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The *Gaia* spectrophotometric standard stars survey – IV. Results of the absolute photometry campaign

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ABSTRACT

We present Johnson–Kron–Cousins *BVRI* photometry of 228 candidate spectrophotometric standard stars for the external (absolute) flux calibration of *Gaia* data. The data were gathered as part of a 10-yr observing campaign with the goal of building the external grid of flux standards for *Gaia* and we obtained absolute photometry, relative photometry for constancy monitoring, and spectrophotometry. Preliminary releases of the flux tables were used to calibrate the first two *Gaia* releases. This paper focuses on the imaging frames observed in good sky conditions (about 9100). The photometry will be used to validate the ground-based flux tables of the *Gaia* spectrophotometric standard stars and to correct the spectra obtained in non-perfectly photometric observing conditions for small zero-point variations. The absolute photometry presented here is tied to the Landolt standard stars system to $\simeq 1$ per cent or better, depending on the photometric band. Extensive comparisons with various literature sources show an overall $\simeq 1$ per cent agreement, which appears to be the current limit in the accuracy of flux calibrations across various samples and techniques in the literature. The *Gaia* photometric precision is presently of the order of 0.1 per cent or better, thus various ideas for the improvement of photometric calibration accuracy are discussed.

Key words: techniques: photometric – catalogues – surveys – stars: general.

1 INTRODUCTION

*Gaia*¹ (Gaia Collaboration 2016a) is a cornerstone mission of the European Space Agency (ESA) that has been performing an all-sky survey since the beginning of the scientific operations in 2014 July, about seven months after the lift-off on 2013 December 19. *Gaia* is building the most complete and precise 6D map of our Galaxy by observing almost 1.7 billion sources from its privileged position at the Lagrangian point L2 and its data are already producing major advancements in all branches of astronomy, from the Solar system and stellar structure to the dynamics of the Milky Way and cosmology

(Perryman et al. 2001; Mignard 2005; Pancino 2020). A description of the satellite and a list, inevitably non-exhaustive, of the mission scientific goals is available in Gaia Collaboration (2016a), while an up-to-date list of refereed *Gaia* papers since launch (more than 3600 as of 2020 July) is maintained on the ESA webpages.²

The very first products provided to the astronomical community were the photometric science alerts,³ with the first transient announced on 2014 August 30, whereas Solar system alerts for new asteroids⁴ started in 2016. The first intermediate data release (*Gaia* DR1) was published on 2016 September 14 (Gaia Collaboration 2016b) and the second intermediate data release (*Gaia* DR2) took

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¹ <https://www.cosmos.esa.int/web/gaia/home>

² <https://www.cosmos.esa.int/web/gaia/peer-reviewed-journals>

³ <https://gsaweb.ast.cam.ac.uk/alerts>

⁴ <https://gaiafunso.imcce.fr/>

place on 2018 April 25 (Gaia Collaboration 2018). The next releases will give increasingly accurate and complete sets of astrophysical data. The upcoming *Gaia* third and following releases are announced by ESA in their regularly updated ‘data release scenario’.⁵ The nominal 5-yr mission ended on 2019 July 16, but the *Gaia* micropropulsion fuel exhaustion is foreseen only by the end of 2024. A 2 yr mission extension was approved and further extensions are under discussion. The final *Gaia* data release will presumably be based on 8, hopefully 10, yr of observations, providing a new astrometric foundation for astronomy.

