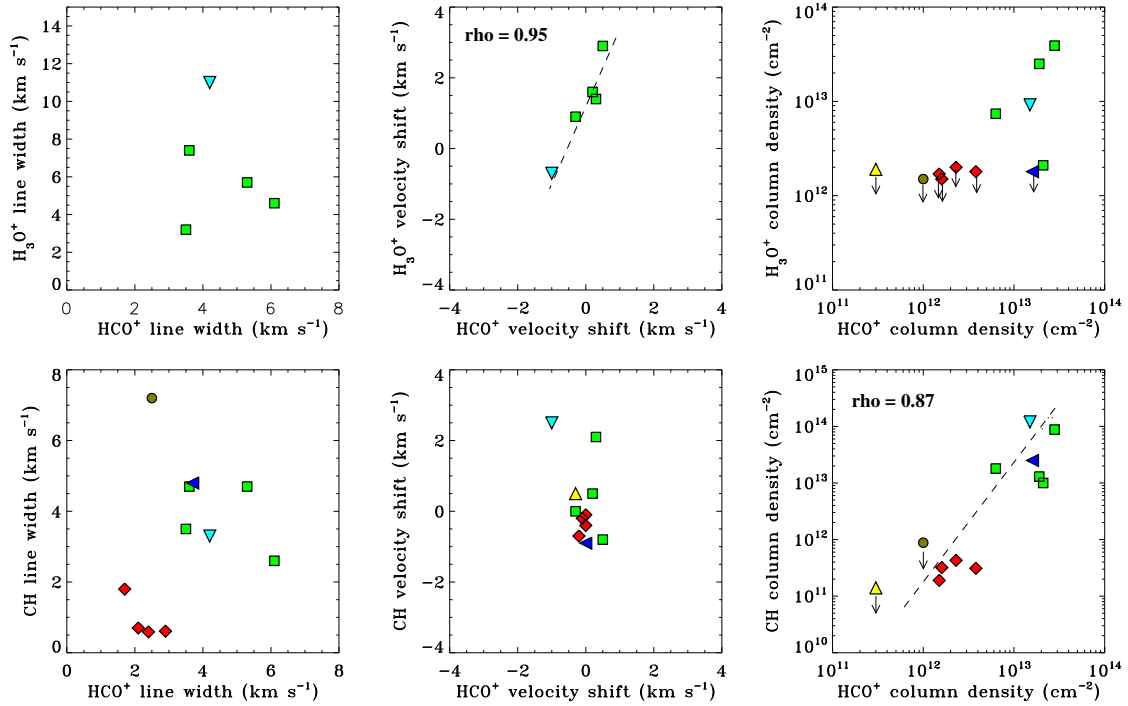


Fig. 4. Observed emission line parameters of H_3O^+ and CH vs. observed line parameters of HCO^+ (narrow component) for line width and shift relative to the systemic velocity, and total for column density. For the notation of the symbols see Fig. 3.

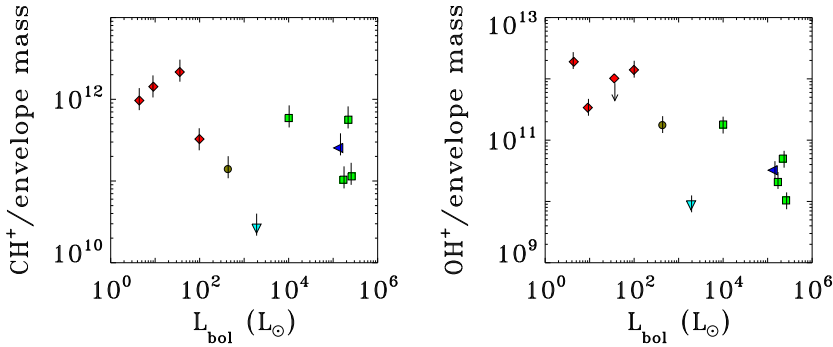


Fig. 5. Proxy CH^+ abundance. *Left:* the ratio of CH^+ column density (cm^{-2}) to envelope mass (in units of $M_\odot$) versus bolometric luminosity (in units of $L_\odot$). *Right:* same for OH^+ . For the notation of the symbols see Fig. 3. The error bars show the margins given in Table 3 for the column density and do not include the uncertainty in the envelope mass.

In Fig. 5 the CH^+ column density as determined from absorption is divided by the envelope mass (Table 1). For optically thin emission this ratio is proportional to the ratio of the total number of CH^+ ions divided by the total number of hydrogen atoms. With the simplification that the CH^+ absorbing region has the same size as that of the H_2 region, this ratio is a proxy for the fractional CH^+ abundance averaged over the YSO envelope. The ratio is shown vs. luminosity in Fig. 5 (left). There is no statistically significant correlation with L_{bol} ($\rho = 0.29$), but the low-mass objects ($<100 L_\odot$) have a factor of four larger CH^+ abundance on average compared to the intermediate- and high-mass objects. The OH^+ abundance (Fig. 5 right) shows a stronger trend ($\rho = 0.54$) and a factor of 30 enhancement on average at the low-mass objects. The same inequality between low- and high-mass objects results if instead of the envelope mass the ^{13}CO ($J = 10-9$) and C^{18}O ($J = 3-2$) line intensities as reported by San José-García et al. (2013) are used.

There are no indications for opacity effects in CH^+ and OH^+ such as rounded or flat peaks in the line shape that could explain Fig. 5. Since FUV ionization, heating, and chemistry are surface effects, but the envelope mass is in a volume, the result may be interpreted by a higher surface-to-volume ratio of

smaller objects. The very low value for the high-mass mid-IR quiet NGC 6334 I(N) (light blue triangle down in both CH^+ and OH^+ in Fig. 5) then would indicate that in massive cold envelopes of high-mass YSOs there are large regions where these molecular ions are not enhanced.

4.4. Correlation of HCO^+ with object parameters

The correlation between the HCO^+ (6–5) column density and bolometric luminosity (Fig. C.7) is among the best. The uncorrected correlation coefficient is 0.83 and the chi-square value is 12.6 relative to the regression line in log-log scale. Radiative transfer modeling of the high-mass AFGL 2591 (Bruderer et al. 2009) and interferometric observations of HCO^+ in the (3–2) transition towards low-mass YSOs indicate a source diameter $\leq 30''$ (Hogerheijde et al. 1997). Morales Ortiz et al. (2014) report optically thick HCO^+ (6–5) emission for NGC 6334 I and a size of $40 \pm 6''$ for the outer envelope. This suggests that the HCO^+ (6–5) emission originates predominantly from an optically thick surface (see also Appendix D). We assume that the emission region is effectively

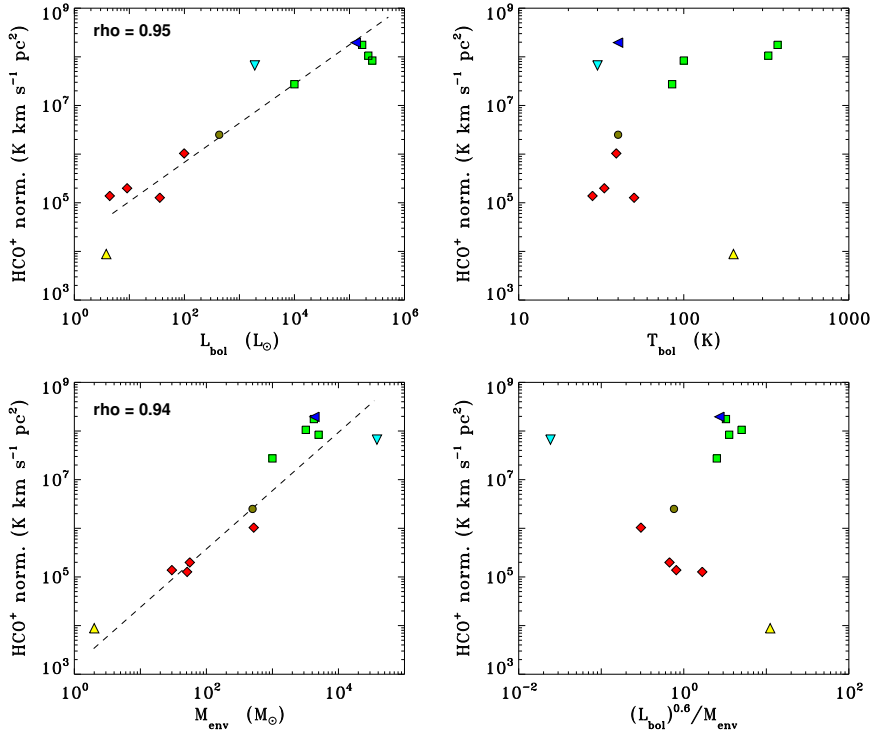


Fig. 6. Integrated line intensity, $\int T_{\text{MB}} dV$, of HCO^+ normalized to 1 pc vs. object parameters given in Table 1. Notation: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

smaller than the *Herschel* beam at 535 GHz (HPBW 44'') for all objects. Thus the HCO^+ (6–5) line luminosity must be corrected for the varying beam dilution at different distances. This is done by normalizing the line luminosity to the same distance (see end of Sect. 3).

The velocity-integrated line intensity of HCO^+ (6–5), normalized to a distance of 1 pc, is depicted in Fig. 6. Its correlations with bolometric luminosity and envelope mass are remarkably good. L 1489, the Class I object, and NGC 6334 I(N), the high-mass object with highest envelope mass, have the largest deviations from the linear regression line (Fig. 6, top left). There is no correlation with bolometric temperature (Fig. 6, top right).

Correcting the integrated line intensity of the HCO^+ , I_{HCO^+} in $[\text{K km s}^{-1}]$, yields a line luminosity, $L_{\text{HCO}^+}^{\text{norm}}$, normalized to a distance of 1 pc. This increases the correlation coefficient with bolometric luminosity to 0.95; the chi-square value reduces to 4.0, indicating that the data points are close to the regression line. The linear regression in log-log scale amounts to a power-law relation

$$d_{\text{pc}}^2 I_{\text{HCO}^+} \propto L_{\text{HCO}^+}^{\text{norm}} \propto (L_{\text{bol}})^{0.76 \pm 0.08}. \quad (6)$$

This tight relation can be interpreted by noting that the luminosity of an optically thick line depends on the one hand on the radius of the line photosphere, which increases with L_{bol} . On the other hand, the temperature of the line photosphere also follows a power law with L_{bol} . The properties of the dust radiative transfer become self-similar (Ivezić & Elitzur 1997) in all models, yielding the observed power-law relations between the relevant parameters. The details are given in Appendix D.

A similar explanation may hold for other optically thick emission lines reported here and elsewhere which correlate between column density and L_{bol} . The numerical modeling described in Appendix D indicates that the power-law exponent in the relation between line and bolometric luminosities depends on the location of the line photosphere in relation to the inner and outer envelope radius.

5. Chemistry constraining FUV and X-rays

Having characterized the observational properties of the hydrides, we investigated their chemistry in order to explore the origin of the observed absorption or emission within the protostellar envelope and to use them as diagnostics of FUV and X-ray emission. There is an extensive literature on the chemistry of ionized hydrides, especially on CH^+ and OH^+ , in diffuse clouds (see Introduction for references). Although some aspects of the chemistry are similar, star-forming regions differ physically from diffuse clouds. YSOs are expected to be more inhomogeneous in density, temperature and irradiation and may have internal sources of ionizing radiation.

5.1. Chemical modeling

Molecular abundances may be used to probe the internal radiation fields of FUV and X-rays, which add to the interstellar UV and cosmic ray ionization. To explore irradiated hydride chemistry in parameter space, abundances were calculated from chemical models for given values, assuming chemical equilibrium, a given density, temperature, FUV and X-ray irradiation (Stäuber et al. 2005). The temperature is kept as a free parameter. In the bulk of the dense envelope, gas and dust temperatures are well coupled; only along the outflow cavity walls are gas temperatures higher than dust temperatures in a narrow boundary layer (e.g., Bruderer et al. 2009; Visser et al. 2012). The sublimation of ices is controlled by the dust temperature, whereas the rates of gas-phase reactions depend on the gas temperature.

The models use the chemical gas-phase reaction network from the UMIST 06 database (Woodall et al. 2007), adopted and updated by Bruderer et al. (2009). The sublimation of the most important ices is included (H_2O , CO_2 , and H_2S at $T_{\text{dust}} > 100$ K; H_2CO , and CH_3OH at $T_{\text{dust}} > 60$ K). The cosmic ray ionization rate of H_2 is assumed to have the value $5 \times 10^{-17} \text{ s}^{-1}$ (e.g., van der Tak & van Dishoeck 2000). The elemental abundances are taken from Stäuber et al. (2005), Table A.1. They practically

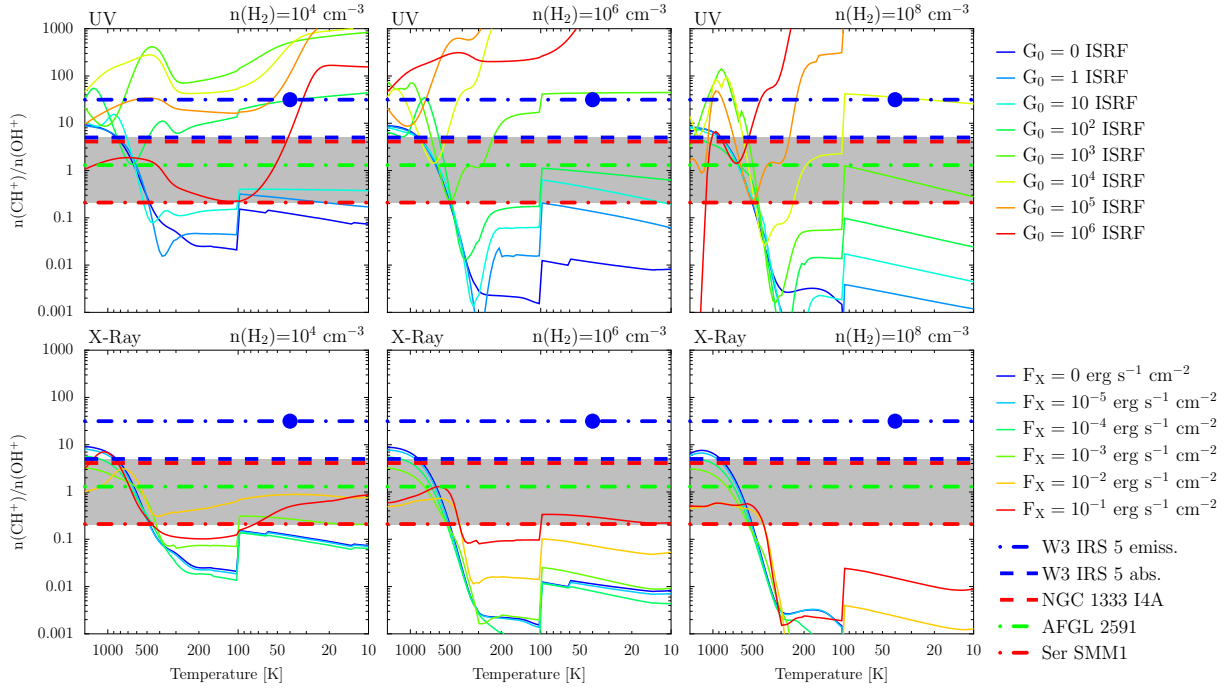


Fig. 7. Column density ratio of CH^+ to OH^+ vs. gas temperature for several chemical toy models (densities given above the figures) for FUV irradiation without X-rays (*top*) and X-ray irradiation without FUV (*bottom*). The radiation levels are color coded. The range of observed values for absorption lines is shaded. The excitation temperature for CH^+ from 1D slab model fitting of emission lines (Table B.1) is indicated with a blue dot.

agree with [Anders & Grevesse \(1989\)](#) except for the O abundance that is lower by $\sim 40\%$ and the same as in [Asplund et al. \(2009\)](#). These models are not intended to quantitatively reproduce the observations, but instead they are single-point toy models to roughly constrain density, gas temperature, and FUV and X-ray irradiation for the parameter ranges that are expected in protostellar envelope models.

The parameter range of toy models (such as that shown in Figs. 7–9) is guided by the assumption that the FUV irradiation originates externally or from the central protostar(s) and that the X-ray fluxes are in the range observed from low-mass Class I and II objects ([Feigelson & Montmerle 1999](#)). The densities were chosen at three levels to reflect the conditions at the outer edge of the envelope, the average envelope and out-flow walls, and the inner envelope and disk atmosphere. Physical models for the envelopes of our sources giving their temperature and density are presented in [Kristensen et al. \(2012\)](#) and [van der Tak et al. \(2013\)](#) (see Figs. D.1 and D.2). We note that the FUV flux, G_0 , and gas temperature are connected through FUV absorption. A gas temperature below 300 K is realistic only for $G_0 < 100$ ISRF at $n = 10^4 \text{ cm}^{-3}$; and for $G_0 < 1000$ ISRF at $n = 10^8 \text{ cm}^{-3}$ ([Visser et al. 2012](#)). ISRF denotes the FUV flux in terms of the standard interstellar radiation field, $1.6 \times 10^{-3} \text{ erg cm}^{-2} \text{ s}^{-1}$ ([Habing 1968](#)).

5.2. CH^+ to OH^+ ratio

Figure 7 shows the model abundance ratio of CH^+ to OH^+ as a function of gas temperature for various types and strengths of irradiation. The range of G_0 given in Table 5 for the emission lines is consistent with the assumption of a gas temperature < 100 K. Similar studies have been made at lower molecular density to interpret observations of diffuse clouds ([Bruderer et al. 2010b](#); [Gerin et al. 2010a](#); [Hollenbach et al. 2012](#)).

Table 5. Ratios of mean column densities according to Table B.1.

Object	$\frac{N(\text{CH}^+)}{N(\text{OH}^+)}$	$\frac{N(\text{OH}^+)}{N(\text{H}_2\text{O}^+)}$	$\frac{N(\text{C}^+)}{N(\text{CH}^+)}$
NGC 1333 I2A	>2.1	–	43 000
NGC 1333 I4A	4.1	>0.39	≤ 16 000
NGC 1333 I4B	>0.48	–	< 170 000
Ser SMM1	0.21	≥ 15.5	3100
L 1489	–	–	–
NGC 7129 FIRS2	0.75	>1.5	–
W3 IRS5	5.0	2.7	>130 000
W3 IRS5 em.	31.5	–	>580 000
NGC 6334 I	1.8	>124.0	–
NGC 6334 I(N)	1.4	>36.1	–
AFGL 2591	1.3	19.4	>28 000
S 140	1.8	>13.6	≥ 8800
NGC 7538 IRS1	0.48	>24.5	–

Notes. The values are derived from lines observed in absorption except where labeled “em.” The – sign is set where both lines are undetected.

The formation of CH^+ through $\text{C}^+ + \text{H}_2 \rightarrow \text{CH}^+ + \text{H}$ is endothermic by 4640 K, which enhances the ratio above 300 K. At low irradiation and gas temperatures below about 230 K, the abundances of CH^+ and OH^+ are below 10^{-12} relative to H_2 , and the ratio decreases with higher density. The CH^+ to OH^+ ratio is an excellent tracer of FUV at a gas temperature $T < 300$ K (top row of Fig. 7), as indicated by the systematic increase in CH^+/OH^+ up to $G_0 = 10^3$ ISRF. The evaporation of H_2O at dust temperatures above 100 K reduces the abundance of CH^+ more than OH^+ and causes a step in CH^+/OH^+ at that temperature ([Stäuber et al. 2005](#)).