Gaia performs astrometric, photometric, and spectroscopic measurements by means of two telescopes, observing in directions separated by 106.5° (the ‘basic angle’), but sharing the same focal plane, one of the largest ever sent to space, that hosts five instruments: the Sky Mapper, the Astrometric Field, the Blue Photometer, the Red Photometer, and the Radial Velocity Spectrometer (Gaia Collaboration 2016a). *Gaia* spectrophotometry in particular comes from different instruments. The first is the Astrometric Field, an array of 62 CCDs operating in white light and defining the *Gaia* *G* band, determined by the reflectivity of the mirrors and the quantum efficiency of the detectors. The *G* band covers the optical range (330–1050 nm), peaking around 600 nm. The colour information comes instead from the Blue and Red Photometers (BP and RP), providing low resolution dispersed images in the blue (330–680 nm, $30 \lesssim R \lesssim 100$) and in the red (640–1050 nm, $60 \lesssim R \lesssim 90$) domains. In particular, extremely precise three-band photometry was published in *Gaia* DR2 (Evans et al. 2018), with sub-millimagnitude internal uncertainties. The photometry was obtained by integrating data from the astrometric field and the spectrophotometers, producing the *G*, *G*_{BP}, and *G*_{RP} integrated magnitudes. The quality of the data is so exquisite and unprecedented that subtle systematic effects at the mmag level cannot be tested with existing data sets, because no photometric survey has such similar precision (Evans et al. 2018). The upcoming *Gaia* release will be split into two releases: an early release (EDR3), publishing improved integrated magnitudes, and a DR3 release that will include also the epoch-averaged BP and RP spectra for a selected subset of the observed sources.

As outlined by Pancino et al. (2012) and Carrasco et al. (2016), while the *Gaia* internal calibration is based solely on *Gaia* data, external spectrophotometric standard stars (hereafter SPSS) are required to report the calibration of *Gaia* spectra and integrated photometry on to a physical flux scale. Given the instrument complexity, a large set of SPSS (about 200) is required, adequately covering a wide range of spectral types. The best existing set in the literature in 2006 was CALSPEC (Bohlin, Gordon & Tremblay 2014), but it only contained about 60 stars and the spectral-type coverage was limited for our purpose. The CALSPEC set has evolved significantly over time, most notably by refining the quality of the spectra, their calibration, and by adding three very red objects (Bohlin, Deustua & de Rosa 2019), but still contains only about 90 spectra covering the entire *Gaia* wavelength range. Moreover, even the latest CALSPEC set lacks K and M-type stars, which are mandatory for calibrating *Gaia*. For this reason in 2006 we started an extensive ground-based observing campaign, to provide a suitable SPSS grid, extending the list of the CALSPEC stars that matched our original criteria, both by doubling the number of sources, and by better sampling the colour space towards intermediate and red colours, especially in the FGK stars range and in the early M-type stars. Our spectrophotometric

calibration is tied to the CALSPEC scale by using their three hydrogen white dwarfs (G191-B2B, GD71, GD153, see Bohlin, Colina & Finley 1995) as calibrators of the *Gaia* SPSS grid.

In this paper, we present the results of our absolute photometry campaign. Given the difficulty of obtaining a large amount of very high quality spectrophotometry, we decided to gather photometric observations of our SPSS candidates⁶ with the following goals:

- (i) to refine the literature photometry of the SPSS candidates, that often had large uncertainties;
- (ii) to validate the flux tables obtained from the spectrophotometry under photometric conditions (Sanna et al. 2019)⁷;
- (iii) to validate – and when necessary to adjust – the flux calibration of the spectra obtained under reasonably good but not perfectly photometric conditions.

This is the fourth paper of the *Gaia* SPSS series. The first paper presented the ground-based project, the candidate SSPS, and some preliminary results (Pancino et al. 2012); the second paper presented a detailed study of instrumental effects and the techniques used to minimize their impact (Altavilla et al. 2015); the third paper presented the results of our constancy monitoring campaign (within ± 5 mmag), including all variability curves, and led to the exclusion of several candidate SPSS (some were widely used standards; Marinoni et al. 2016). In this paper, we focus on the imaging data obtained during photometric nights, and we present the absolutely calibrated magnitudes of 228 stars, including 198 candidates SPSS and 30 rejected candidate SPSS. The final release of flux tables based on the spectrophotometric observations will be presented in a forthcoming paper.

The paper is organized as follows: in Section 2 we present the observing campaign and the data analysis; in Section 3 we present the photometric calibration; in Section 4 we validate our results, comparing them with several literature data collections; in Section 5 we discuss the present status of spectrophotometric calibrations in the literature and future prospects, and we finally draw our conclusions.