The ratios of molecules calculated from observed column densities (Table B.1) of the first class are listed in Table 5. Some

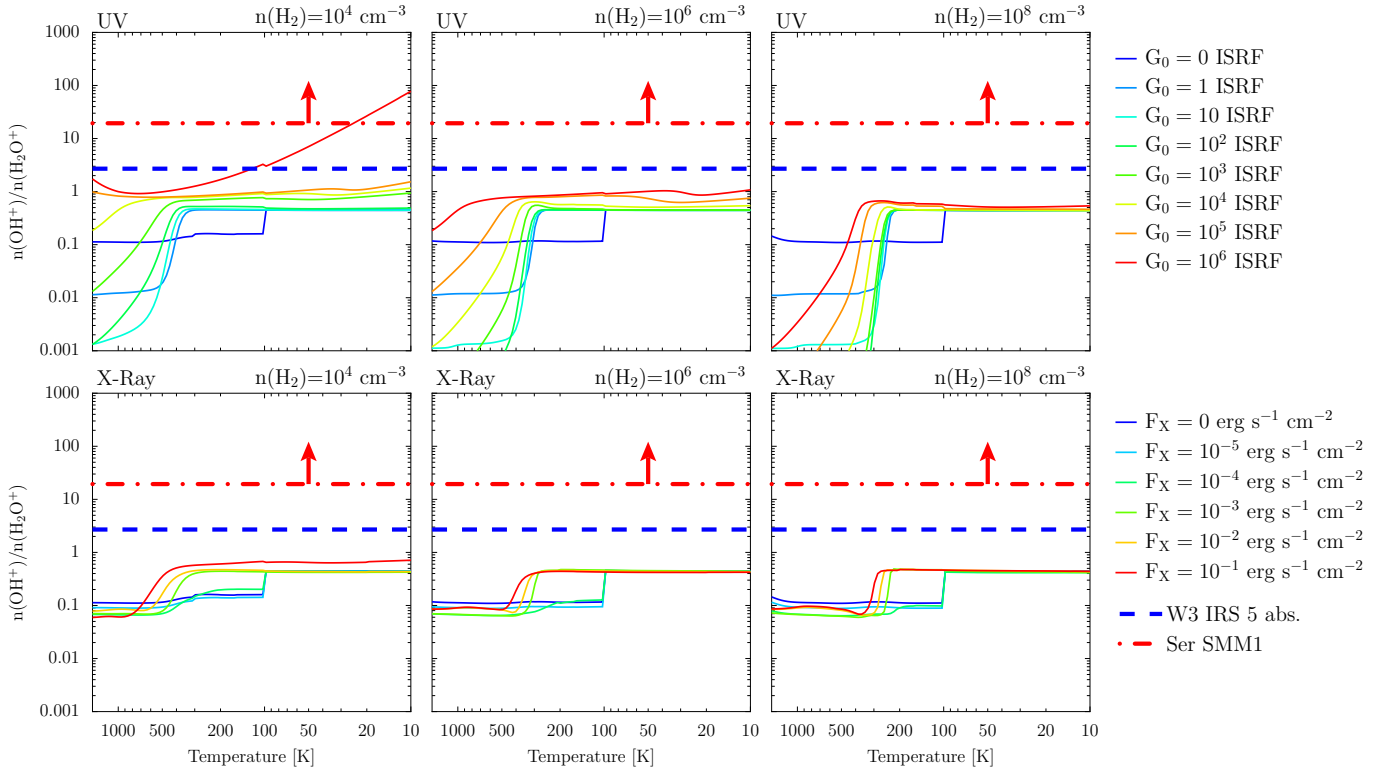


Fig. 8. Same as Fig. 7 for column density ratio of OH^+ to H_2O^+ . The ratio given for Ser SMM1 is a lower limit because of the only tentative detection of H_2O^+ .

observed values taken from Table 5 are indicated in Fig. 7 with horizontal lines. They are in the range from 0.2 to 5.0 for lines observed in absorption. The only ratio available from emission lines (toward W3 IRS5) yields a value well above that range. In contrast to the FUV case, the CH^+/OH^+ ratio is less sensitive to the value of the X-ray flux (bottom row of Fig. 7).

The CH^+/OH^+ ratio may be underestimated in our simplified modeling because of two effects. Vibrationally excited H_2 reacts exothermically with C^+ , favoring CH^+ formation (Agúndez et al. 2010) and enhancing the CH^+ column density by a factor of two (Zanchet et al. 2013). Another factor of two may result from formation pumping, which is more important for CH^+ (Bruderer et al. 2010a, Table 9) than for OH^+ (Gómez-Carrasco et al. 2014). However, temperature and irradiation affect the CH^+/OH^+ ratio more, thus justifying the qualitative conclusions drawn above.

Figure 7 suggests that there are two temperature ranges that can match the observed CH^+ to OH^+ ratios. At temperatures above about 500 K, where $\text{O}+\text{H}_2 \rightarrow \text{OH} \rightarrow \text{H}_2\text{O}$, no irradiation is required to achieve the observed values. The second possible range is $T < 300$ K, which is consistent with the rather low excitation temperatures of even the emission lines derived from full chemical and radiation transfer modeling (e.g., Bruderer et al. 2010b). In case of low density ($n(\text{H}_2) \approx 10^4 \text{ cm}^{-3}$), the required G_0 value is between 0 and a few times 10 ISRF for all objects seen in absorption. In the case of high density ($n(\text{H}_2) \approx 10^6 \text{ cm}^{-3}$ and higher), the FUV range is from $G_0 = 1$ to a few 10^5 ISRF. For both low- and high-mass YSOs, the envelope densities at the half-power beam radius (HPBR) of *Herschel* at 1 THz are typically $\sim 10^5 \text{ cm}^{-3}$. Densities at the cavity wall can be lower, but are unlikely to be so by more than an order of magnitude. On the other hand, shocks can compress the walls and actually lead to higher densities. Thus, the entire range of 10^4 – 10^6 cm^{-3} is

plausible. The lack of emission suggests that these hydrides are not present in the innermost part of the envelope where densities can be as high as 10^8 cm^{-3} .

In the following we discuss five well-observed cases. The inferred G_0 ranges for these sources, in the temperature range of 10–100 K, are given in Table 5, assuming the density at the HPBR. The uncertainty of the density is assumed to be smaller than a factor of two and is included in the G_0 range.

1. In the low-mass object NGC 1333 I4A a protostellar X-ray luminosity $L_x = 10^{32} \text{ erg s}^{-1}$, only geometrically attenuated, would yield a flux of only $5.3 \times 10^{-3} \text{ erg s}^{-1} \text{ cm}^{-2}$ at the HPBR. According to the toy models (Fig. 7), this is not sufficient to reproduce the observed CH^+/OH^+ ratio at the HPBR density according to the envelope model (Kristensen et al. 2012). The interpretation by FUV irradiation, on the other hand, needs an FUV flux $G_0 \approx 300$ ISRF at the HPBR density and at a gas temperature of 30 K.
2. Similarly, to reproduce the observed CH^+/OH^+ ratio toward Ser SMM1, X-rays emitted by the protostar could provide a flux of $< 10^{-2} \text{ erg s}^{-1} \text{ cm}^{-2}$ at the HPBR and are unlikely according to Fig. 7. In contrast, an FUV flux of only a few ISRF is required due to the low ratio observed.
3. Based on interferometric observations of sulfur-containing molecules, Benz et al. (2007) have proposed that the high-mass object AFGL 2591 is an X-ray emitter. Corrected for the updated distance (Table 1), the estimated X-ray luminosity amounts to $L_x = 9 \times 10^{32} \text{ erg s}^{-1}$. At *Herschel*'s HPBR, the X-ray luminosity, geometrically attenuated, would yield a flux of $2.6 \times 10^{-4} \text{ erg s}^{-1} \text{ cm}^{-2}$, which is not sufficient to reproduce the observed ratio (density model of van der Tak et al. (2013)). On the other hand, van der Tak et al. (1999) suggest the central object to be a

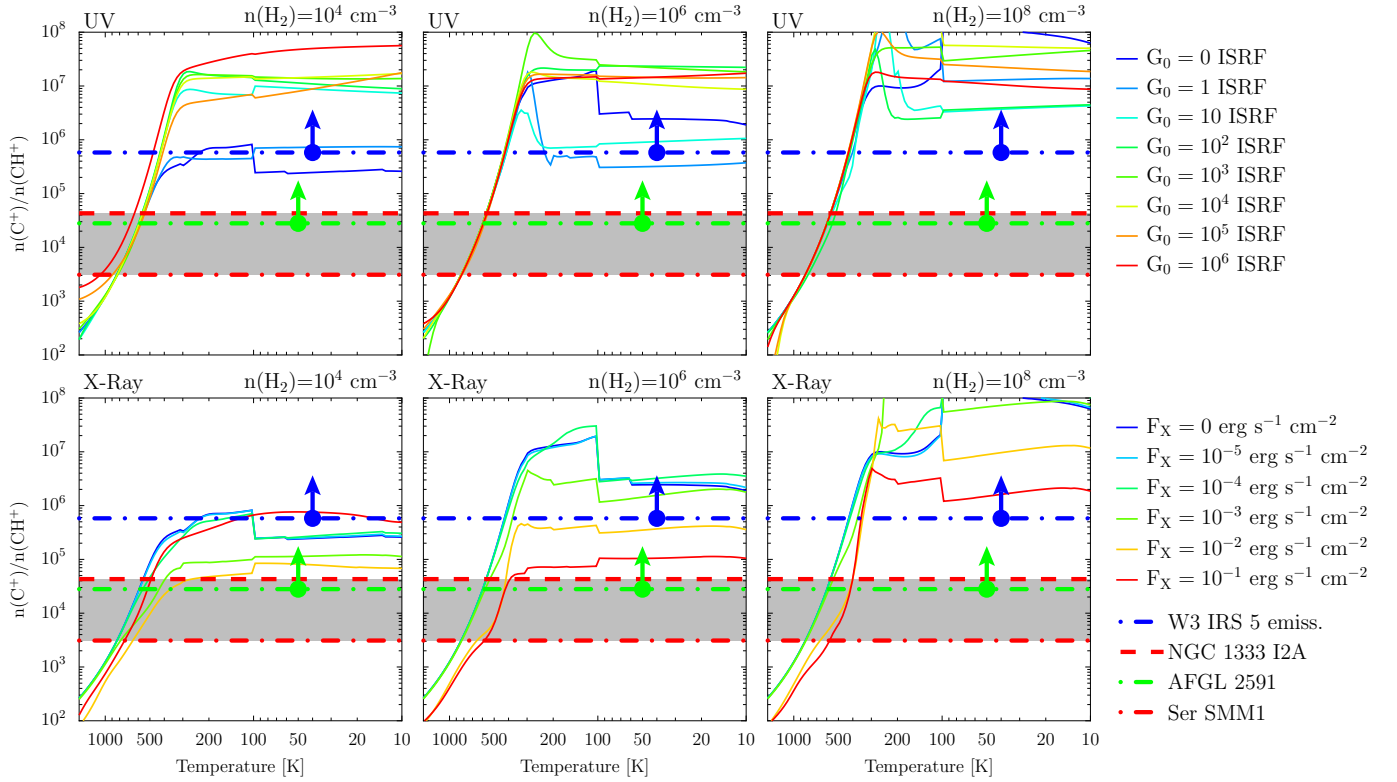


Fig. 9. Same as Fig. 7 for column density ratio of C^+ to CH^+ .

B star with an effective temperature of 3×10^4 K having a luminosity of $2.2 \times 10^5 L_\odot$ (corrected for new distance), emitted mostly in FUV. If only geometrically attenuated, it yields $G_0 = 1.5 \times 10^5$ ISRF at the *Herschel* HPBR, three orders of magnitude higher than required. Thus an attenuated FUV flux can readily reproduce the observed ratio.

4. The conclusion that FUV dominates over X-rays is similar for the high-mass object W3 IRS5, for which the reported X-ray luminosity is 5×10^{30} erg s $^{-1}$ (Hofner et al. 2002). At *Herschel*'s HPBR, this X-ray flux is geometrically attenuated to a level of 4×10^{-6} erg s $^{-1}$ cm $^{-2}$, which is not sufficient to produce the observed CH^+/OH^+ ratio. The FUV flux required to match observations at the HPBR density and 30 K amounts to $G_0 \approx 90$ ISRF.
5. For W3 IRS5 in emission, the excitation temperature of CH^+ was determined from 1D slab modeling, which indicates a value of 38 K (Table B.1). It is represented in all plots of Fig. 7 by a blue dot.

5.3. OH^+ to H_2O^+ ratio

Figure 8 shows the modeling results for the OH^+/H_2O^+ ratio. It generally decreases with temperature. Contrary to the CH^+/OH^+ ratio, the observations clearly exclude high temperatures. Thus combining the two observed ratios, the hot temperature range is ruled out.

In the absence of irradiation, the model ratio of OH^+ to H_2O^+ (Fig. 8) is around 0.4 for temperatures < 100 K. In the parameter range presented in Fig. 8, the OH^+/H_2O^+ ratio is near unity or below for all irradiation fluxes except very high G_0 at low density. The value of ≥ 15.5 observed for the low-mass object Ser SMM1 can only be reproduced at a density of 10^4 cm $^{-3}$ and an FUV flux G_0 around 10^6 , or an X-ray flux of 10 erg s $^{-1}$ cm $^{-2}$ (not shown

in Fig. 8). Both fluxes exceed the expected upper limits for low-mass objects at the *Herschel* half-power beam radius.

The requirement for the high-mass object W3 IRS5 OH^+/H_2O^+ ratio can only be met with $G_0 > 10^6$ at a density of 8×10^4 cm $^{-3}$. The required X-ray flux of 10 erg s $^{-1}$ cm $^{-2}$ is far above the observed value from Hofner et al. (2002) if the emitting X-ray source is near the center of the YSO. Thus, we cannot explain the observed ratios with irradiation of the central object(s) and the density expected from envelope models.

As OH^+ is mainly destroyed through reactions with H_2 to form H_2O^+ , a high OH^+ to H_2O^+ abundance ratio points at a low density. Indeed, in diffuse clouds OH^+/H_2O^+ ratios of 1–15 have been observed, suggesting densities < 100 cm $^{-3}$ with a molecular fraction of only a few percent (Gerin et al. 2010b; Indriolo et al. 2015). Such low densities are unlikely to be present in protostellar systems on the scales covered by the *Herschel* beam. We therefore also considered the alternative scenario of non-equilibrium chemistry in dissociative shocks which may enhance both OH and OH^+ in star-forming regions (Neufeld & Dalgarno 1989; Kristensen et al. 2013) (see Sect. 6).

5.4. C^+ to CH^+ ratio

The modeled C^+/CH^+ ratio (Fig. 9) is low at high temperature due to the rapid formation of CH^+ above 300 K (see above) and strongly increases from 2000 K to 300 K. For temperatures below 300 K, the ratio traces well the irradiating FUV and X-ray fluxes. X-rays reduce the ratio. For low irradiation, the ratio strongly increases with increasing density.

The observed ratio of C^+ to CH^+ is generally lower for low-mass objects (Table 5). For Ser SMM1 and NGC 1333 I2A, it is below the values predicted by the models except for temperatures around 900 and 500 K, respectively (Fig. 9).

Table 6. *Herschel* HPBR(10.7'' at 1 THz) at the source distance, density of envelope model at HPBR, line mode, and derived FUV flux range at the site of the molecules inferred from the observed ratio.

Object	Radius [AU]	Density [cm ⁻³]	Line mode	G_0 ISRF
NGC 1333 I4A	2500	1.3×10^6	abs.	200–400
Ser SMM1	4400	6.0×10^5	abs.	2–8
AFGL 2591	35 000	7.0×10^4	abs.	20–80
W3 IRS5	21 000	1.1×10^5	abs.	80–200
W3 IRS5	21 000	1.1×10^5	em.	300–600

Several interpretations are possible: (i) a gas temperature higher than 500 K may be expected from FUV irradiation of gas along the outflow walls (e.g., Visser et al. 2012). (ii) The two molecular regions may not be co-spatial. If the C⁺ absorbing or emitting region is more extended than the CH⁺ absorbing region, but smaller than the beam and the continuum source, the true C⁺/CH⁺ ratio of the column densities in the co-spatial regions would be larger. (iii) The observed C⁺ line is self-absorbed in high-mass objects, thus column densities are underestimated (see Appendix A). (iv) The H₂ density may be lower than 10⁴ cm⁻³ in the C⁺ emitting region and be comparable to intercloud conditions. (v) Alternatively, chemistry in a shock may again play a role.

In conclusion, CH⁺/OH⁺ are the most reliable ratios and their comparison with models suggests that substantial protostellar FUV fluxes are needed at the site of the molecules to fit the observations. This statement is based on the assumption that the molecular hydrogen density is approximately given by the source models at the *Herschel* HPBR. X-ray emission cannot play a role unless it originates closer to the line absorption/emission region than the protostar.

5.5. The case of X-ray irradiation

X-rays are effective destroyers of water in the inner envelope (Stäuber et al. 2006), so it is important to put limits on their flux in cases where no direct X-ray observations are possible. In general, we find no evidence for strong X-ray emission based on the observations of the hydrides presented here. This could be viewed to be in contradiction with Stäuber et al. (2007), who find three indicators for X-rays: CO⁺, CN, and SO⁺. The abundances of the first two molecules can also be explained by FUV irradiation of outflow cavity walls (Bruderer et al. 2010a), whereas the sulfur chemistry is in general poorly understood and may not be co-spatial.

The non-detection of H₃O⁺ toward the low-mass objects imposes limits on their X-ray luminosity. According to Stäuber (2006) (Table 6.5), who derived the H₃O⁺ line intensities for the prototypical Class 0 object IRAS16293-2422, our observed upper limits (<0.14 to <0.19 K km s⁻¹) suggest that the X-ray luminosities are <10³⁰ erg s⁻¹. For the prototypical Class I object TMC1 however, an X-ray luminosity of 10³¹ erg s⁻¹ is predicted to produce a line intensity below the sensitivity of these H₃O⁺ observations (Stäuber 2006, Table 6.6). Thus the upper limit for TMC1 is more than 10³¹ erg s⁻¹ and does not constrain the X-ray luminosity further.

6. Origin of ionized hydrides

The first group of molecules, CH⁺, OH⁺, H₂O⁺, and C⁺, is observed preferentially in blue-shifted absorption. 1D slab

modeling indicates that the excitation temperature of the ions is low (≤ 40 K, Sect. 4), below the radiation temperature of the background. However, a gas temperature of several hundred K would be necessary for efficient formation of CH⁺ through C⁺ + H₂. Thus the lines must be subthermally excited and the molecules are mostly in the ground state. Since the ions are destroyed by collisions with molecular hydrogen, a low density and high irradiation are required for enhanced abundances. This is consistent with the abundance ratios reported in Sect. 5. The collisional destruction may also explain why the ion hydride lines are rarely in emission and seem to originate from further out, where they absorb the continuum.

Several line characteristics indicate that the observed molecules are located not in diffuse clouds in the foreground but are related to star-forming regions: (i) the column densities correlate with source luminosity and envelope mass (Figs. C.4–C.9). (ii) The line velocities correlate with the source velocity, yielding consistently small line shifts (Figs. C.4–C.9). (iii) All lines (except H₂O⁺) are occasionally detected in emission, which requires high density in cases like CH⁺ and SH⁺.

Morales Ortiz et al. (2014) reported blue-shifted components of several HCO⁺, CO and N₂H⁺ emission lines toward NGC 6334 I. They interpret them by a shell of the envelope irradiated by external FUV, having a density of 10⁵ cm⁻³, and expanding at a velocity of -1.5 km s⁻¹. We consider such an interpretation for the first group of molecules unlikely, which have line shifts in the range of -10 to 10 km s⁻¹, exceeding the values expected for the outer edge of the envelope. Such a scenario may apply to CH, but not to the molecular ions which are clearly different in line shape, width and velocity from CH and to the other molecules in the second group.

Blue-shifted emission and absorption of H₂O has been discussed by Kristensen et al. (2013) as connected with the outflow directed toward Earth, where the continuum emitted by a disk or the dense inner envelope is absorbed. In the low-mass objects studied, this offset component is shifted by -12.7 to 0.9 km s⁻¹ relative to the YSO velocity and has a line width between 4 – 40 km s⁻¹. Several of the ionized molecules have similar broad and shifted profiles as those of H₂O.