2 OBSERVATIONS AND DATA REDUCTION

The observing campaign for the *Gaia* SPSS (see also Pancino et al. 2012) started in the second half of 2006 with five pilot runs, used to refine the observing strategy. The main campaign, for both the spectroscopic and photometric data acquisition, started in 2007 January and ended in 2015 July, for a total of 967 different observing nights at eight different telescopes (see Table 1). The data collected during the whole campaign amount to $\simeq 70\,600$ scientific frames ($\simeq 64\,000$ images, and $\simeq 6600$ spectra). Here we focus on the imaging data gathered in good observing conditions (about 9100 frames).

2.1 Photometric observations and data summary

From the whole body of imaging observations, we extracted more than 27 000 individual photometric catalogues, one for each observed imaging frame with sufficient quality ($\simeq 5000$ of which with Landolt 1992a standard stars fields measurements, $\simeq 22\,000$ related to candidate SPSS). The breakdown of the photometric catalogues for each

⁶The final selection of SPSS for the calibration of *Gaia* is done on the flux tables obtained from the spectrophotometry, therefore in this paper all SPSS will be considered candidates.

⁷The *Gaia* Technical Notes cited in this work are publicly available on the ESA webpage: <https://www.cosmos.esa.int/web/gaia/public-dpac-documents>.

⁵<https://www.cosmos.esa.int/web/gaia/release>

Table 1. Facilities used in the photometric observations of the *Gaia* SPSS. The first three columns report the telescope, instrument, and site of each facility used. The last four columns report, respectively: the total number of frames dedicated to imaging, the percentage contributed by each facility, the total number of frames obtained in photometric and good nights, and the percentage contributed by each facility.

Telescope	Instrument	Location	Imaging (#)	Imaging (per cent)	Photometry (#)	Photometry (per cent)
ESO NTT 3.6 m	EFOSC2	La Silla, Chile	2943	10.6	1673	18.4
TNG 3.6 m	DOLoRes	Roque de los Muchachos, Spain	5337	19.2	3217	35.4
NOT 2.6 m	ALFOSC	Roque de los Muchachos, Spain	1140	4.1	497	5.5
CAHA 2.2 m	CAFOS	Calar Alto, Spain	972	3.5	198	2.2
Cassini 1.5 m	BFOSC	Loiano, Italy	6889	24.9	69	0.8
SPM 1.5 m	La Roca	San Pedro Mártir, Mexico	8652	31.2	3440	37.8
REM 0.6 m	ROSS/ROSS2	La Silla, Chile	1695	6.1	0	0.0
TJO 0.8 m	MEIA	Montsec, Spain	60	0.2	0	0.0

facility used is shown in Table 1, as well as the number of catalogues that were specifically used in this paper (about 9000).

We obtained reliable absolutely calibrated magnitude measurements for 228 candidate SPSS in the Johnson–Kron–Cousins *BVR* bands and in some cases in the *I* band as well. The data used here were gathered in 95 observing nights under clear sky conditions. Of these, three nights did not have Landolt fields observations of sufficient quality to determine a reliable night solution, 38 were judged non-photometric, 22 were reasonably good, and 32 were judged photometric (see Section 3.3 for more details). We observed $\simeq 88$ per cent of the SPSS candidates at least once under photometric conditions while $\simeq 9$ per cent were observed under good but not fully photometric conditions. Six additional stars observed only in non-photometric conditions are not considered here. The relative photometry data taken for time-series monitoring of the SPSS constancy were presented by Marinoni et al. (2016) and will not be discussed here.

The lists of candidate SPSS and rejected candidates presented here (see Tables 4, 5) does not correspond entirely to those by Pancino et al. (2012). On the one hand, a few more candidate SPSS were rejected since 2012 because of variability, either detected by Marinoni et al. (2016) or by other literature sources, or because of other problems such as close companions, problems during observations, and so on (see notes to Table 5). In particular, 14 candidate SPSS originally included in Pancino et al. (2012) were rejected, while two new candidates were observed after 2012 and included only here. On the other hand, not all good SPSS candidates⁸ were observed under photometric conditions, and thus some do not appear in this paper. In particular, we present here absolute photometry for 228 SPSS candidates, of which 30 are now rejected and presented separately.⁹ Finally, for two good SPSS candidates, SPSS 159 (WD 0050-332) and SPSS 219 (WD 0106-358), we could not obtain reliable absolute photometry, unfortunately.

2.2 Data reduction and aperture photometry

To allow for the most homogeneous and accurate reduction possible, a specific characterization of all the instruments used was initially carried out (Altavilla et al. 2015), including a detailed study of the stability of the calibration frames (i.e. master bias, dark, master flat,

and bad pixel mask). The imaging frames used here were thus pre-reduced, by removing instrument signatures, following the procedure described in detail by Marinoni et al. (2012, 2016). Briefly, the procedure includes the standard bias (and overscan, when available) subtraction and flat-field normalization. Dark current correction was not needed for the six facilities used for absolute photometry. Bad pixels were flagged and used in an accurate quality control procedure (hereafter QC, see also Marinoni et al. 2014, for details) of the master frames considering saturation, signal-to-noise ratio (SNR), defects, etc. Our procedures were mostly based on IRAF¹⁰ (Tody 1986, 1993), but also on in-house scripts.

Once the data were corrected for instrumental signatures, we proceeded to measure aperture photometry on all imaging frames taken on nights where also standard stars from the Landolt (1992a) catalogues were observed. We used SEXTRACTOR (Bertin & Arnouts 1996) to sum up the flux contained in large apertures, chosen as six times the full-width at half-maximum (FWHM) of the stellar profiles, to minimize flux losses. The same criterion was applied to SPSS and Landolt calibration observations. The procedure is described in detail in Marinoni et al. (2014). We profited, among other things, from the variety of output flags from SEXTRACTOR to perform additional QC checks as detailed by Marinoni et al. (2014), related to both the frame and the stars, concerning saturation, SNR, seeing and focus, bad pixels, the number of good Landolt stars in standard frames, and so on.

The resulting photometric catalogues, one for each frame, contain instrumental magnitudes for each relevant star in each frame, either Landolt standards or SPSS candidates, depending on the type of observation. The instrumental magnitudes are defined as

$$m = -2.5 \log_{10} DN_{\text{star}}, \quad (1)$$

where m is the instrumental magnitude (in our case b , v , r , or i) and DN_{star} is the signal of the star, here represented by the total CCD counts measured inside the aperture after subtracting the sky background.

3 PHOTOMETRIC CALIBRATION

To transform the instrumental aperture magnitudes to the Landolt system, we used a standard procedure (see e.g. Stetson et al. 2019): we first computed the night solutions using observations of Landolt standard fields and then applied the solutions to the

⁸At this point, we consider as good SPSS candidates those matching the initial criteria defined by Pancino et al. (2012), that were not rejected so far based on new information, and that have good spectroscopic observations.

⁹One of the good SPSS candidates, SPSS 355 or SDSS J125716+220059, has good photometry, but no spectroscopic observations, so it is unlikely to be included in the final *Gaia* SPSS grid.

¹⁰IRAF was distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

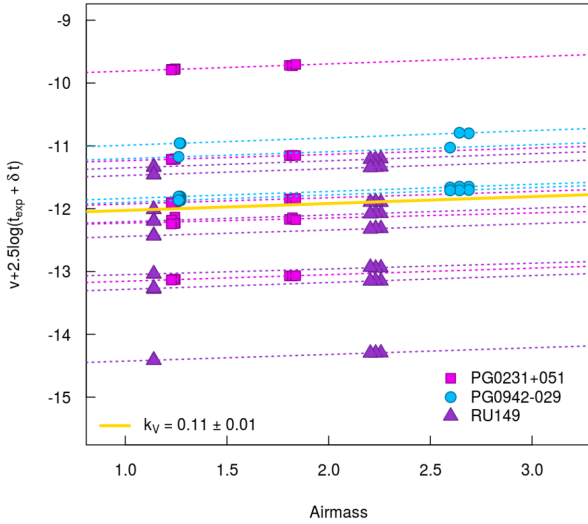


Figure 1. Example of determination of the extinction coefficient k_v in the V band, for the night of 2008 November 26, at the ESO NTT telescope. Dotted lines – for each star in a given Landolt field – are linear fits of the stars’s instrumental v magnitude corrected for exposure time, as a function of effective airmass. Each slope represents an estimate of k_v : their median and semi-interquartile range provide a robust estimate of k_v for the night (yellow thick line).