The observed abundance ratios suggest either an H₂ density lower than 10⁴ cm⁻³ or an enhanced FUV flux by an internal source. Such low H₂ densities were proposed for diffuse clouds (Sect. 5) but not for star-forming regions (see Fig. D.1). For the well-studied high-mass object AFGL 2591 a detailed physical-chemical model has been developed including non-LTE line radiative transfer by Bruderer et al. (2010a), which indicates that the enhanced FUV from the central B star is key in explaining the abundances of species like CO⁺ and CH⁺. As a result of the high critical densities of diatomic hydrides, they found CH⁺ to be subthermally excited using densities of the order of 10⁶ cm⁻³ in the molecular region. Depending on the continuum radiation field, the lines can thus be in absorption even though they form in dense regions. The low density option cannot be excluded but the line profiles favor the enhanced FUV flux interpretation. This FUV radiation may be emitted either from the surface of the protostar or from fast shocks in the jets. In the following we discuss three origins for these ions: (A) the irradiated cavity walls; (B) the disk wind; or (C) the slow shock of the wind impacting the cavity wall. Cartoons are presented in Fig. 10 for illustration.

6.1. Scenario A: irradiated cavity walls

The walls of the outflow cavities may be illuminated by freely propagating or only partially absorbed FUV radiation. In

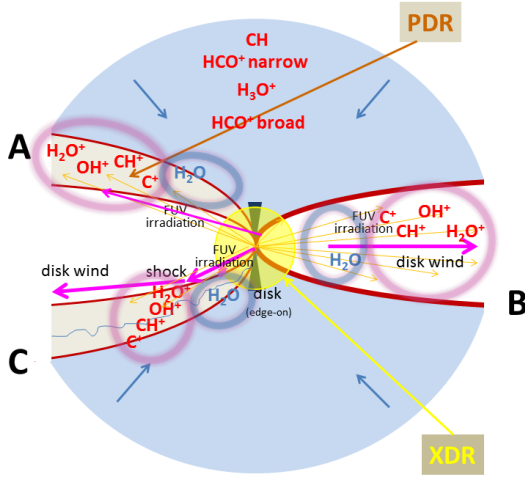


Fig. 10. Cartoons of three scenarios described in the text for the origin of the observed CH^+ , OH^+ , H_2O^+ , and C^+ absorptions. A: irradiated outflow walls with slow shocks entraining the outer layers of the walls; B: disk wind irradiated by protostellar FUV; C: fast dissociative shocks irradiated by protostellar FUV.

concave cavities, a protostellar FUV flux irradiates the walls, heats and ionizes the gas at the large surface to the envelope (Spaans et al. 1995; Stauber et al. 2007; Bruderer et al. 2009). Detailed modeling yields good agreement with observed column densities in two high-mass objects (Bruderer et al. 2010a; Benz et al. 2013). The scenario is possible for lines that are broadened, but not shifted. The observed blue-shift is however not compatible with stationary outflow walls. Another element is needed: the ionized molecules must be coupled to the outflow and be entrained.

6.2. Scenario B: disk wind

Another possible location of the CH^+ , OH^+ , H_2O^+ , and C^+ ions is protostellar wind. Panoglou et al. (2012) have studied the survival of molecules in disk winds of low-mass objects. In MHD driven winds irradiated by FUV from accretion shocks, the wind density at 100 AU in Class 0 objects is 10^6 cm^{-3} , about one order of magnitude below the envelope density (Kristensen et al. 2012). The temperature at this distance is around 1000 K, and the velocity reaches 40 km s^{-1} . None of our observed lines show such high velocities. According to the Panoglou et al. (2012) models, the wind densities are high enough so that dust absorption shields the molecules sufficiently from being photo-dissociated. H_2O forms via the endothermic neutral-neutral reactions. At slightly larger distances (10–1000 AU) ionized molecules form. Figure 8 in Panoglou et al. (2012) suggests a column density of about $5 \times 10^{14} \text{ cm}^{-2}$ for CH^+ in Class I objects, which exceeds the observed upper limit for L 1489 by more than an order of magnitude (Table B.1). A more serious discrepancy is the copious amount of SH^+ predicted by the wind model. A column density of $2 \times 10^{12} \text{ cm}^{-2}$ was predicted for Class 0 and 10^{14} cm^{-2} for Class I, exceeding some of the observed upper limits by more than two orders of magnitude (Table B.1). Panoglou et al. (2012) do not make predictions for the other species observed here and not for high-mass objects.

6.3. Scenario C: shocked cavity wall

The disk wind interacts with the cavity wall; such interaction is most likely a shock. Having a velocity component perpendicular

to the wall of about 10 km s^{-1} , the shock produces gas temperatures of a few thousand K, which is not high enough for FUV emission. Kristensen et al. (2013) and Mottram et al. (2014) considered this scenario as the origin of the blue-shifted component of H_2O toward low-mass YSOs. The shock front and internal layers are uneven, turbulent, and driven by the outward motion of the wind. Thus emission and absorption lines are medium-broad and blue shifted, the closer they originate from the cavity wall, the broader and more shifted the lines.

Kristensen et al. (2013) note that the chemical abundances predicted by the fast shock model of Neufeld & Dalgarno (1989) for CO, H_2O , and OH agree with observed values within an order of magnitude. However, the abundances of CH^+ , OH^+ , and HCO^+ are under-predicted by more than an order of magnitude. The low velocities of the blue-shifted components ($\ll 100 \text{ km s}^{-1}$) also suggest that the UV irradiation is not created within the shock itself. Molecular ions like CH^+ and OH^+ thus are proposed to form already in the pre-shock material by FUV irradiation from some source external to the shock.

The FUV radiation with luminosity L^{FUV} may originate from the accretion shock onto the protostar covering a fraction of its surface or (for high-mass objects) from the hot surface of the protostar. At a distance r and without absorption, the FUV flux G_0 is given by

$$G_0 = \frac{L^{\text{FUV}} L_{\odot}}{4\pi r^2 G_0^{\text{ISRF}}} = 850 \frac{L^{\text{FUV}}}{r_{1000}^2} [\text{ISRF}], \quad (7)$$

where L^{FUV} is the FUV luminosity in units of $L_{\odot}$, r_{1000} is the distance of the radiation source in units of 1000 AU, and $G_0^{\text{ISRF}} = 1.6 \times 10^{-3} \text{ erg cm}^{-2} \text{ s}^{-1}$. If the source of this radiation is located at the NGC 1333 I4A protostar for example, the luminosity required by the observed CH^+/OH^+ ratio (given in Sect. 6.2) would be $L_{\text{FUV}} = 1.5 L_{\odot}$. This is compatible with the reported bolometric luminosity of $L_{\text{bol}} = 9.1 L_{\odot}$. A hot spot of $3 \times 10^4 \text{ K}$ would have to have a diameter of $0.13 R_{\odot}$ to emit this luminosity. Similarly, one derives $L_{\text{FUV}} = 0.023 L_{\odot}$ for Ser SMM1. Visser et al. (2012) independently report $L_{\text{FUV}} < 0.1 L_{\odot}$ for their three low-mass sources based on highly excited CO and H_2O lines measured with *Herschel*/PACS. Such a source of FUV originating from accretion at the star-disk interface is not implausible, and thus we favor Scenario C.

7. Conclusions

This paper presents an exploratory high-resolution survey of hydrides in star-forming regions in far-infrared and submillimeter wavelengths. Objects range from low mass to high mass. The observed lines reported here include CH^+ , OH^+ , H_2O^+ , H_3O^+ , SH^+ , $\text{HCO}^+(6-5)$, C^+ , and CH. The selected lines bring the effects of ionization by internal sources into focus. The observed line properties suggest molecules in protostellar envelopes, entrainments of outflows, and diffuse interstellar foreground clouds. Only the components likely to be associated with the YSOs are studied here.

1. The detected lines can be grouped into two sets (see summary in Fig. 1): the first group includes CH^+ , OH^+ , and possibly H_2O^+ and C^+ . These ion lines are predominantly in absorption, have line widths 5–15 km s^{-1} , and are blue-shifted relative to the systemic velocity. All these species (except H_2O^+) also have an emission component in one or more sources.

2. Our preferred scenario for the first group of molecules is a slow shock heating and entraining envelope material combined with protostellar FUV irradiation (Scenario C) predicted for high-mass stars. It is compatible with our observations and previous modeling of cavity walls. An alternative interpretation where the ions exist in hypothetical low H_2 density regions ($<10^4 \text{ cm}^{-3}$) cannot be excluded, but is less likely based on the line profiles.
3. A second group including CH and $HCO^+(6-5)$ is observed predominantly in emission. The line widths are $\leq 5 \text{ km s}^{-1}$, and the line shifts with respect to the systemic velocities are small. H_3O^+ and SH^+ may also be part of this group, but have larger average line widths (Table 4). This group of lines is thought to originate in the bulk of the envelope.
4. The correlations of line characteristics confirm the grouping. CH^+ and OH^+ (and to a lesser extent C^+) correlate in their velocity shifts, and tentatively in line widths and column densities (Fig. 3). The relationships are further illustrated in the superposition of spectral profiles, showing similar emission and absorption features (Fig. 2). H_3O^+ and CH correlate with HCO^+ in column density and scatter around zero shift in velocity relative to the systemic velocity (Fig. 4).
5. The beam-averaged column density of all molecules correlates with bolometric luminosity (Figs. C.4–C.9) and thus increases from low-mass to high-mass objects. The best correlations are found for CH, CH^+ , and HCO^+ . As the envelope mass correlates with luminosity (Bontemps et al. 1996), it is not surprising that the column density of all molecules also correlates with envelope mass (except H_3O^+).
6. The correlation between the distance-corrected line intensity and bolometric luminosity reaches a correlation coefficient of 0.95 for $HCO^+(6-5)$ (Fig. 6). Appendix D offers an interpretation based on optically thick emission and the self-similarity of the dust radiative transfer.
7. Comparing observational and modeled abundance ratios provides a rough indication of FUV and X-ray irradiation. For absorption lines, the observed CH^+/OH^+ ratios can be reproduced in simple chemical models for reasonable FUV fluxes. For the emission lines of W3 IRS5, the required FUV flux is $G_0 = 300\text{--}600 \text{ ISRF}$ at a density of $1.1 \times 10^5 \text{ cm}^{-3}$. This value is far below that expected from unabsorbed FUV emission by an unbloated central high-mass object.
8. Our *Herschel* data yield no evidence for X-ray irradiation from any of the studied line ratios, even for sources where X-rays have been observed. Also in low-mass objects, the spatial resolution at scales of a few 1000 AU is not sufficient to detect molecular traces of X-rays. The effect of X-rays (if any) is limited to the innermost part of the envelope and disk, requiring higher spatial resolution. Upper limits of the X-ray luminosity can be derived from H_3O^+ observations for some objects.

Herschel/HIFI observations enable a big step forward in our knowledge on hydrides. Some of hydrides suggest strong irradiation of low molecular density regions, thus regions where H_2O is destroyed by photodissociation (see Introduction). It is consistent with low H_2O abundances in outflows as inferred by Visser et al. (2012), Kristensen et al. (2013), Mottram et al. (2014), and Karska et al. (2014). Surprisingly, the first group of ion molecules shows similarity with the offset component of H_2O , indicating proximity of origin. Inhomogeneity of the inner region of star-forming regions may explain the contradiction. The next important step can be expected from imaging observations of CH^+ and OH^+ in lines that are observable from the

ground. Such observations will soon be possible with ALMA and may confirm the suggested scenario. High spatial resolution HCO^+ observations at various J transitions will help to find evidence for position dependent ionization rates in the innermost region including the disk where X-rays and other ionization sources (e.g., Ceccarelli et al. 2014) may be important.

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Appendix A: Analysis of individual observations

The observed line spectra are individually shown in Figs. A.1–A.8. The velocity scale refers to the line frequency in the LSR. If several line components exist, the scale is relative to the most intense fine or hyperfine structure line indicated by an asterisk in Table 2. The systemic velocity of the YSO as given in Table 1 is marked with a vertical dashed red line. For lines with several fine or hyperfine structure components, the line thickness and dash length indicate the theoretical intensities in decreasing order (arbitrary scale). The line shapes are modeled with Gaussian fits. If more than one component exists, several Gaussians are fitted to estimate the line parameters, which are given in Table B.1.

A.1. CH^+

CH^+ ($J = 1-0$) is detected in absorption toward the low-mass objects of Class 0 (Fig. A.1). The detection is only tentative toward NGC 1333 I4B, and there is no hint of the line toward L 1489 (Class I), where the continuum is weak and the upper limit is higher than for the absorptions detected in the Class 0 objects (Table B.1). Toward the intermediate-mass object NGC 7129 FIRS2, the absorbed line width is relatively large and more similar to some high-mass sources. Contrary to the low-mass objects, where the line is shifted to the blue of the systemic velocity, the line toward NGC 7129 FIRS2 is shifted to the red.

CH^+ is predominantly observed in absorption, but toward high-mass some objects also in emission (Fig. A.1). AFGL 2591 and W3 IRS5 show pronounced P-Cygni profiles, with absorption to the blue of an emission peak. In S 140 the continuum is removed by frequency switching. The peaks between 20 and 30 km s^{-1} are the negative ghosts of the lines observed near the systemic velocity. The spectrum can be interpreted by an emission and an absorption on each side or as an emission in the middle of a broad (about 9 km s^{-1}) and probably saturated absorption. We assume the first option to derive lower limits for the line intensity and absorption, and the second option for upper limits. The column densities in Table B.1 refer to these limits. NGC 7538 IRS1, on the other hand, shows an inverse P-Cygni profile. Emission and absorption are listed separately, including the column depths of each transition. NGC 6334 I and I(N) show a double absorption dip, separated by about 10 km s^{-1} . The deeper one is wider, the other one is more red-shifted and narrower. The similarity of the two dips toward the two adjacent objects suggests absorption by diffuse clouds in the foreground (Emprechtinger et al. 2010). However, the spectra of NGC 6334 I were fitted by a 1D slab model (Bruderer et al. 2010a, Appendix B) including the $\text{CH}^+(2-1)$ transition (see below), which resolved the deeper dip into a blue-shifted and a red-shifted component. The blue-shifted component of the deeper dip is assumed to originate from the YSO, but the red-shifted component is questionable. We interpret the other dip as due to diffuse clouds in the foreground.

The CH^+ lines presented in Fig. A.1 and attributed to the YSO consist of one or two Gaussian components. A significant deviation from symmetry, however, is noted toward AFGL 2591, which has extended absorption between -25 and -35 km s^{-1} , thus from -19 to -29 km s^{-1} relative to the systemic velocity. This tail has been noted before by Bruderer et al. (2010b), and as well in ^{12}CO and ^{13}CO ($v = 1-0$) infrared absorption by Mitchell et al. (1990) and van der Tak et al. (1999).

Methanol emission overlaps in the presented frequency range toward the massive objects NGC 6334 I and AFGL 2591

at 36.1 and 47.5 km s^{-1} relative to the systemic velocity. The respective transitions are at 824.7197 GHz ($20_{-1,0}-19_{0,0}$) in the lower sideband, and at 835.0039 GHz ($4_{5,5}-5_{4,0}$) in the upper sideband. The line at 835.1851 GHz ($17_{-3,0}-17_{2,0}$) is the only methanol line that is directly in the range of CH^+ emission. It is prominent toward NGC 6334 I at -24.4 km s^{-1} and minuscule toward AFGL 2591 at -22.5 km s^{-1} . CH^+ absorption by foreground clouds is noticeable in all high-mass sources. It lines up with absorptions of the ground-state H_2^{18}O line in the second dip of W3 IRS5, AFGL 2591, and NGC 6334 I(N) (van der Tak et al. 2013).

CH^+ ($J = 2-1$) was observed in some of the sources (Fig. A.2). None of the low-mass (Class 0) observations detected the line. The high-mass mid-IR quiet object NGC 6334 I(N) was also not detected, but AFGL 2591, W3 IRS5, and NGC 7538 IRS1 show emission. The spectra of the first two objects also contain a weak blue-shifted absorption, indicating a P-Cygni profile (as noted already in Bruderer et al. 2010a; Benz et al. 2011). The non-detections of the low-mass objects in $\text{CH}^+(2-1)$ are consistent with the assumed excitation temperature (9 K) and total derived CH^+ column densities given in Table B.1.

A.2. OH^+

OH^+ ($N_J = 1_1-0_1$) absorption is clearly detected in the low-mass object Ser SMM1 (Fig. A.3, second row, left). The two lines (each a doublet, see Table 2) have similar shape and the flux ratio is consistent with optically thin. They are possibly detected toward NGC 1333 I4A in absorption, but only at a signal-to-noise of 4σ (sigma). The detection is doubtful since the separation between the hyperfine components is 2 km s^{-1} smaller than expected. We use the fitted line intensity as an upper limit in Table B.1. Even weaker are the lines in NGC 1333 I4B, but the similarity in blue shift with the CH^+ absorption lines (Fig. A.1, top right) corroborates the detection. The line widths toward the NGC 1333 I4A and I4B (if real) are extremely narrow with a FWHM of 1.4 and 1.7 km s^{-1} . The fitted lines in NGC 7129 FIRS2 have a width of >7.4 and 10 km s^{-1} (Fig. A.3, second row, right). OH^+ is not detected toward NGC 1333 I2A and L 1489. The low continuum of L 1489 makes a detection difficult and yields a high upper limit on the column density (Table B.1).

Toward massive objects, OH^+ is mostly in absorption. W3 IRS5 (Fig. A.3, bottom left) has an emission peak at a 12σ level (Benz et al. 2010). It confirms the protostellar origin of OH^+ in this source. The emission is slightly red-shifted but close to a blue-shifted absorption, thus suggesting a P-Cygni profile similar to but less pronounced than that in CH^+ . We note also a tail in absorption blue-shifted by 10–17 km s^{-1} relative to W3 IRS5, similar to CH^+ toward AFGL 2591. As the two main OH^+ fine structure lines each have substructures, only the strongest feature is fitted with a Gaussian. The absorption integrated over all fine structure lines and the total column density integrated over all levels are given in Table B.1. NGC 6334 I and AFGL 2591 show also an absorption component that is blue-shifted by 4–10 km s^{-1} relative to the systemic velocity and two components red-shifted by typically 4–15 km s^{-1} . The blue-shifted component is missing in S 140, NGC 6334 I(N), and NGC 7538 IRS1. W3 IRS5 and NGC 7538 IRS1 have a second, deeper pair of absorption lines shifted to the red by 27.5 and 55 km s^{-1} , respectively. They partially coincide with absorptions in $\text{CH}^+(1-0)$, suggesting diffuse interstellar foreground (Indriolo et al. 2015).