SPSS instrumental magnitudes to obtain the absolutely calibrated magnitudes. Before computing the absolutely calibrated magnitudes, however, we performed a detailed assessment of the night quality, as described in the following sections.

3.1 Extinction coefficients

The actual calibration process was split into two separate steps. In the first step, we took into account the atmospheric and exposure-time effects using the following equation

$$m' = m + 2.5 \log_{10}(t_{\text{exp}} + \delta t) - k_M X, \quad (2)$$

where m' is the corrected instrumental magnitude (in our case b' , v' , r' , or i'), t_{exp} is the exposure time, δt is the shutter effect, necessary to obtain the effective exposure time (determined as in Altavilla et al. 2011, 2015), k_M is the extinction coefficient in the M band (in our case k_B , k_V , k_R , or k_I), and X is the effective airmass.¹¹ To compute the atmospheric extinction coefficient for each band and each observing night, we used repeated observations of the same stars in a few Landolt standard fields, observed at different X , to compute i independent estimates of the extinction coefficient, k_{M_i} , as exemplified in Fig. 1. We then used their median as a robust estimate of k_M for the night in each band, and their interquartile range as the related uncertainty δk_M . To be noted that standard star fields were occasionally observed also at large zenith distances to probe the atmospheric absorption in a wide airmass range whereas scientific targets were observed preferably as high as possible above the horizon to ensure high quality measurements. Having several nights at different observing sites, we could compare our typical extinction

coefficients with literature estimates for each observing site. To compute typical coefficients, we used the average of 2–25 nights, depending on the site, as detailed in Table 2. Unfortunately, our data are not sufficient to properly sample seasonal variations, which might be relevant and characterized by lower values in winter (Metlov 2004; Sánchez et al. 2007). For Calar Alto, we used extinction data by Sánchez et al. (2007), who also provided uncertainties; for La Palma, we found useful data, valid only for very clear nights, without aerosols, in the RGO/La Palma technical note n. 31, and detailed in the William Herschel Telescope website¹²; for typical nights the values could be increased by $0.05 \text{ mag airmass}^{-1}$; for La Silla we used values from the ESO 1993 user manual¹³; for San Pedro Mártir we used the values by Schuster & Parrao (2001). The results of the comparison are summarized in Fig. 2, displaying excellent agreement. To be consistent with literature data, in Figs 2 and 5 we computed k_B as described above, neglecting colour dependencies, but for the actual calibration of the B -band magnitudes we expanded equation (2) to account for secondary extinction correction effects:

$$m' = m + 2.5 \log_{10}(t_{\text{exp}} + \delta t) - (k'_M + k''_M c) X, \quad (3)$$

where k'_M and k''_M are the primary and secondary extinction coefficients respectively, c is the observed colour index, that we approximated as the difference between b' and v' computed with equation (2) (see also Section 3.2). The second-order extinction coefficients can be determined applying equation (3) to a pair of stars with extreme colours observed in the same field and spanning a wide airmass range, e.g. the reddest and the bluest stars in a standard star field repeatedly observed during the night. Once k'_B is known, we can apply equation (3) again, this time to stars spanning a wide airmass range, regardless of their colour, e.g. stars in a standard star field repeatedly observed during the night, to determine k''_B , as exemplified by Buchheim (2005). Due to the difficulties in measuring k''_B , we used the mean value obtained over several nights, while for k'_B we used the values obtained night by night. The average values of k'_B and k''_B for each telescope¹⁴ are shown in Table 3. It is to be noted that the k'_B values corresponding to k''_B are not the k_B values reported in Table 2 (in fact the slope mentioned in Fig. 1 corresponds to the term $k'_M + k''_M c$ in equation 3). According to our data, the k'_B values are roughly $\sim 0.03 \text{ mag airmass}^{-1}$ larger, on average, than k_B .¹⁵ The B -band second-order extinction term makes blue stars dim faster than red stars as they approach the horizon. However, the secondary extinction coefficients in VRI are smaller than in B and smaller than the uncertainties, so we neglected them as normally done (Sung et al. 2013).

3.2 Zero-points and colour terms

Once the instrumental magnitude was corrected for exposure time and extinction, the photometric solution for the night could be computed with the equation

$$M = m' + f_M c + Z P_M, \quad (4)$$

where M is the calibrated magnitude (in our case B , V , R , or I); f_M is the colour-term of the calibration equation; c is a colour

¹¹The effective airmass is computed with the IRAF task *setairmass* according to the formula described in Stetson (1989) to approximate the mean airmass $\bar{X}$ of long exposures better than the mid-observation value $X_{1/2}$: $\bar{X} = (X_0 + 4X_{1/2} + X_1)/6$, where X_0 and X_1 are the airmasses at the beginning and at the end of the exposure, respectively.

¹²http://www.ing.iac.es/astronomy/observing/manuals/html_manuals/wht_instr/pfip/prime3_www.html

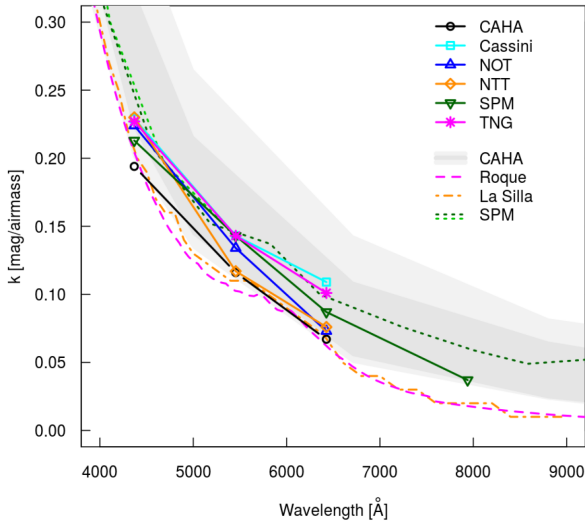
¹³<https://www.eso.org/sci/observing/tools/Extinction.html>

¹⁴The SPM 1.5 m adopted different CCDs along the observing campaign but the secondary extinction coefficients computed for each CCD are all consistent within the uncertainties, hence we used a single value.

¹⁵The large k'_B value measured in Loiano is based on a single, possibly problematic, night.

Table 2. Atmospheric extinction coefficients obtained in our photometry campaign. The number of nights used for the statistics is also indicated.

Site	Telescope	# nights	k_B (mag airmass ⁻¹)	δk_B	k_V (mag airmass ⁻¹)	δk_V	k_R (mag airmass ⁻¹)	δk_R	k_I (mag airmass ⁻¹)	δk_I
Calar Alto	CAHA 2.2 m	3	0.194	0.023	0.116	0.017	0.067	0.032	–	–
Loiano	Cassini 1.5 m	2	0.229	0.014	0.143	0.006	0.109	0.006	–	–
Roque	NOT 2.6 m	2	0.224	0.021	0.134	0.013	0.073	0.026	–	–
La Silla	NTT 3.6 m	10	0.230	0.015	0.117	0.013	0.076	0.009	–	–
San Pedro Mártir	SPM 1.5 m	25	0.213	0.021	0.133	0.043	0.087	0.034	0.037	0.003
Roque	TNG 3.6 m	12	0.227	0.034	0.143	0.024	0.101	0.016	–	–

**Figure 2.** Extinction coefficients k_M plotted as a function of the effective wavelengths of the *BVRI* passbands by Bessell & Murphy (2012), measured at the six observing sites, as detailed in the upper legend. Literature data are also shown for comparison (see Section 3.1 for references), as detailed in the lower legend.

built using the observed instrumental magnitude m' and a nearby passband (e.g. $b' - v'$ for the *V*-band calibration)¹⁶ that takes into account the dependence of the solution on the spectral energy distribution of the considered star; and ZP_M is the absolute zero-point of the solution. Slight deviations between the standard stars' photometric system and the photometric system actually adopted in the observations, that depends on the passbands and on the overall optical throughput of the telescope and the camera, are expected, as extensively discussed in Sections 4.1 and 4.2. Such differences are tracked and corrected through observations of several standard stars, spanning a wide range of colours. If the standard stars' photometric system and the photometric system actually adopted in the observations perfectly match, f_M should be ideally equal to zero. Nevertheless slight deviations between the two systems, that depend on the passbands and on the overall optical throughput of the telescope and the camera actually used, are expected, as extensively discussed in Sections 4.1 and 4.2. In this case the colour-term can be computed through observations of several standard stars, spanning a wide range of colours.