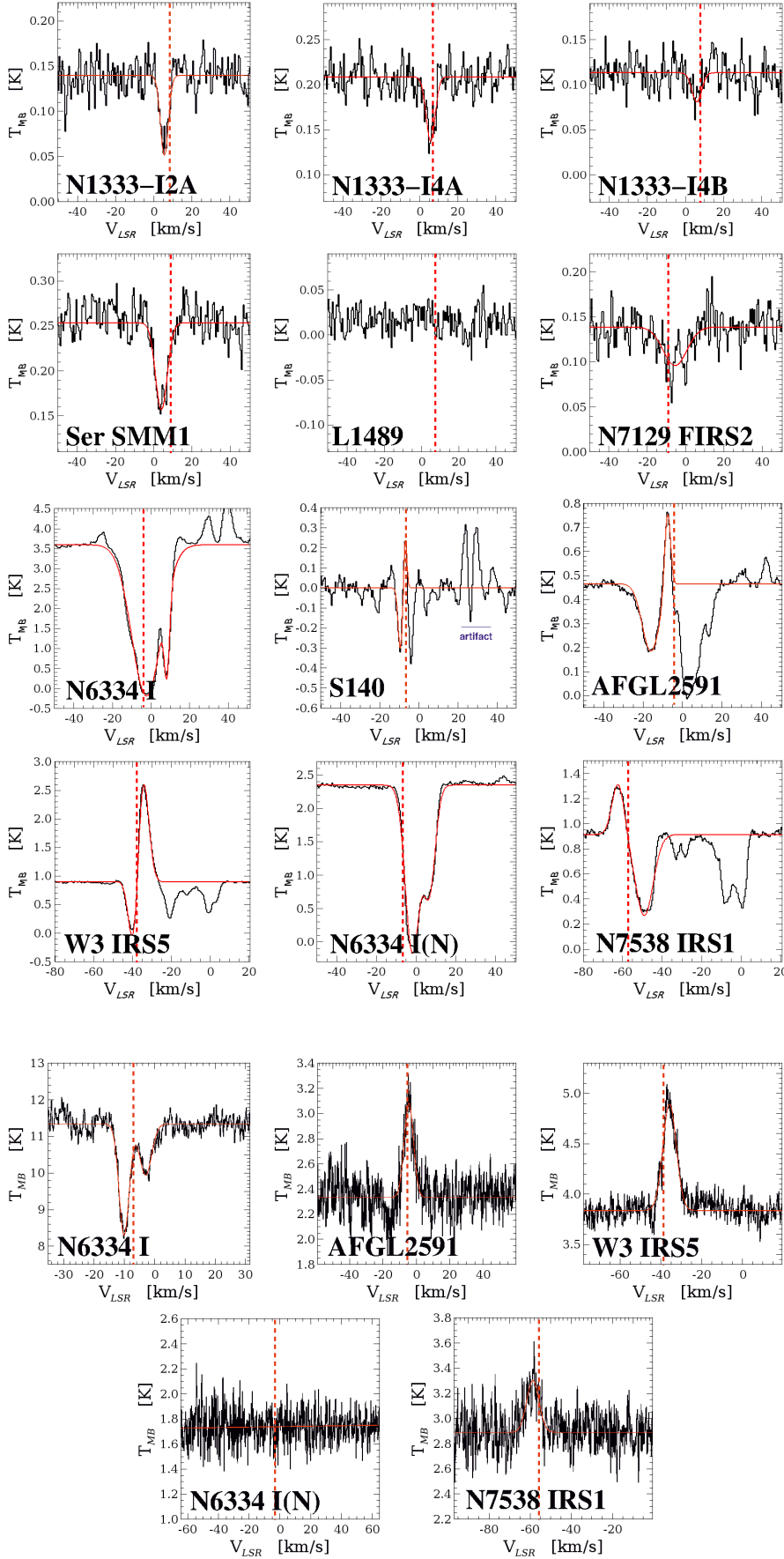


Fig. A.1. $\text{CH}^+(1-0)$ line at 835 GHz. The position of the line shifted by the systemic velocity of the YSO is indicated with a vertical red dashed line. Where the line is detected, a Gaussian in red is fitted and its parameters in width and shift are given in Table B.1. The feature at 25 km s^{-1} toward S 140 is an artifact of the frequency switching mode. For the same reason the background continuum is not available for this object.

Fig. A.2. $\text{CH}^+(2-1)$ line at 1669 GHz observed toward the high-mass objects. Where detected, a Gaussian fit is shown in red and the parameters are given in Table B.1.

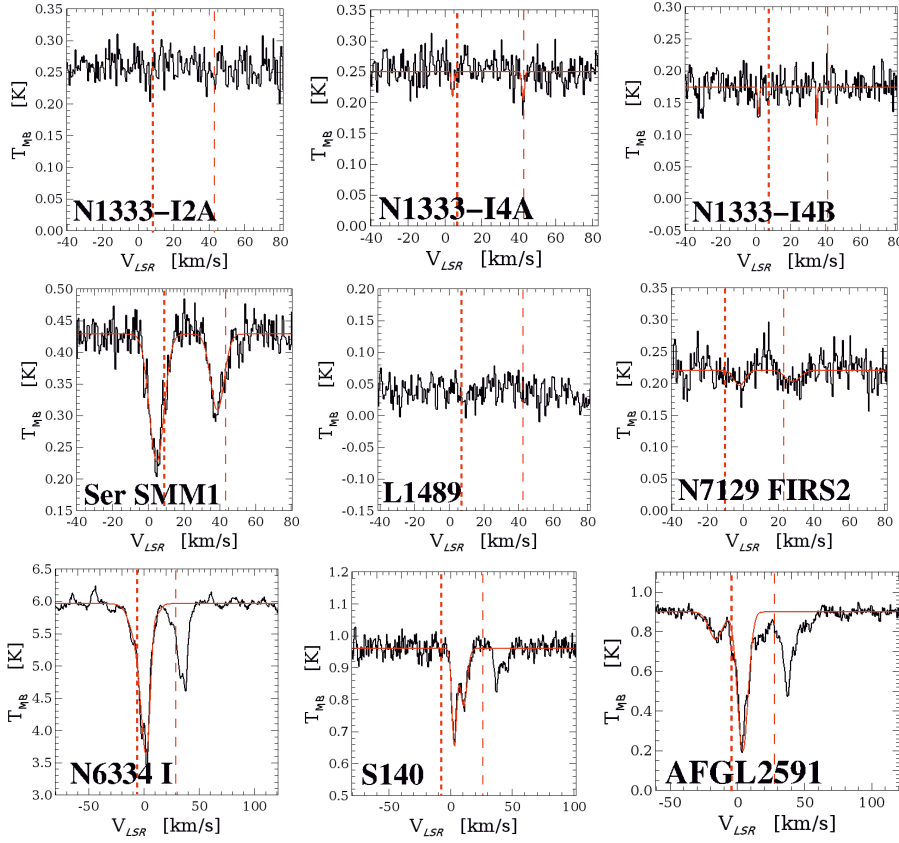


Fig. A.3. $\text{OH}^+(N_J = 1_1-0_1)$ lines at 1033 GHz. The positions of the two strongest fine structure lines, ($N_{JF} = 1_{1\frac{1}{2}}-0_{1\frac{1}{2}}$) and ($1_{1\frac{1}{2}}-0_{1\frac{3}{2}}$), are indicated, shifted by the systemic velocity of the YSOs. The thickness of the two lines indicates the relative theoretical intensities. Where the lines are detected, two Gaussians in red are fitted.

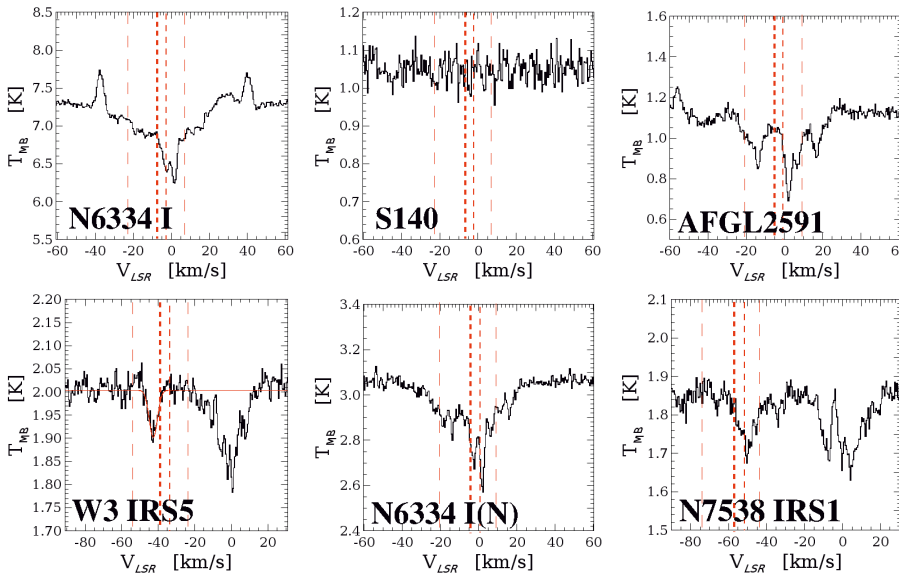


Fig. A.4. Ortho- H_2O^+ ($N_{KaKaJ} = 1_{11\frac{3}{2}} - 0_{00\frac{1}{2}}$) lines at 1115 GHz observed toward the high-mass objects. The position of the strongest lines shifted by the systemic velocity of the YSO is indicated with vertical red dashed lines. Their thickness indicates the theoretical intensities. Only the blue-shifted line of W3 IRS5 is fitted by a Gaussian (red, see text). Its parameters are given in Table B.1.

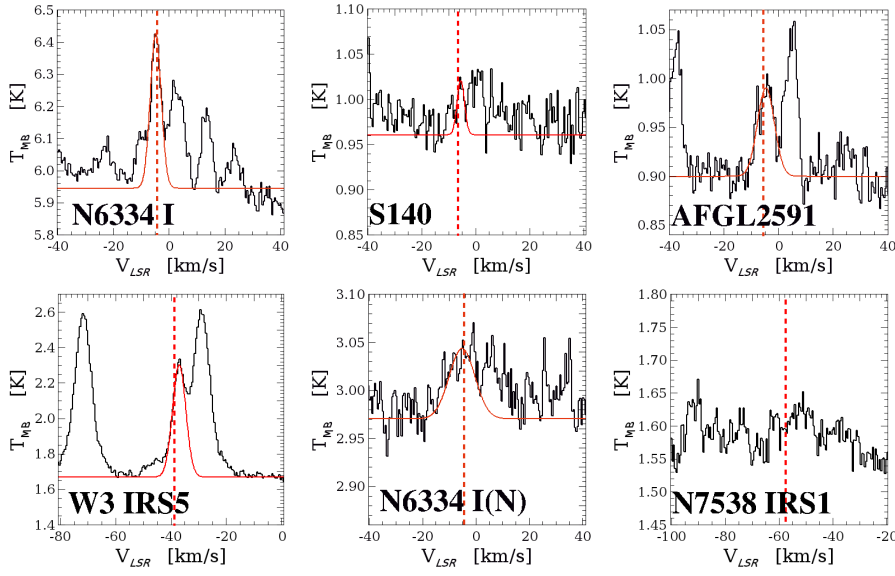


Fig. A.5. Ortho- $\text{H}_3\text{O}^+(4_3^+-3_3^-)$ line at 1031 GHz observed toward the high-mass objects. The observed line is fitted by a Gaussian (red) and its parameters are given in Table B.1. An SO line at $+10.1 \text{ km s}^{-1}$ relative to the systemic velocity and lines from the other sideband appearing at 6 and 8 km s^{-1} are blended (see text).

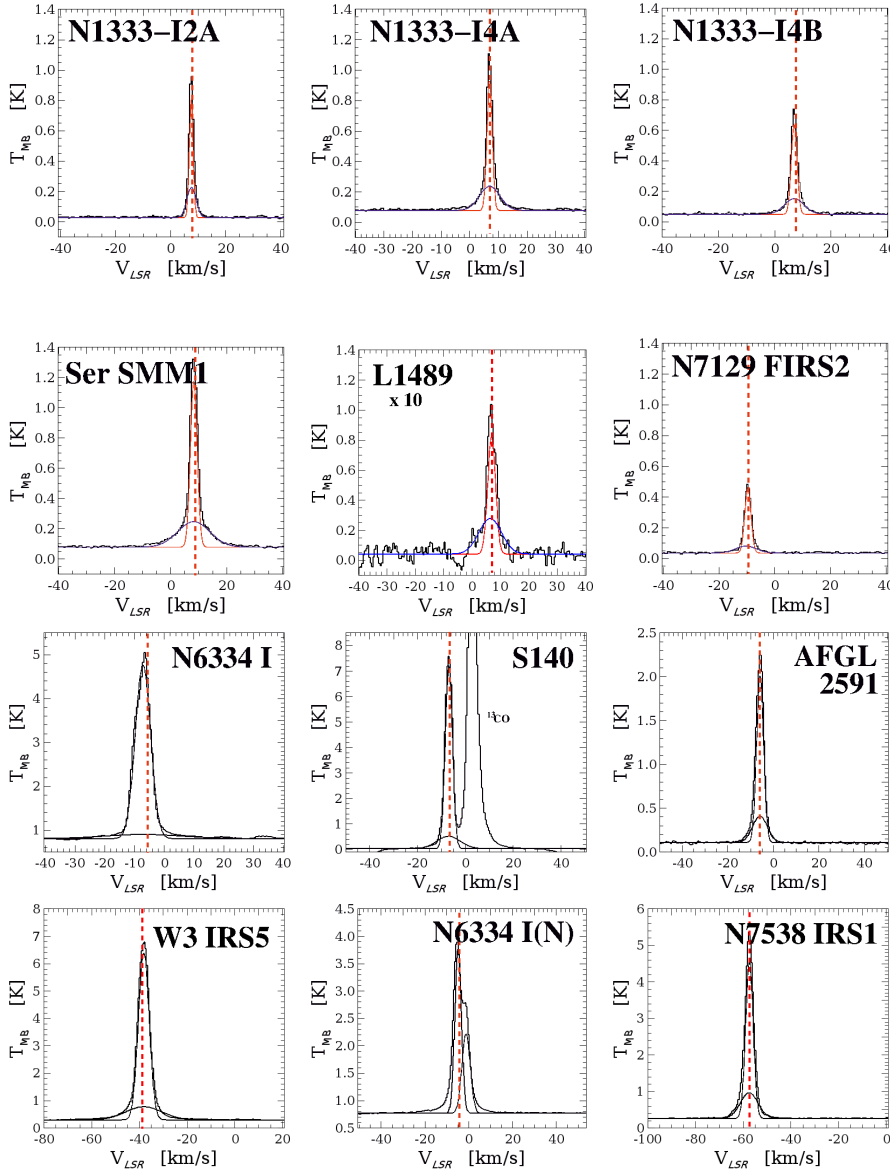


Fig. A.6. $\text{HCO}^+(6-5)$ line at 535 GHz. A two-Gaussian fit is shown, emphasizing the center and the wings of the line. Both sets of parameters are given in Table B.1. The strong line at 3 km s^{-1} in S140 is ^{13}CO ($J = 5-4$) from the other sideband.

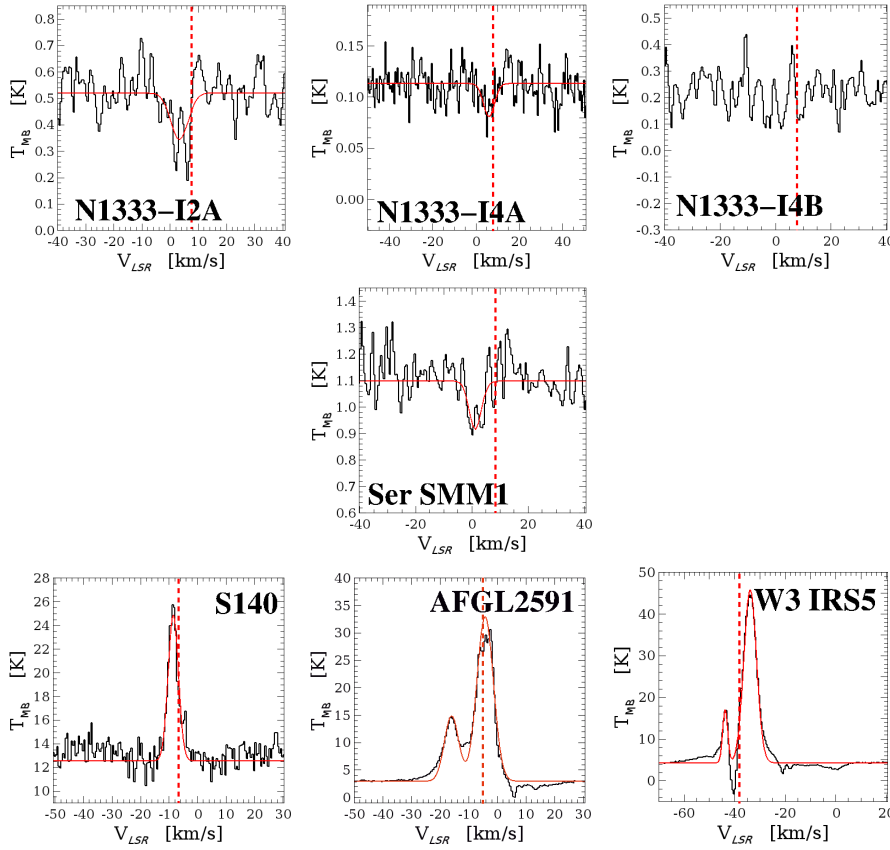


Fig. A.7. C⁺ fine structure line at 1901 GHz. Where detected, a Gaussian fit is shown in red and the parameters are given in Table B.1.

A.3. H₂O⁺

The ortho-H₂O⁺ ($N_{K_a K_b} = 1_{11} - 0_{00}$, $J = \frac{3}{2} - \frac{1}{2}$) hyperfine transitions were not detected toward the low- and intermediate-mass objects. The rms noise is between 20 and 24 mK, yielding upper limit column densities around $5 \times 10^{12} \text{ cm}^{-2}$ for Class 0 objects (Table B.1). The only notable exception is Ser SMM1, for which there is a tentative absorption at the 5σ level, blue-shifted by -3.5 km s^{-1} (see Fig. 2, bottom). We use it as an upper limit in Table B.1.

Observations of the high-mass sources are presented in Fig. A.4. Where detected, H₂O⁺ is in absorption. Deep absorptions are found near zero LSR velocity; they are probably caused by diffuse interstellar foreground clouds. The component intrinsic to the object is not always clearly detected. Exceptions are blue-shifted absorptions in AFGL 2591 and W3 IRS5 that have been attributed to the YSO by Bruderer et al. (2010b) and Benz et al. (2010), respectively. Absorptions at -54 , -65 , and around -81 km s^{-1} toward NGC 7538 IRS1 may be associated with the YSO, but blue-shifted by -9.9 km s^{-1} . We use this tentative detection as an upper limit of the intensity. H₂O⁺ toward NGC 7538 IRS1 shows a second complex set of absorption lines red-shifted from the systemic velocity. It is attributed to diffuse clouds in the foreground (Indriolo et al. 2015). Relatively broad and blue-shifted absorption lines of H₂O⁺ have been reported in other sources by Wyrowski et al. (2010) and attributed to the outflows. Consistent with this suggestion, we have not detected any narrow absorptions of H₂O⁺, excluding the envelope as the source. A tentative emission at $0-6 \text{ km s}^{-1}$ (Benz et al. 2010) is not confirmed by the new analysis. For NGC 6334 I and I(N) the absorption profiles are nearly identical in V_{LSR} , strongly suggesting that the absorption is not intrinsic to the source but caused by foreground diffuse interstellar clouds.

There are nearby methanol lines at -37.2 and $+40.1 \text{ km s}^{-1}$ toward NGC 6334 I from the lower sideband (1100.469236 GHz, $(13_{8,0} \rightarrow 14_{7,0})$ and 1100.757207 GHz ($13_{5,1} \rightarrow 13_{6,1}$), but no strong methanol line interferes with H₂O⁺.

The column densities listed in Table B.1 were multiplied by 1.33 to account for the unobserved para-H₂O⁺ lines, assuming an ortho-to-para ratio of 3 (Indriolo et al. 2015).

A.4. H₃O⁺

Para-H₃O⁺ ($J_K^p = 3_2^+ - 2_2^-$) emission has been previously detected in high-mass YSOs from the ground by Wootten et al. (1991) and Phillips et al. (1992). Recently Lis et al. (2014) observed H₃O⁺ toward W31C in absorption in the inversion transitions and derived $T_{\text{rot}} \approx 380 \text{ K}$.

There are no detections of ortho-H₃O⁺ ($4_3^+ - 3_3^-$) in low- and intermediate-mass objects. The rms noise is between 17 and 20 mK, yielding upper limit column densities $< 2.0 \times 10^{12} \text{ cm}^{-2}$ for an assumed excitation temperature of 225 K (Table B.1). The line is detected in massive objects (Fig. A.5), but blended with the SO ($N_J = 24_{24} - 23_{23}$) line at 10.1 km s^{-1} and by lines from the lower sideband. All lines are fitted, and the fit of the H₃O⁺ line is reported in Table B.1. The identifications of H₃O⁺ in S 140 and NGC 6334 I(N) are tentative because of limited sensitivity. The fitted values are considered to be upper limits. The line was not detected in NGC 7538 IRS1.

A.5. SH⁺

The detection of SH⁺ ($N_{\text{JF}} = 1_{2\frac{5}{2}} - 0_{1\frac{3}{2}}$) and ($1_{2\frac{5}{2}} - 0_{1\frac{3}{2}}$) in emission toward W3 IRS5 was previously reported (Benz et al. 2010). We confirm here the detection, but cannot find it either in

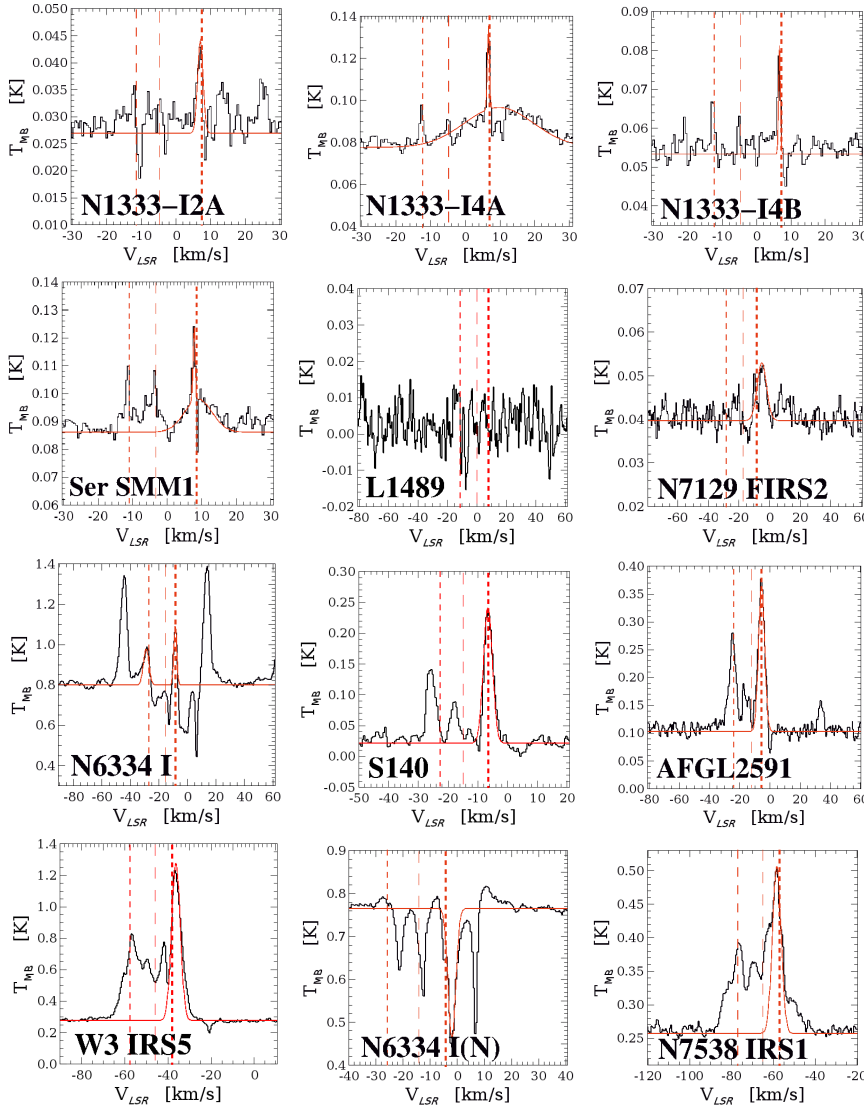


Fig. A.8. CH lines at 537 GHz. The positions of the fine structure lines are shown shifted by the systemic velocity of the YSOs. The thickness of the three lines indicates the relative theoretical intensities. Where the lines are detected, a Gaussian curve in red is fitted to the strongest transition and its parameters are given in Table B.1. The broad feature in N1333 I4A is an interfering H_2O line from the other sideband.

emission or absorption toward the other objects of low, intermediate and high mass. The upper limit on the SH^+ column density toward AFGL 2591 is $<1.5 \times 10^{11} \text{ cm}^{-2}$, a factor of 30 lower than the upper limit derived by Stäuber et al. (2007) from the transition $N_{\text{JF}} = 1_{0\frac{1}{2}} - 0_{1\frac{3}{2}}$ at 345.944 GHz, but six times smaller than detected toward W3 IRS5. The reason for the difference between the two YSOs may be the high gas-phase sulphur abundance in W3 IRS5, noted before, e.g., by Helmich & van Dishoeck (1997) and van der Tak et al. (2003). Stäuber et al. (2007) report a nine times stronger SO^+ line intensity toward W3 IRS5 than for AFGL 2591 and attribute it to different sulphur abundances in the gas. SH^+ is also not detected toward the similar object NGC 6334 I, where the background is high and a line, probably methanol ($14_{2,13} - 14_{1,14}$) at 526.02589 GHz, overlaps.

We have not seen, nor especially searched for, SH^+ absorption lines that are strongly shifted from the systemic velocity suggesting absorption by diffuse interstellar clouds.

A.6. HCO^+

HCO^+ ($J = 6-5$, $v = 0$) is clearly detected in emission toward all objects. It is fitted here with two Gaussians, one for the

line peak and one for the wings (Figs. A.6). The properties of the two components are discussed in Sect. 5.2. Table B.1 gives the values of the fits in peak, width, and shift; the line intensity and column density are integrated over both components. A red-shifted shoulder toward L 1489 is noticeable in Fig. A.6, second row, middle; and a double peak is clearly visible in HRS resolution. A similar feature was reported for this object in HCO^+ (3–2) and (4–3) by Brinch et al. (2007) and interpreted as a disk contribution.

A.7. C^+

If C^+ ($^2\text{P } J = \frac{3}{2} - \frac{1}{2}$) is detected toward low-mass objects, it is in absorption (Fig. A.7). The detection level is 5σ toward Ser SMM1. The red-shifted emission peak is statistically not significant. We note, however, that PACS observations of this source report C^+ in emission preferentially from the outflows (Goicoechea et al. 2012). The Gaussian curve fitted for NGC 1333 I2A indicates a statistical significance of 7σ for an absorption feature. The C^+ line is tentatively detected toward NGC 1333 I4A. A 4.1σ absorption is found at the expected

velocity and yields an upper limit for the column density. C^+ is not detected toward NGC 1333 I4B. Where detected in low-mass objects, the line is shifted on average by $-5.9 \pm 0.8 \text{ km s}^{-1}$ and has an average line width of $6.0 \pm 1.0 \text{ km s}^{-1}$. The differences between the two off-source reference positions for the low-mass objects are small and do not indicate significant variations in large-scale C^+ emission. Thus the absorption lines seem to be inherent to the source.

The line profiles of the three observed high-mass objects (Fig. A.7) can be interpreted by two emission peaks or by a broad peak, reduced by a narrow absorption or emission at the reference position. Toward W3 IRS5 the spectrum falls below the continuum level, suggesting that the line is self-absorbed. This interpretation is also assumed for the other two objects. An absorption feature is seen near the systemic velocity in all three objects. The integrated emission line intensities in Table B.1 thus yield lower limits in column density. For line width and line shift, we have fitted two Gaussian emission peaks. Both peaks are integrated to measure the column density.

A difference between the off-position emissions was detected for AFGL 2591 at -11.1 , -5.2 , 4.7 , and 5.7 km s^{-1} in V_{LSR} . The latter is most significant and has an integrated intensity of 8.6 K km s^{-1} , thus about 3% of the total emission. These differences are interpreted as slightly different large-scale emissions, which cause spurious dips in the spectrum when subtracted. In addition, AFGL 2591 seems to have several intrinsic red-shifted absorption features. In particular, the feature at 13 km s^{-1} is not detectable in the difference of the off-positions. It is also visible in the CH^+ ($1-0$) line (Fig. A.1, fourth row, right) and was reported by Bruderer et al. (2010b).

The C^+ spectrum of W3 IRS5 is similar and also has many spectral components. Most prominent are the peak at -43.9 and the main peak at -33.9 km s^{-1} interrupted by a minimum at -40.3 km s^{-1} amounting to $-3.14 \pm 0.06 \text{ K}$. The difference between the emissions of two reference positions amounts to 2.1 K km s^{-1} , but peaks at $-38.4 \pm 0.2 \text{ km s}^{-1}$, the systemic velocity. Nevertheless, the minimum observed at -40.3 km s^{-1} seems to be caused mostly by off-source emission. For S 140, observed in OTF mode, the reference position does not emit C^+ emission above 1.2 K km s^{-1} (Emery et al. 1996); thus the off-beam contamination is small. We conclude that the integrated line emission of the C^+ line in the observed high-mass objects is not severely altered by emission at the reference position.

A.8. CH

The CH ($2\Pi_{3/2} J = \frac{3}{2}-\frac{1}{2}$) hyperfine transitions were detected in emission toward all the low-mass and intermediate-mass objects except toward the Class I object L 1489 (Fig. A.8, second row, middle). The line widths of the narrow component toward NGC 1333 I4A, NGC 1333 I4B and Ser SMM1 are remarkably small (average $0.63 \pm 0.06 \text{ km s}^{-1}$) and were analyzed using the High Resolution Spectrometer (HRS/HIFI) data. In these cases, the line width appears to be reduced by a narrow red-shifted absorption, forming an inverse P-Cygni profile. Toward NGC 1333 I2A the line is not absorbed and its width is 1.9 km s^{-1} . This value is comparable to the line widths found previously from the outer part of quiescent envelopes in $C^{17}O$ and $C^{18}O$ ($J = 2-1$) lines (e.g., Jørgensen et al. 2002, : $0.7-2.1 \text{ km s}^{-1}$). The same objects as in this study were observed in $C^{18}O$ ($J = 3-2$) by San José-García et al. (2013), who report line widths of $1.47 \pm 0.53 \text{ km s}^{-1}$. Values between $2-3 \text{ km s}^{-1}$ were reported by Kristensen et al. (2012) for the narrow component of the 557 GHz H_2O ($1_{10}-1_{01}$) line mostly seen in absorption. The similarities suggests that the narrow component of the CH lines originate in the same region of the outer envelope as the low- J CO lines.

In addition, Ser SMM1 (Fig. A.8, second row, left) has also a broad emission component (FWHM 9.4 km s^{-1}). Its column density is an order of magnitude larger than for the narrow component.

In massive objects (Fig. A.8), the CH lines at 537 GHz are observed in emission as well as in absorption. Emission and absorption are mixed toward NGC 6334 I, as previously reported by van der Wiel et al. (2010). CH absorption dominates in NGC 6334 I(N) having a more massive envelope. In both objects at least one other system of absorption lines at positive velocity ($\approx 7 \text{ km s}^{-1}$) is observed, originating probably in diffuse interstellar clouds in the foreground. For S 140, AFGL 2591, and NGC 7538 IRS 1 emission dominates. In W3 IRS5 emission also dominates, but combines with a blue-shifted absorption to an apparent P-Cygni profile. Methanol line emission in the lower sideband interferes toward NGC 6334 I. In the velocity range of Fig. A.8, bottom left, they appear at -40.0 and 18.4 km s^{-1} . There is no other obvious interfering line in-between. Thus we assume that all minima and maxima between -34 and 14 km s^{-1} are due to CH emission and absorption.

Appendix B: Observed line parameters vs. objects, quantitative results

The line profiles were fitted by one or two Gaussians and their parameters are given in Table B.1. Only the line components moving with the systemic velocity of the YSO within $\pm 12 \text{ km s}^{-1}$ are listed. Some components even within that range may originate from diffuse clouds in the foreground. Suspected cases are indicated by “DC” in the following tables. The YSO origin of the lines is discussed in Appendix A. The line peak, T_{max} , is given above (or below) the continuum background, T_b , in main beam temperature and refers to the strongest fine structure transition. For non-detections the upper limit is given by 3 times the measured rms noise. The line width, ΔV , is the full width at half maximum (FWHM) above (or below) background of the Gaussian fit for the strongest component. The line shift, δV , relative to the LSR also refers to the Gaussian fit of the strongest component. If the line fit was greatly improved using two Gaussians, both are given on separate lines in the tables. Errors are a few units of the last decimal. The accuracies of the line width and line shift are better than 1 km s^{-1} . Line peak intensities have uncertainties of 10–20%, which is mostly caused by calibration errors, but above 1 THz due to noise or baseline fitting errors.

Intensity, $\int T_{\text{MB}} dV$, refers to the integrated line profile in the observed main beam temperature above the background of lines in emission. Integration usually goes from -40 km s^{-1} to $+40 \text{ km s}^{-1}$ relative to the line peak. In cases of line blending, the interfering line is also characterized by a Gaussian; the

target line fitted parameters are used for line integration and indicated with an asterisk (*). In cases of several fine or hyperfine lines, they were all integrated. If not detected, the upper limit for lines expected in emission refers to $1.2 \sqrt{\delta v \Delta V} \times 3\sigma$, where δv is the spectral resolution (1.1 km s^{-1}), σ is the rms noise of the background, and ΔV is the expected line width (put to 5 km s^{-1}).

For lines in absorption, the integral in optical depth τ over velocity is given, where $\tau(V) = \ln[T_b/T_{\text{MB}}(V)]$. T_b is the background main beam temperature and $T_{\text{MB}}(V)$ the observed main beam temperature at velocity V . For $\tau \ll 1$, the upper limit of an undetected absorption line amounts to the integrated line intensity below background divided by the background. Thus the upper limit for an undetected absorption line is $\int \tau(V) dV \approx 1.2 \sqrt{\delta V \Delta v} \times 3\sigma/T_b$. It assumes 20% calibration uncertainty.

Level column densities are extracted by integrating the observed lines or absorption profiles, neglecting re-emission or re-absorption of the final state (thus optical depth $\tau \ll 1$) and applying either Eqs. (3) or (4). The column density of a particular level was extended to the total column density of a species i , N_i , summed over all levels using Eq. (6) and assuming an appropriate excitation temperature (given also in Table B.1). The reasons for the assumed value of T_{ex} are discussed in the text (beginning of Sect. 4). The errors introduced based on an expected range of T_{ex} , as well as by noise and background subtraction are given in Table 3 by factors that define the error range of column densities around the value given in Table B.1. The column densities are not corrected for beam filling or optical thickness.

Table B.1. Observed line parameters of objects.

	$T_{\max}$ [K]	rms [K]	T_b [K]	ΔV [km s ⁻¹]	V_{line} [km s ⁻¹]	δV [km s ⁻¹]	$\int T_{\text{MBdV}}$ @ = $\int \tau dV$	T_{ex} [K]	N_i [cm ⁻²]
CH⁺ (1–0) 835.1375 GHz									
NGC 1333 I2A	−0.088	0.015	0.14	4.9	5.6	−1.9	3.8@	9	1.1(13)
NGC 1333 I4A	−0.071	0.016	0.21	5.6	5.8	−1.1	2.7@	9	8.0(12)
NGC 1333 I4B	−0.032	0.014	0.11	6.0	6.0	−1.0	1.3@	9	2.9(12)
Ser SMM1	−0.096	0.013	0.25	7.3	4.1	−4.1	5.8@	9	1.7(13)
L 1489	>−0.030	0.010	0.014	—	—	—	<6.3@	9	<1.9(13)
NGC 7129 FIRS2	−0.043	0.017	0.14	14.5	−5.4	4.5	2.4@	9	7.0(12)
W3 IRS5	−1.3	0.009	0.89	7.1	−38.5	−0.1	10.0@	8 ^a	4.4(13) ^a
	2.1	0.009	0.89	3.0	−34.5	3.9	9.8	38 ^a	9.6(12) ^a
NGC 6334 I	−3.6	0.030	3.7	5.9	−2.6	5.1	>48@	7 ^a	2.6(14) ^a DC
	−2.2	0.030	3.7	4.5	−11	−3.3	1.6@	12 ^a	5.7(13) ^a
NGC 6334 I(N)	−2.5	0.014	2.3	3.5	−1.9	2.6	<34@	9	≤1.0(14)
	−1.5	0.014	2.3	7.1	6.5	11.0	4.9@	9	1.5(13) DC
AFGL 2591	−0.28	0.010	0.47	10.3	−16.0	−10.5	8.7@	3 ^a	1.8(14) ^a
	0.33	0.010	0.47	13.5	−7.5	−2.0	0.86	43 ^a	8.5(12) ^a
S 140	−0.30	0.030	—	2.7	−9.5	−2.4	2.1–20.1@	9	0.6–5.9(13)
	0.27	0.030	—	1.9	−7.0	0.1	<0.38–2.4	38	0.16–1.0(12)
NGC 7538 IRS1	0.63	0.014	0.91	13.5	−57.5	−0.1	9.3	44 ^a	4.1(12) ^a
	−0.90	0.014	0.91	8.8	−51.8	5.6	8.7@	3 ^a	1.1(14) ^a
CH⁺ (2–1) 1669.2813 GHz									
NGC 1333 I2A	<0.17	0.058	—	—	—	—	<0.48	—	—
NGC 1333 I4A	<0.17	0.058	—	—	—	—	<0.49	—	—
NGC 1333 I4B	<0.18	0.061	—	—	—	—	<0.51	—	—
Ser SMM1	<0.22	0.074	—	—	—	—	<0.63	—	—
W3 IRS5	1.1	0.045	4.1	7.7	−35.9	2.5	8.7	—	—
NGC 6334 I	−2.8	0.12	11.4	3.9	−10.3	−2.6	1.15@	—	—
	−0.92	0.16	11.4	4.5	−2.5	5.2	0.36@	—	—
NGC 6334 I(N)	<0.31	0.11	1.7	—	—	—	<0.87	—	—
AFGL 2591	0.85	0.077	2.3	8	−4.6	0.9	3.7	—	—
NGC 7538 IRS1	0.41	0.12	2.9	10.7	−57.7	0.3	2.7	—	—
OH⁺ (1–0) 1033.1186 GHz									
NGC 1333 I2A	<0.055	0.018	0.26	—	—	—	<−0.59@	9	<5.2(12)
NGC 1333 I4A	−0.040	0.020	0.25	1.4	4.1	−2.8	≤0.2@	9	≤1.9(12)
NGC 1333 I4B	−0.043	0.019	0.17	1.7	1.8	−5.2	≤0.63@	9	≤5.7(12)
Ser SMM1	−0.20	0.065	0.43	9.7	4.8	−3.7	8.3@	9	7.3(13)
L 1489	<0.50	0.017	0.037	—	—	—	<3.9@	9	<3.4(13)
NGC 7129 FIRS2	−0.024	0.021	0.22	7.4	−1.9	8.0	1.0@	9	8.8(12)
W3 IRS5	−0.2	0.015	1.7	5.9	−42	−3.6	0.99@	9	8.8(12)
	0.1	0.015	1.7	9.4	−33	5.4	0.50	38	5.9(11)
NGC 6334 I	−0.55	0.031	6.0	5.9	−10.0	−2.3	0.66@	9	5.2(12)
	−2.1	0.031	6.0	6.4	−1.6	6.1	2.8@	9	2.3(13) DC
NGC 6334 I(N)	−0.99	0.021	3.0	4.9	−1.6	2.9	3.8@	9	3.3(13)
	−1.35	0.021	3.0	3.5	3.2	7.7	3.7@	9	3.3(13) DC
AFGL 2591	−0.14	0.016	0.90	11.8	−16.1	−10.6	1.0@	3 ^a	1.6(13) ^a
	−0.71	0.016	0.90	9.4	2.8	8.3	3.6@	3 ^a	6.1(13) ^a DC
S 140	−0.30	0.024	0.96	4.5	−4.1	3.0	1.5@	9	1.8(13)
	−0.18	0.024	0.96	6.7	3.5	10.6	1.3@	9	1.5(13) DC
NGC 7538 IRS1	−0.18	0.026	1.6	12.0	−48	9.4	1.6@	9	1.4(13)

Notes. $T_{\max}$ refers to the line peak intensity, negative values indicate absorption in [K] below background; ΔV to the FWHM line width; V_{line} to the line mean velocity; $\delta V = V_{\text{line}} - V_{\text{LSR}}$ to the line shift with respect to the systemic velocity of the object; rms to the root mean square noise level; T_b to the background (continuum) intensity; the integrated line flux (line luminosity) is given in [K km s⁻¹], @ indicates integrated optical depth [km s⁻¹]; T_{ex} is the assumed excitation temperature; and N_i is the total column density. Cases where the fitted line model had to be used for intensity or absorption instead of the observed data because of line blending are indicated with an asterisk (*), and values labeled (a) are from 1D slab model fitting (Bruderer et al. 2010a, Appendix B). A minus sign (−) indicates observations but no detection. Absorption components indicated with “DC” are suspected to originate from diffuse interstellar clouds in the foreground. The error range in emission measure is up to factors of 0.8–2 for emission lines, and factors of 0.8–1.5 for lines in absorption. Details and error margins of the column densities are given in Sect. 4 and Table 3.

Table B.1. continued.

	$T_{\max}$ [K]	rms [K]	T_b [K]	ΔV [km s ⁻¹]	V_{line} [km s ⁻¹]	δV [km s ⁻¹]	$\int T_{\text{MB}} dV$ @ = $\int \tau dV$	T_{ex} [K]	N_i [cm ⁻²]
H₂O⁺									
1115.2041 GHz									
NGC 1333 I2A	<0.069	0.023	0.34	–	–	–	<0.57 [@]	9	<4.9(12)
NGC 1333 I4A	<0.060	0.020	0.29	–	–	–	<0.58 [@]	9	<4.9(12)
NGC 1333 I4B	<0.069	0.023	0.20	–	–	–	<0.97 [@]	9	<8.5(12)
Ser SMM1	<0.071	0.024	0.52	5.5	5.0	–3.5	<0.52 [@]	9	≤4.7(12)
L 1489	<0.065	0.022	0.033	–	–	–	<5.60 [@]	9	<5.1(13)
NGC 7129 FIRS2	<0.060	0.020	0.25	–	–	–	<0.68 [@]	9	<6.0(12)
W3 IRS5	–0.10	0.018	2.0	5.3	–42.7	–4.3	0.36 [@]	9	3.2(12)
NGC 6334 I	<0.054	0.018	7.3	–	–	–	<0.070 [@]	9	<6.3(11)
NGC 6334 I(N)	<0.070	0.023	3.1	–	–	–	<0.063 [@]	9	<1.9(12)
AFGL 2591	–0.27	0.017	1.1	13.5 ^a	–16.4 ^a	–10.9 ^a	0.24 [@]	8 ^a	5.4(12) ^a
	–0.57	0.017	1.1	4.5 ^a	2.2 ^a	7.7 ^a	0.37 [@]	3 ^a	8.3(12) ^a DC
S 140	<0.096	0.032	1.0	–	–	–	<0.27 [@]	9	<1.8(12)
NGC 7538 IRS1	≤0.042	0.018	1.9	4.5	–66.1	–9.9	≤0.057 [@]	9	≤5.1(11)
H₃O⁺									
1031.2995 GHz									
NGC 1333 I2A	<0.069	0.019	0.26	–	–	–	<0.18	225	<1.7(12)
NGC 1333 I4A	<0.069	0.020	0.25	–	–	–	<0.19	225	<2.0(12)
NGC 1333 I4B	<0.053	0.017	0.17	–	–	–	<0.14	225	<1.5(12)
Ser SMM1	<0.063	0.019	0.43	–	–	–	<0.17	225	<1.8(12)
L 1489	<0.066	0.017	0.036	–	–	–	<0.18	225	<1.9(12)
NGC 7129 FIRS2	<0.054	0.017	0.23	–	–	–	<0.15	225	<1.5(12)
W3 IRS5	0.61	0.017	1.7	5.7	–37.0	1.4	3.8*	225	3.9(13)
NGC 6334 I	0.48	0.015	5.9	4.6	–4.8	2.9	2.4*	225	2.5(13)
NGC 6334 I(N)	0.048	0.018	3.0	11	–5.2	–0.7	≤0.89*	225	≤9.2(12)
AFGL 2591	0.090	0.0095	0.90	7.4	–4.6	0.9	0.71*	225	7.4(12)
S 140	0.046	0.016	0.96	3.2	–5.5	1.6	<0.2*	225	<2.1(12)
NGC 7538 IRS1	<0.061	0.020	1.5	–	–	–	<0.17	225	<1.8(12)
SH⁺									
526.0479 GHz									
NGC 1333 I2A	<0.011	0.0037	0.028	–	–	–	<0.031	38	<5.5(10)
NGC 1333 I4A	<0.013	0.0044	0.082	–	–	–	<0.037	38	<6.5(10)
NGC 1333 I4B	<0.014	0.0046	0.0051	–	–	–	<0.039	38	<6.9(10)
Ser SMM1	<0.015	0.0051	0.085	–	–	–	<0.043	38	<7.6(10)
L 1489	<0.016	0.0053	0.009	–	–	–	<0.045	38	<8.0(10)
NGC 7129 FIRS2	<0.017	0.0057	0.036	–	–	–	<0.048	38	<8.5(10)
W3 IRS5	0.062	0.0055	0.29	5.2	–38.9	–0.50	0.56*	38	9.5(11)
NGC 6334 I	<0.026	0.0087	0.81	–	–	–	<0.073	38	<1.3(11)
NGC 6334 I(N)	<0.015	0.0050	0.077	–	–	–	<0.042	38	<7.4(10)
AFGL 2591	<0.029	0.0097	0.11	–	–	–	<0.082	38	<1.5(11)
NGC 7538 IRS1	<0.014	0.0048	0.26	–	–	–	<0.041	38	<7.3(10)

Notes. Values labeled (a) are from 1D slab model fitting by [Bruderer et al. \(2010b\)](#). H₂O⁺ column densities are total values assuming an ortho-to-para ratio of three.

Table B.1. continued.

	$T_{\max}$ [K]	rms [K]	T_b [K]	ΔV [km s ⁻¹]	V_{line} [km s ⁻¹]	δV [km s ⁻¹]	$\int T_{\text{MB}} dV$ @ = $\int \tau dV$	T_{ex} [K]	N_i [cm ⁻²]
HCO⁺ 535.0615 GHz									
NGC 1333 I2A	0.78	0.0038	0.028	1.7	7.5	0.0	2.3	38	1.5(12)
	0.20	0.0038	0.028	3.9	7.9	0.4			
NGC 1333 I4A	0.86	0.0050	0.078	2.1	6.9	0.0	3.6	38	2.3(12)
	0.15	0.0050	0.078	7.1	8.5	1.6			
NGC 1333 I4B	0.60	0.0052	0.050	2.4	6.9	-0.1	2.5	38	1.6(12)
	0.099	0.0052	0.050	8.1	7.3	0.3			
Ser SMM1	1.1	0.0057	0.078	2.9	8.3	-0.2	6.0	38	3.8(12)
	0.15	0.0057	0.078	14	8.2	-0.3			
L 1489	0.078	0.0033	0.0021	3.3	6.9	-0.3	0.45	38	3.0(11)
	0.024	0.0033	0.0021	9.4	6.2	-1.0			
NGC 7129 FIRS2	0.42	0.0055	0.036	2.5	-9.7	0.2	1.6	38	1.0(12)
	0.046	0.0055	0.036	8.3	-9.3	0.6			
W3 IRS5	6.1	0.0063	0.29	5.3	-38.1	0.3	44	38	2.8(13)
	0.48	0.0063	0.29	18	-38.9	-0.5			
NGC 6334 I	4.0	0.0055	0.80	6.1	-7.2	0.5	29	38	1.9(13)
	0.095	0.0055	0.80	30	-5.7	2.0			
NGC 6334 I(N)	2.3	0.0057	0.77	4.2	-5.5	-1.0	23	38	1.5(13)
	1.9	0.0057	0.77	5.3	-1.2	3.3			
AFGL 2591	1.9	0.010	0.11	3.6	-5.8	-0.3	9.7	38	6.3(12)
	0.30	0.010	0.11	7.7	-7.0	-1.5			
S 140	7.2	0.013	0.026	3.5	-6.9	0.2	33*	38	2.1(13)
	0.49	0.013	0.026	12	-6.2	0.9			
NGC 7538 IRS1	4.3	0.0041	0.26	3.7	-57.4	0.0	25	38	1.6(13)
	0.78	0.0041	0.26	8.7	-58.1	-0.7			
C⁺ 1900.5369 GHz									
NGC 1333 I2A	-0.18	0.076	0.52	7.2	3.2	-4.3	2.8@	38	4.7(17)
NGC 1333 I4A	-0.040	0.059	0.70	5.8	1.1	-5.8	≤0.69@	38	≤1.2(17)
NGC 1333 I4B	<2.4	0.081	0.23	-	-	-	<2.8@	38	<4.7(17)
Ser SMM1	-0.18	0.076	1.1	5.1	1.3	-7.2	0.93@	38	1.6(17)
W3 IRS5	42	0.055	4.3	5.9	-33.8	4.6	>310	38	>5.6(18)
	13	0.055	4.3	2.4	-43.7	-5.3	-		
AFGL 2591	30	0.172	3.0	6.8	-4.2	1.3	>280	38	>5.0(18)
	12	0.172	3.0	5.9	-15.9	-10.4	-		
S 140	12	0.78	12.5	4.3	-8.5	-1.4	>28	38	≥5.0(17)
CH 536.7611 GHz									
NGC 1333 I2A	0.017	0.0024	0.027	1.8	7.1	-0.4	0.031	38	1.9(11)
NGC 1333 I4A	0.040	0.0026	0.078	0.70	6.8	-0.1	0.068	38	4.3(11)
NGC 1333 I4B	0.029	0.0025	0.053	0.59	6.8	-0.2	0.051	38	3.2(11)
Ser SMM1	0.028	0.0022	0.086	0.61	7.8	-0.7	0.049	38	3.1(11)
	0.012	0.0022	0.086	9.4	9.0	0.5	0.094	38	6.3(12)
L 1489	<0.017	0.0058	0.00099	-	-	-	<0.022	38	<1.4(11)
NGC 7129 FIRS2	0.013	0.0025	0.040	7.2	-4.9	5.0	0.14	38	8.8(11)
W3 IRS5	1.0	0.0060	0.28	4.7	-36.3	2.1	14	38	8.8(13)
NGC 6334 I	0.28	0.014	0.80	2.6	-8.5	-0.8	2.1	38	1.3(13)
NGC 6334 I(N)	-3.0	0.0059	0.7	3.3	-2.0	2.5	3.3@	6	1.2(14)
AFGL 2591	0.26	0.0086	0.10	4.7	-5.5	0.0	2.9	38	1.8(13)
S 140	0.22	0.0061	0.021	3.5	-6.6	0.5	1.6	38	1.0(13)
NGC 7538 IRS1	0.25	0.0059	0.26	4.8	-58.3	-0.9	4.0	38	2.5(13)

Notes. Column densities of HCO⁺ (6–5) are lower limits because of high optical thickness (see Sect. 3).

Appendix C: Details of correlation analysis

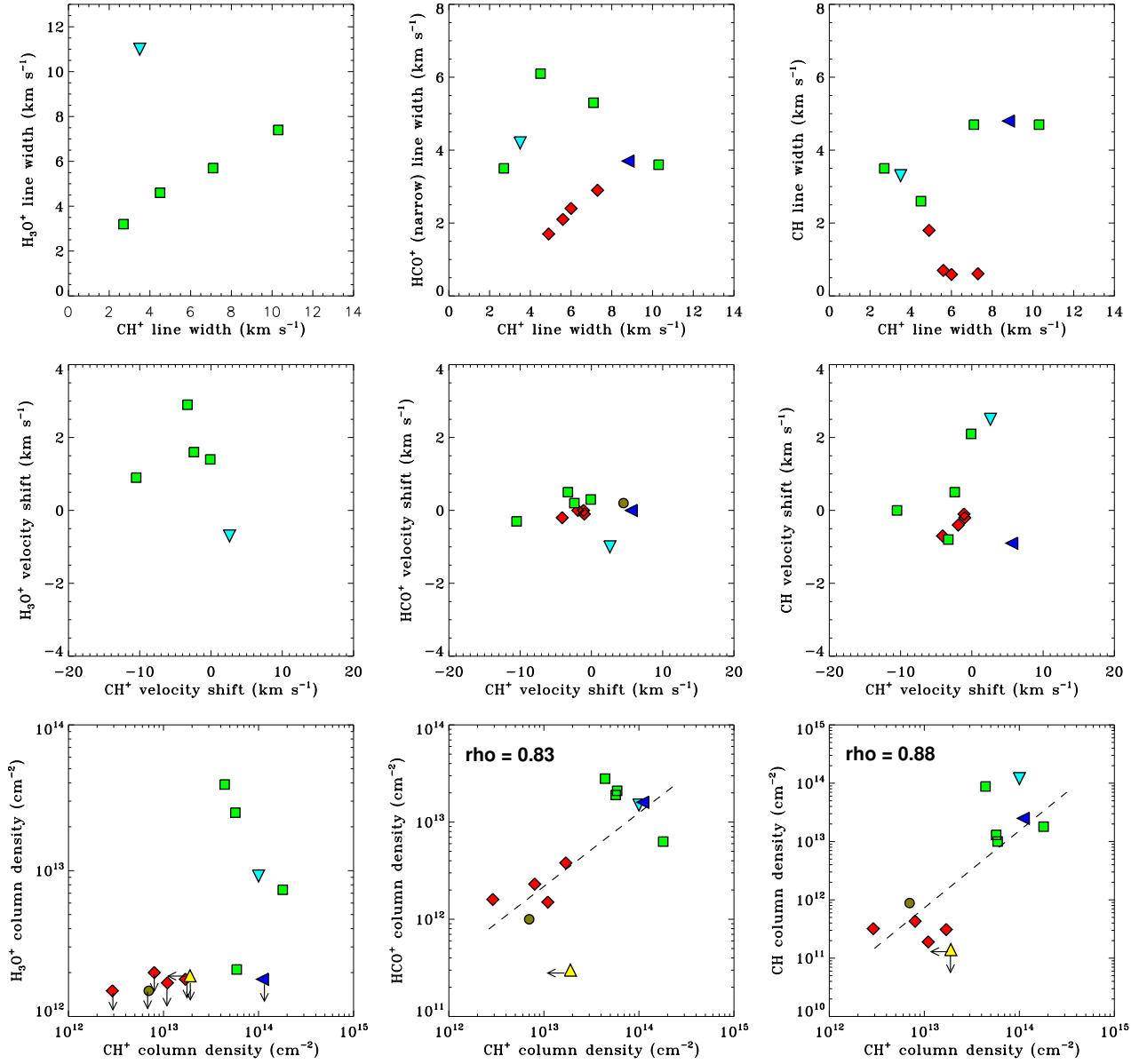


Fig. C.1. Observed line parameters (Table B.1) of H_3O^+ , HCO^+ (narrow component), and CH vs. the observed line characteristics of CH^+ . The Pearson correlation coefficient ρ is given where statistically significant (see Sect. 4.2). The upper limit for L 1489 is not included in the analysis. The symbols indicate different types of objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

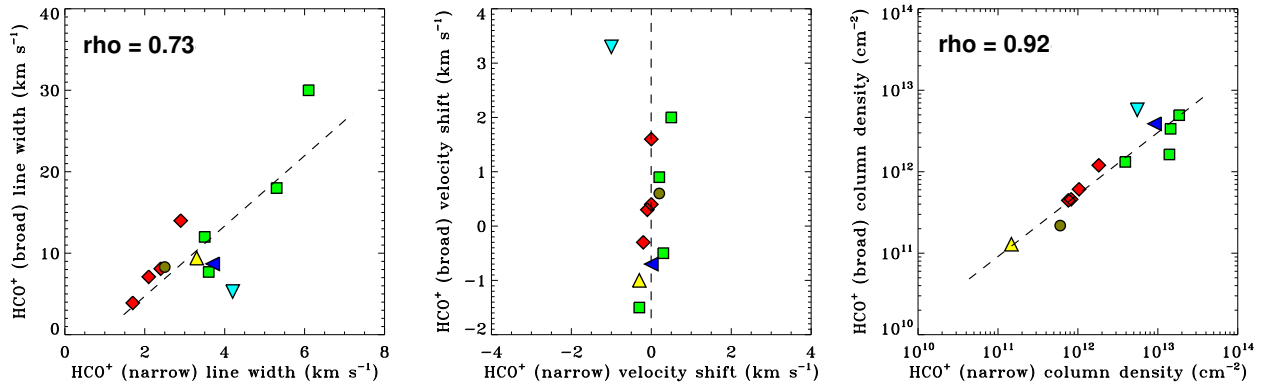


Fig. C.2. Observed line parameters of the narrow component vs. the broad component of $\text{HCO}^+(6-5)$ as given in Table B.1. For the notation of the symbols see Fig. C.1.

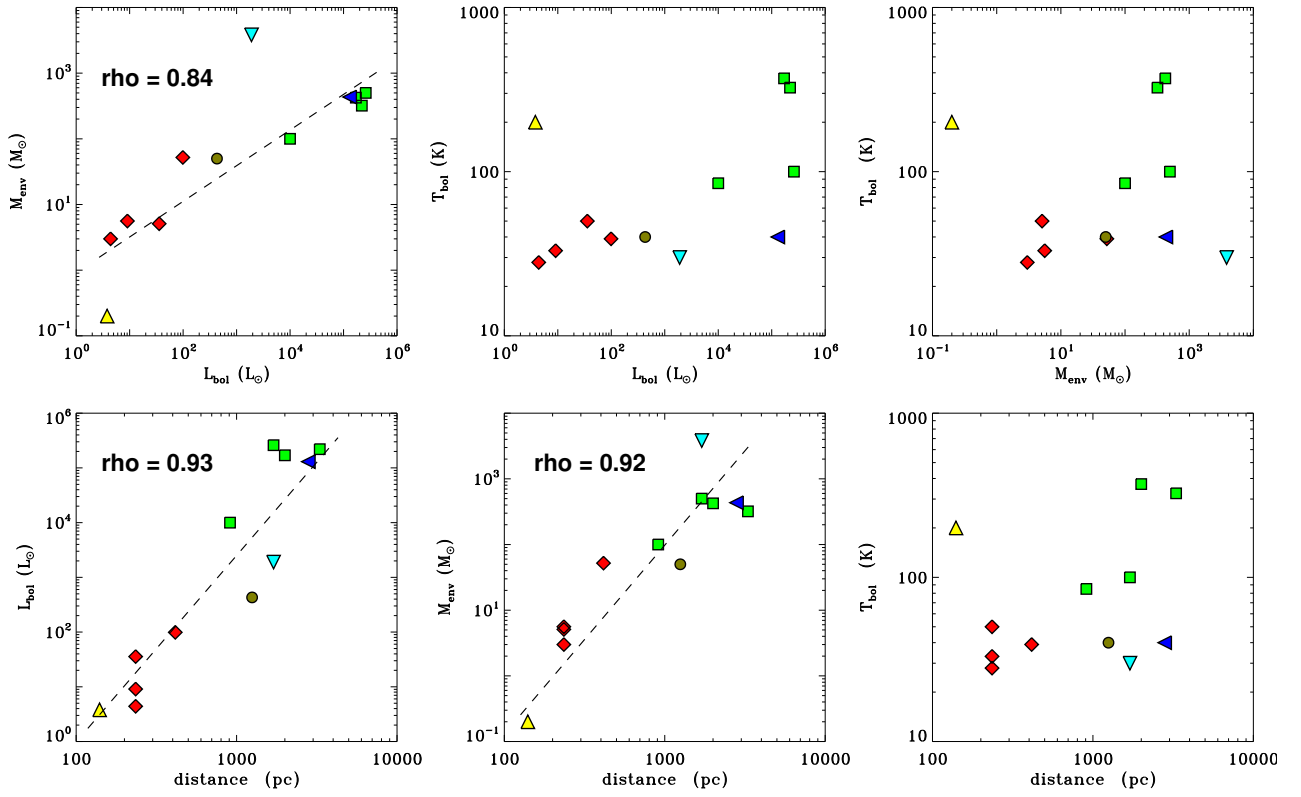


Fig. C.3. Correlations between object parameters as listed in Table 1. The symbols indicate different types of objects: red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

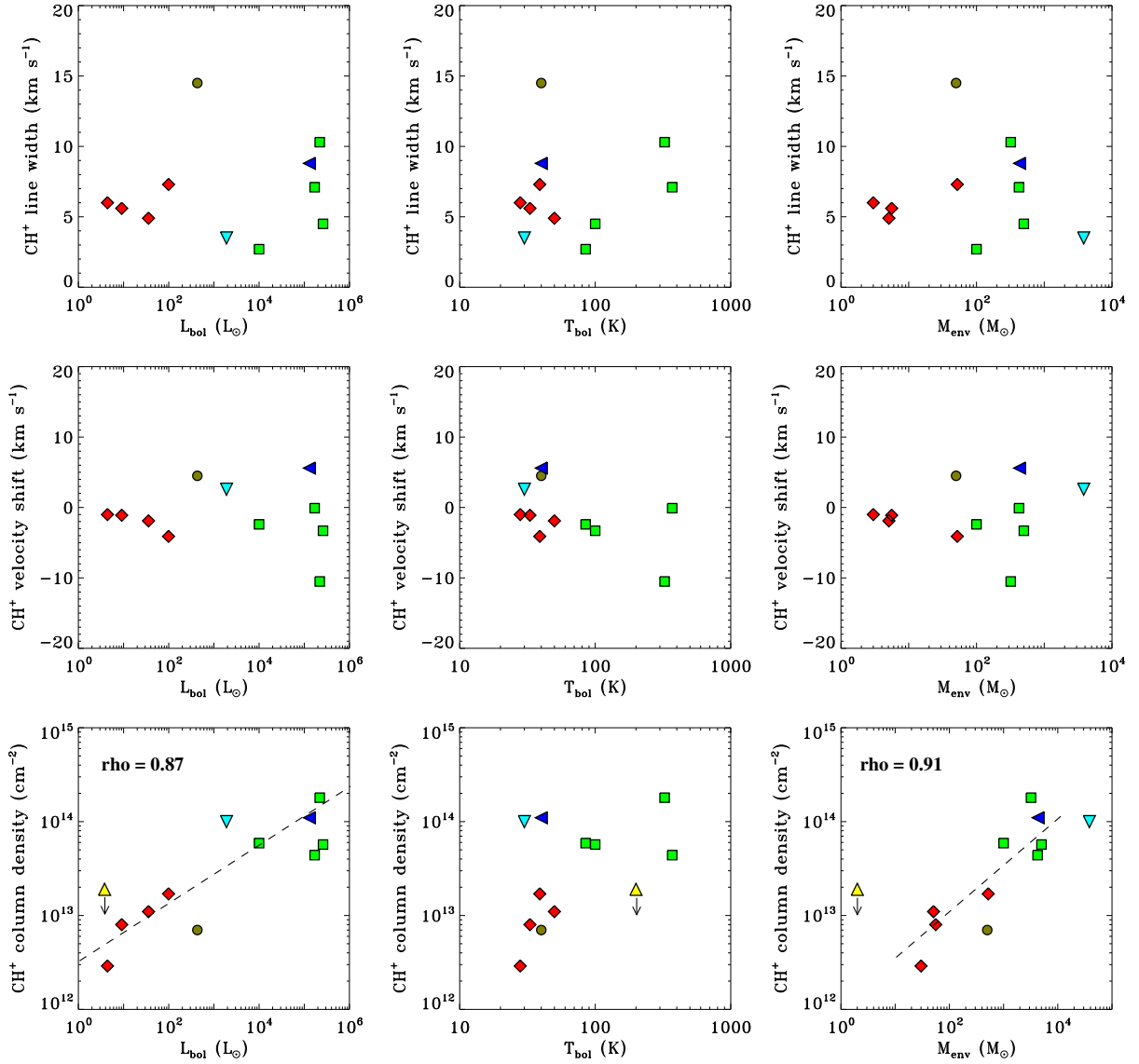


Fig. C.4. Observed CH⁺(835 GHz) line characteristics (Table B.1) vs. object parameters given in Table 1. Only the line component in absorption is shown. L 1489 is not included in the correlation coefficient ρ , given where statistically significant. The symbols indicate different types of objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

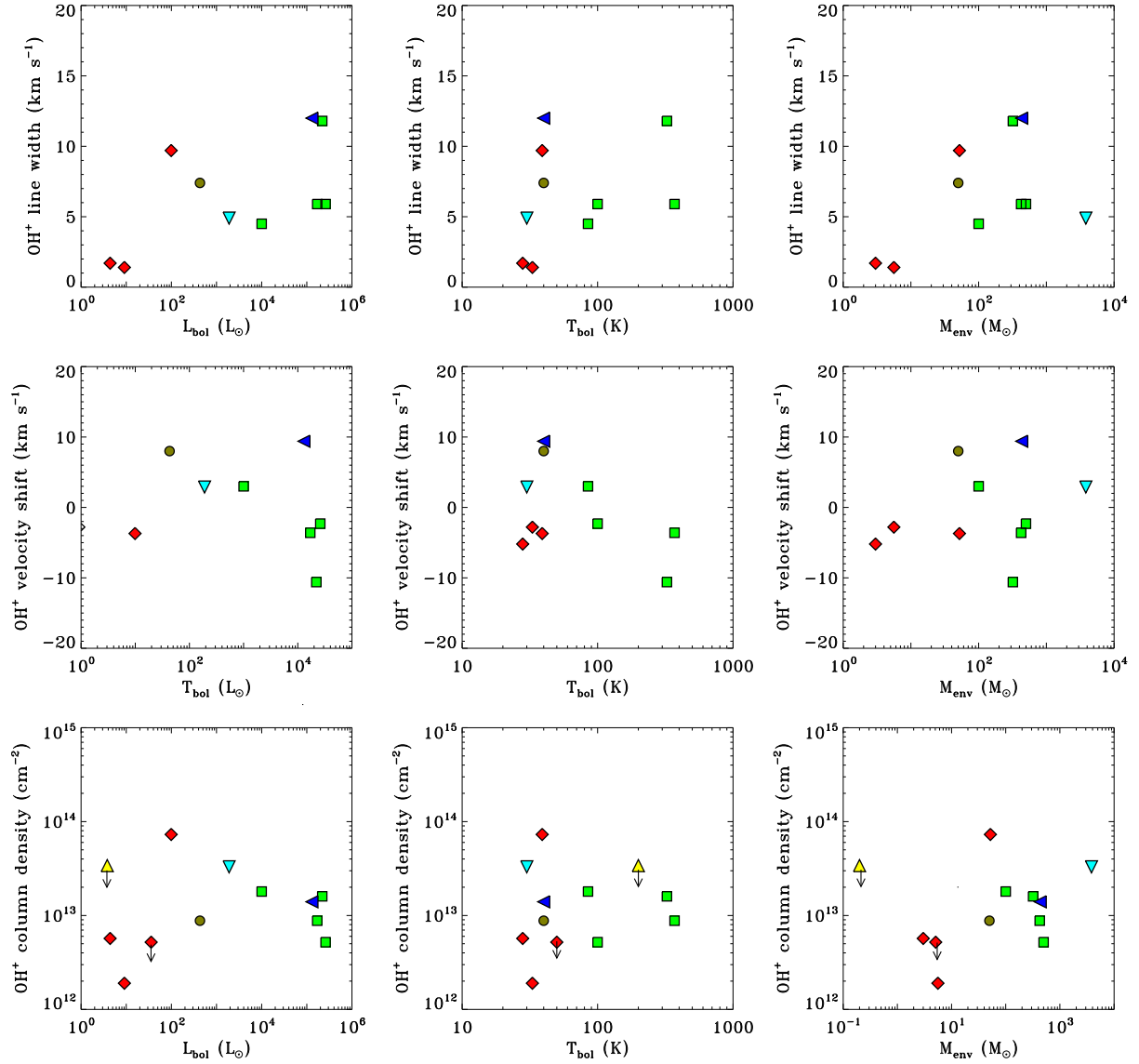


Fig. C.5. Observed OH⁺(1033 GHz) line characteristics (Table B.1) vs. object parameters given in Table 1. Only the line component in absorption is considered. The correlations are not statistically significant. The symbols indicate different types of objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

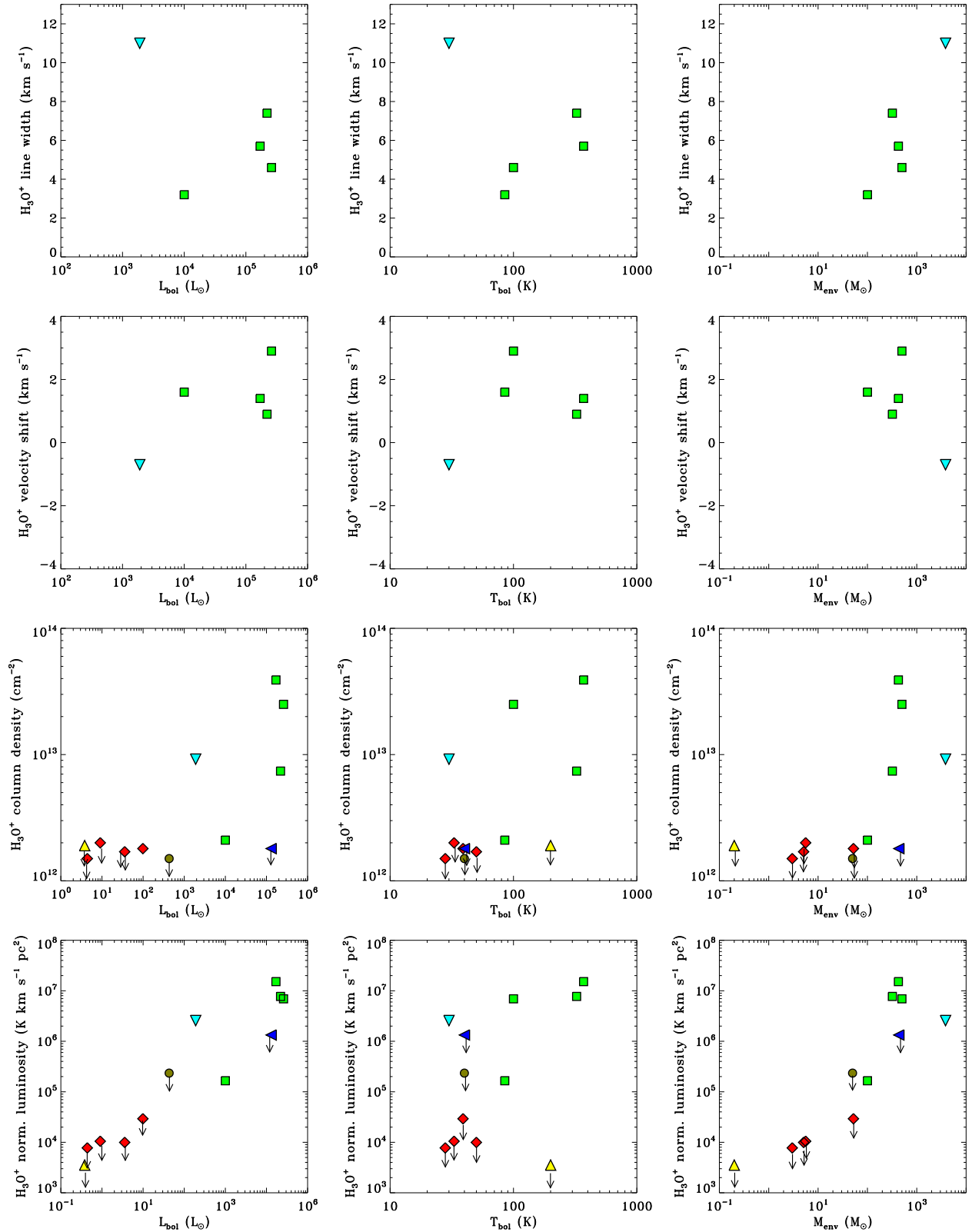


Fig. C.6. Observed H_3O^+ (1031 GHz) line characteristics (Table B.1) vs. object parameters given in Table 1. The line is in emission. The *bottom row* shows the line luminosity multiplied with distance squared (normalized to 1 pc) to correct in case of point-source emission. The symbols mark different types of objects: red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

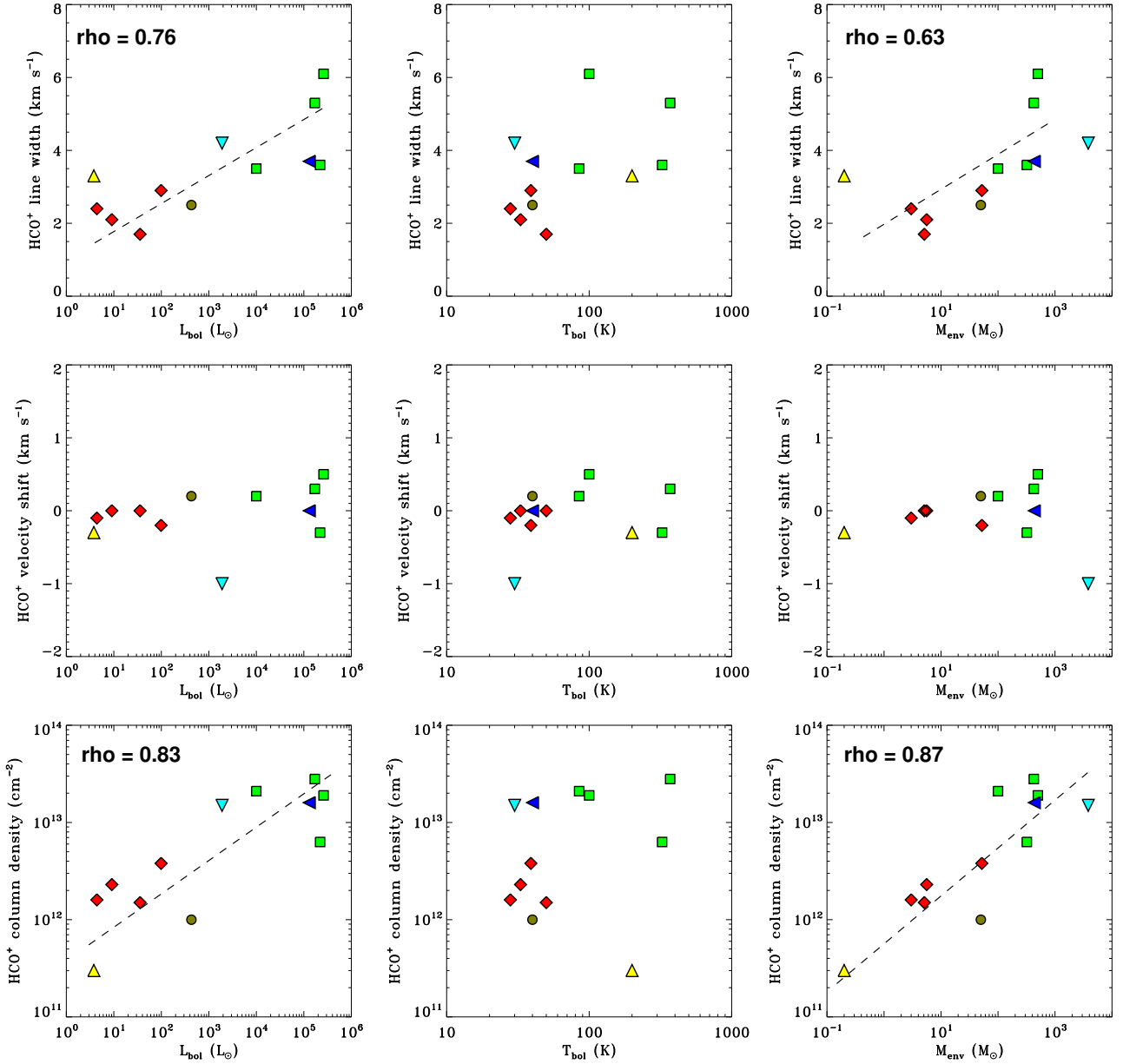


Fig. C.7. Observed line width and shift of the narrow component of HCO⁺(6–5) and its total column density (Table B.1) vs. object parameters given in Table 1. The line is in emission. The correlations of intensity normalized in distance are displayed in Fig. 6. The symbols indicate different types of objects: red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

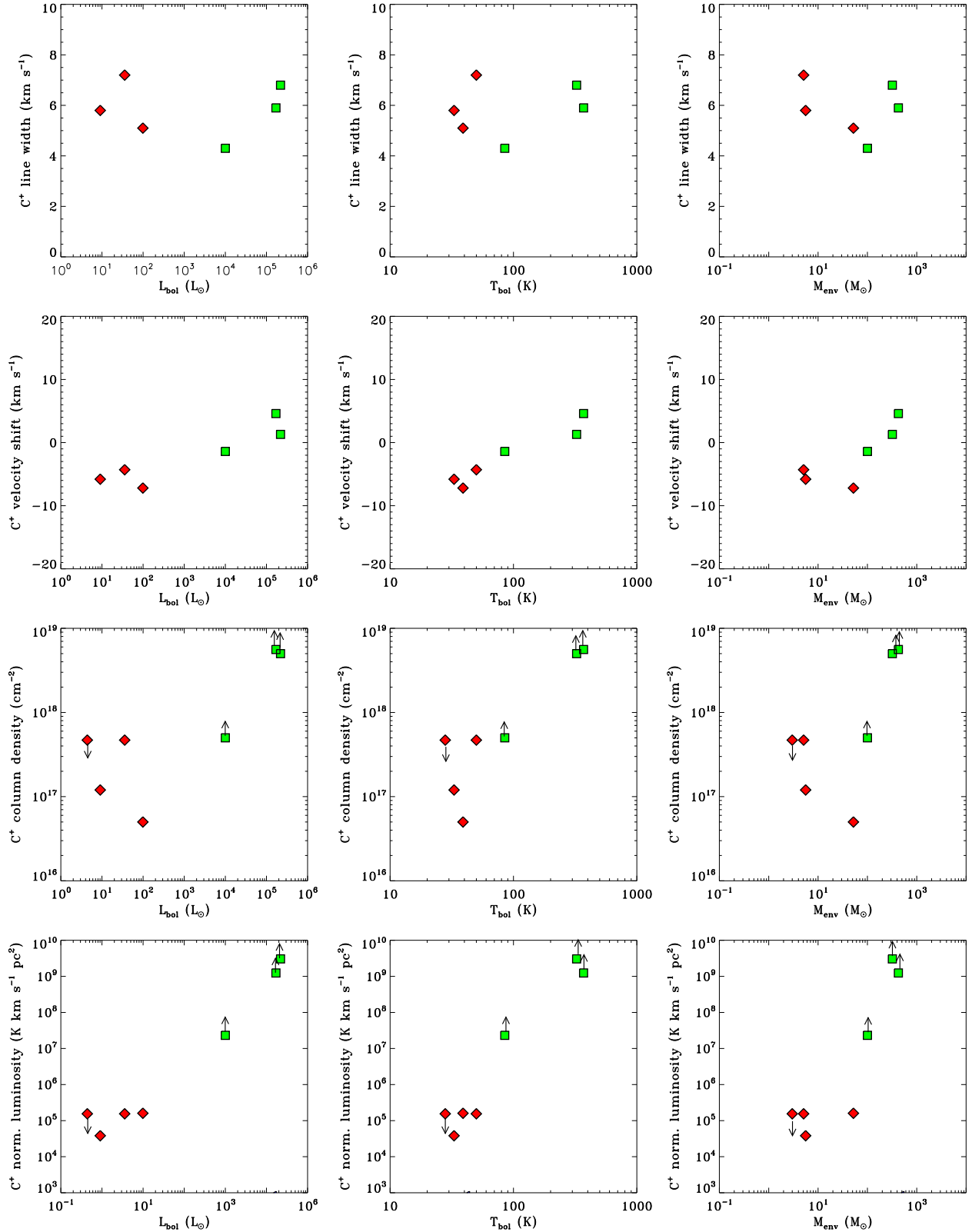


Fig. C.8. Observed C^+ (1900 GHz) line characteristics (Table B.1) vs. object parameters given in Table 1. The line is in absorption toward the low-mass objects and in emission toward the high-mass objects. The bottom row shows the luminosity of the transition normalized for the case of point-source emission. The symbols indicate different types of objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

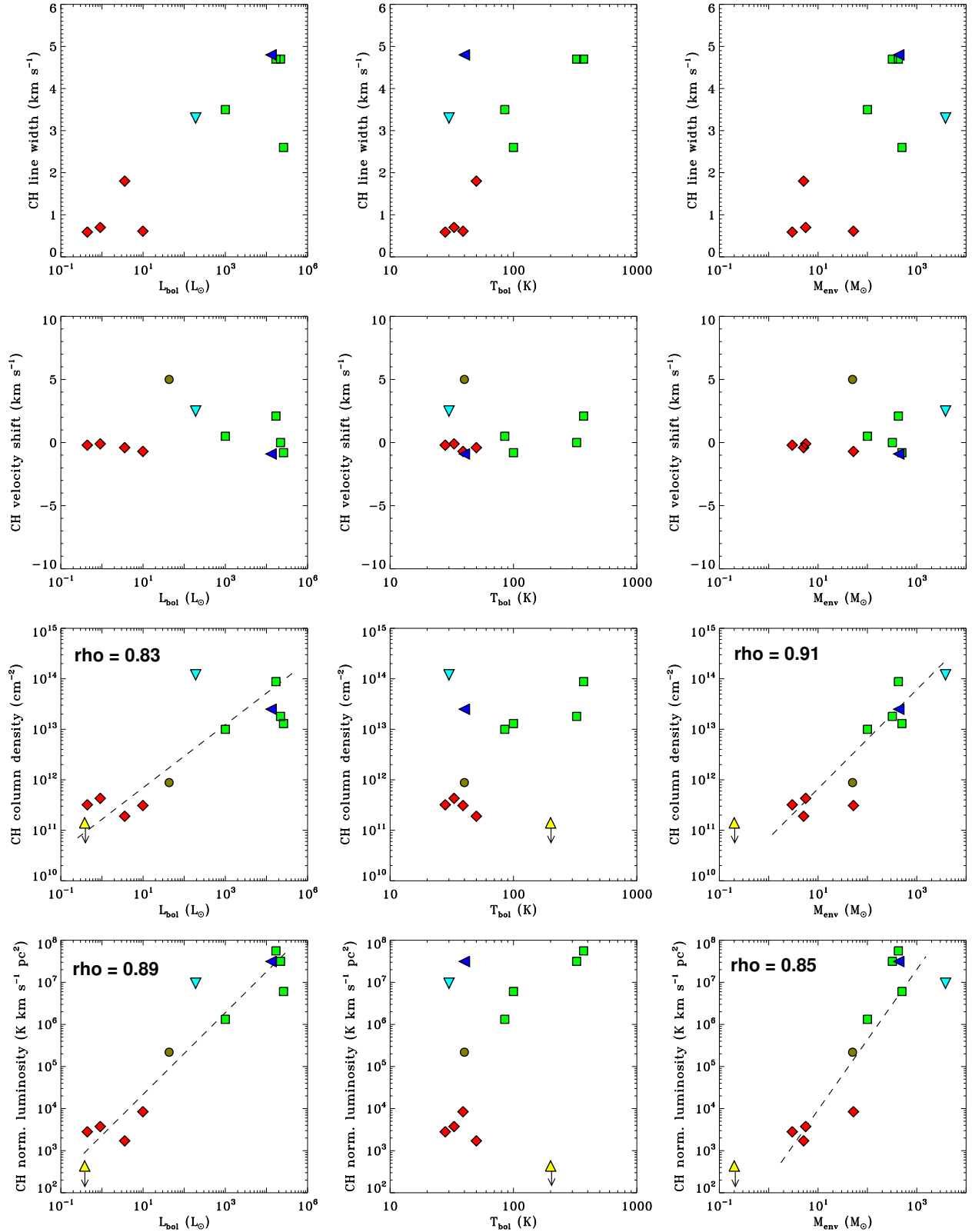


Fig. C.9. Observed CH (536 GHz) line characteristics (Table B.1) vs. object parameters given in Table 1. Only the line component in emission is considered; for Ser SMM1 only the narrow component. The bottom row shows the luminosity normalized to 1 pc for the case of point-source emission. L 1489 is not included in the correlation coefficient ρ , which is given where statistically significant. The symbols indicate different types of objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

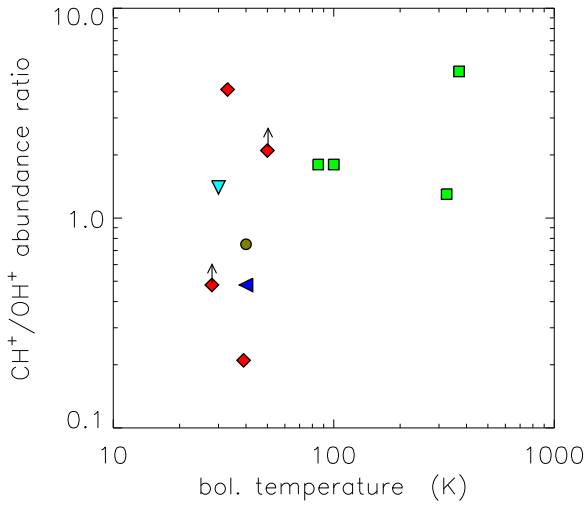


Fig. C.10. CH^+/OH^+ column density ratio of absorption components vs. bolometric temperature. L 1489 (Class I) has upper limits in both CH^+ and OH^+ , and is not shown. The symbols indicate different types of objects: Red diamonds for Class 0, yellow triangle up for Class I (L 1489), brown circle for intermediate mass, light blue triangle down for high-mass mid-IR quiet (NGC 6334 I(N)), green square for high-mass mid-IR bright and hot molecular core, and dark blue triangle left for high-mass ultra-compact HII (NGC 7538 IRS1).

Table C.1. Observations according to the *Herschel* Science Archive (last six digits of ObsID, preceding 1342 omitted).

Object	CH^+ 1–0	CH^+ 2–1	OH^+ 1 ₁ –0 ₁	H_2O^+ 1 ₁₁ –0 ₀₀	H_3O^+ 4 ₃₀ –3 ₃₁	SH^+ 1 ₂ –0 ₁	HCO^+ 6–5	CH 1 _{–1} –1 ₁	C^+ $^2P_{3/2}$ – $^2P_{1/2}$
NGC 1333 I2A	203229	215966	203180	191657	203180	202024	202024	202024 192206	201840
NGC 1333 I4A	203230	203951	203181	191656	203181	202023	202023	202023 192207	201841
NGC 1333 I4B	203228	203952	203178	191655	203178	202022	202022	202022 202033	201842
Ser SMM1	207620	207660	207656	207379	207656	207581	207581	207581 194463	208575
L 1489	203227		203159	203938	203159	203187	203187		
NGC 7129 FIRS2	201704		197969	191676	197969	198330	198330	192362	
NGC 6334 I	214305	214454	204514 204515	206385	204514	205281	205281		
S 140	196463		197966 197967	200762	197966		195050	195050	190781
AFGL 2591	196471 196472	196531	195021 195022	196429 196430	195021 195022	194484	194484	194484	195118 195119
W3 IRS5	201701 201702	201763 201764	191608 191609	191661 191662	191608 191609	191501 191502	191501 191502	191501 191502	191774 191775
NGC 6334 I(N)	214306 214307	214455	204516 204517	206383	204516 204517	205280	205280	205280	
NGC 7538 IRS1	201703	200758	197962 197963	191663 197976	197962 197963	198331	198331 197976	198331	

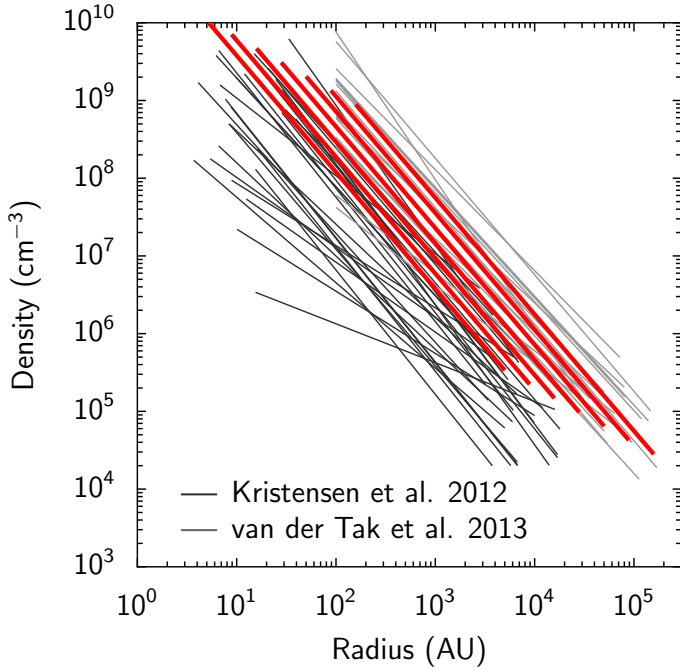


Fig. D.1. Density profiles derived from observations (grey: high mass, black: low mass) compared to the model density profiles (red), which represent seven bolometric luminosities of $L_{\text{bol}} = \{1, 10, \dots, 10^6\} L_{\odot}$, increasing to the right.

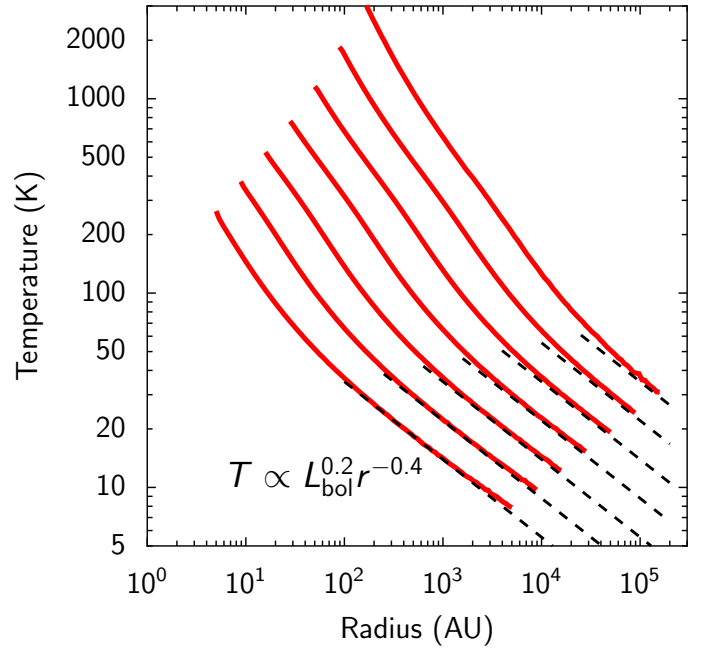


Fig. D.2. Temperature profiles of the seven models (red) given in Fig. D.1 derived by a dust radiative transfer calculation. The fits used in the analytic approximation (Eq. (D.6)) are indicated by dashed lines (black).

Appendix D: HCO⁺ Correlation with L_{bol}

The correlation between the bolometric luminosity L_{bol} and the HCO⁺($J = 6-5$) distance-corrected integrated line intensity is excellent (Fig. 6). To explain the tight correlation, a set of radiative transfer models is run. We assume a spherically symmetric envelope with a power-law density profile

$$n(r) = n_0 \left(\frac{r}{r_{\text{out}}} \right)^{\alpha} \quad (\text{D.1})$$

and a radial range between r_{in} and r_{out} . To roughly approximate the envelope properties constrained by Kristensen et al. (2012) toward low-mass stars and van der Tak et al. (2013) toward high-mass stars, we set $\alpha = -1.5$, $r_{\text{in}} = 5 L_{\text{bol}}^{1/4}$ AU, and $r_{\text{out}}/r_{\text{in}} = 1000$. The parameter n_0 is adjusted to reproduce the $M_{\text{env}} = 1.1 L_{\text{bol}}^{0.54}$ relation presented in Fig. C.3, top left, and given in Eq. (5). Figure D.1 shows the resulting density profiles, which lie within the range of profiles derived from observations. The largest deviation at low density is for the (low envelope mass) Class I object.

The model density profiles serve as input for a dust radiative transfer calculation to obtain the dust temperature. The code of Bruderer et al. (2010a), benchmarked against DUSTY (Ivezić & Elitzur 1997) in Bruderer (2010), Appendix D, is applied. We assume good coupling between dust and gas temperatures in the bulk mass of the envelope (Doty & Neufeld 1997; Doty et al. 2002), from where the HCO⁺ emission originates, thus $T_{\text{gas}} \approx T_{\text{dust}}$ is an appropriate approximation. The result is shown in Fig. D.2. In the outer layers, the temperature is a power law, which is used later in the analytical approach (Eq. D.6).

For the model calculations we use various constant fractional abundances of HCO⁺ between $x_{\text{HCO}^+} = 10^{-10}$ and $x_{\text{HCO}^+} = 10^{-7}$. The line radiative transfer problem is solved with the RATRAN code (Hogerheijde & van der Tak 2000). Molecular data from the LAMDA database (Schöier et al. 2005) are used. The

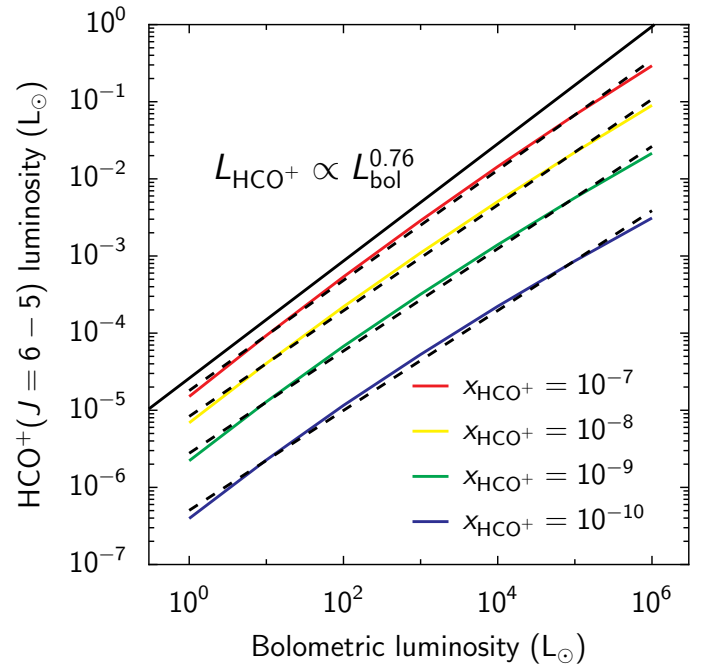


Fig. D.3. L_{bol} vs. $L_{\text{HCO}^+}(J = 6-5)$ relation (full curves). The color indicates the 4 different HCO⁺ abundances used. The model results are compared to the observed $L_{\text{HCO}^+} \propto L_{\text{bol}}^{0.76 \pm 0.08}$ power-law, indicated by a black solid line at the top (in arbitrary units) and power-law fits to the model relation (black dashed lines).

results are presented in Fig. D.3. From the fractional abundance $x_{\text{HCO}^+} = 10^{-10}$ to $x_{\text{HCO}^+} = 10^{-7}$, the power-law index increases from 0.64 to 0.71 (fits shown by dashed lines in the figure). We have also calculated models with a HCO⁺ freeze-out taken into account, decreasing the HCO⁺ abundance by a factor of 30 in regions with temperature below 20 K, but the results do not

change significantly (power-law index between 0.66 and 0.79). Independent of the fractional abundance of HCO^+ , the radiative transfer models can thus reproduce the observed relation having an exponent of 0.76 ± 0.08 .

To understand the results of the numerical calculation, we roughly retrieve them from an analytical calculation. According to the model calculations, the HCO^+ ($J = 6-5$) line is formed in the outer part of the envelope and optically thick; the high dust temperatures in the inner part of the models of the highest L_{bol} models do not affect the results. Thus we will use the fitted power-law temperatures for an analytical derivation below.

Since the HCO^+ lines are optically thick and the line luminosity scales as

$$L_{\text{HCO}^+} \propto r_{\text{thick}}^2 B_{\nu}(T(r_{\text{thick}})), \quad (\text{D.2})$$

where r_{thick} is the radius at which the line gets optically thick ($\tau \approx 1$) and $B_{\nu}(T(r))$, the blackbody function (Rayleigh-Jeans approximation) for the temperature at the radius r . We assume that r_{thick} is such, that the column density, N_{thick} , from this radius to the outer edge of the envelope is the same for all sources. This is a good approximation, since the line opacity is proportional to the column density, but neglects excitation effects. We thus solve

$$N_{\text{thick}} = \int_{r_{\text{thick}}}^{r_{\text{out}}} n(r) dr = \text{const.}, \quad (\text{D.3})$$

for r_{thick} in the two extreme cases $N_{\text{thick}}(\alpha + 1)/n_0 \ll$ and $\gg r_{\text{out}}$. Using the model assumptions and Eq. (5),

$$n_0 \propto M_{\text{env}}/r_{\text{out}}^3 \propto L_{\text{bol}}^{-0.21}. \quad (\text{D.4})$$

Therefore, Eq. (D.3) yields a relation between r_{thick} and L_{bol}

$$r_{\text{thick}} \propto L_{\text{bol}}^{0.25-0.33}, \quad (\text{D.5})$$

where the exponent is limited by the two extreme cases. The temperature profile of the outer envelope can be approximated by

$$T(r) \propto L_{\text{bol}}^{0.2} r^{-0.4}, \quad (\text{D.6})$$

as indicated in Fig. D.2. This relation inserted into Eq. (D.2) yields

$$L_{\text{HCO}^+} \propto r_{\text{thick}}^2 L_{\text{bol}}^{0.2} r_{\text{thick}}^{-0.4}, \quad (\text{D.7})$$

and with the range of power-law indices for r_{thick} given by Eq. (D.5) follows

$$L_{\text{HCO}^+} \propto L_{\text{bol}}^{0.60-0.73}. \quad (\text{D.8})$$

It is consistent with the model calculations (Fig. D.3) and observations (Eq. (6)).

The reason for the tight correlation between L_{bol} and HCO^+ ($J = 6-5$) is the self-similarity of the dust radiative transfer problem (Ivezić & Elitzur 1997), which results in power-law relations for all relevant parameters. Most critical is the temperature. It can be approximated by single power-law in the HCO^+ ($J = 6-5$) line photosphere (Fig. D.2). The different power-law exponents of various YSOs in density, and the deviation from spherical symmetry have little influence on the relation between L_{bol} and HCO^+ . The value of the power-law exponents depends mostly on the radius r_{thick} where the line gets optically thick, thus on the particular molecule and the transition.