¹⁶We use a first-order polynomial approximation of the actual spectral energy distribution in terms of the star's colour, because a few experiments showed that it was not necessary to include a second-order term.

Some authors write equation (4) using the standard tabulated colour C (in our case, from Landolt 1992a) instead of the instrumental colour c (e.g. $B - V$ instead of $b' - v'$). The problem of the choice of the independent variable in equation (4) was discussed at length by Harris, Fitzgerald & Reed (1981). In practice, to find the solution an ordinary least-square algorithm is used, which requires various conditions, including that the independent variables are error-less and the dependent ones are homoscedastic. These conditions are never fully satisfied, but are less violated by the Landolt tabulated magnitudes than by the observed ones. However, Isobe et al. (1990) suggest that the reason to adopt tabulated magnitudes as the independent variables is not so compelling, and the use of the instrumental magnitudes as the independent variable can also be a viable method as far as the errors on instrumental magnitudes are comparable to the errors on the tabulated absolutely calibrated magnitudes. The typical uncertainties on our instrumental magnitudes are about 1–2 per cent, fully compatible with the Landolt ones (see Section 4.1). Therefore, we used the observed instrumental magnitudes in equation (4) as independent variables.

In practice, we proceeded as follows: (i) we used equation (4) separately on each Landolt field observed during the night; (ii) we obtained f_M and ZP_M for each photometric band using ordinary least squares; (iii) we verified that the solutions for each field in the same night are compatible with each other (see Fig. 3), otherwise it might mean that the sky conditions have changed or that the discrepant fields have problems; (iv) we averaged the f_M and ZP_M obtained for each band and used the root mean square deviation to represent the uncertainties δf_M and δZP_M .

To illustrate the quality of the results, we show in Fig. 4 the trends of the ZP_M and f_M in the four available bands for our observing nights at San Pedro Mártir. During the years, the instrument was refurbished four times, with a change of detector, and this has caused visible jumps in the typical values in each band. Moreover, random variations due to variable sky conditions are well visible. Fig. 5 similarly shows the behaviour of ZP_M for our observing runs at the ESO NTT in La Silla. In this case, we could also compare our results with the ones in the ESO Archive.¹⁷ Small difference in the comparison could be caused by different imaging mode (different gain) and other minor effects. In any case, the agreement between our ZP_M data for NTT and the ESO ones is excellent.

3.3 Night quality control

To evaluate whether a given observing night was useful for our purpose, we performed a dedicated quality assessment. A detailed

¹⁷http://www.la.eso.org/sci/facilities/lasilla/instruments/efosc/archive/efosc_czp.dat

Table 3. *B*-band primary and secondary extinction coefficients obtained in our photometry campaign. The number of nights used for the statistics is also indicated.

Site	Telescope	# nights k'_B	k'_B (mag airmass ⁻¹)	$\delta k'_B$	# nights k''_B	k''_B (mag airmass ⁻¹)	$\delta k''_B$
Calar Alto	CAHA 2.2 m	5	0.26	0.05	5	− 0.03	0.03
Loiano	Cassini 1.5 m	1	0.41	0.01	1	− 0.01	0.02
Roque	NOT 2.6 m	2	0.26	0.02	2	− 0.04	0.01
La Silla	NTT 3.6 m	11	0.25	0.02	11	− 0.03	0.02
San Pedro Mártir	SPM 1.5 m	25	0.24	0.02	24	− 0.03	0.02
Roque	TNG 3.6 m	12	0.24	0.04	8	− 0.03	0.02

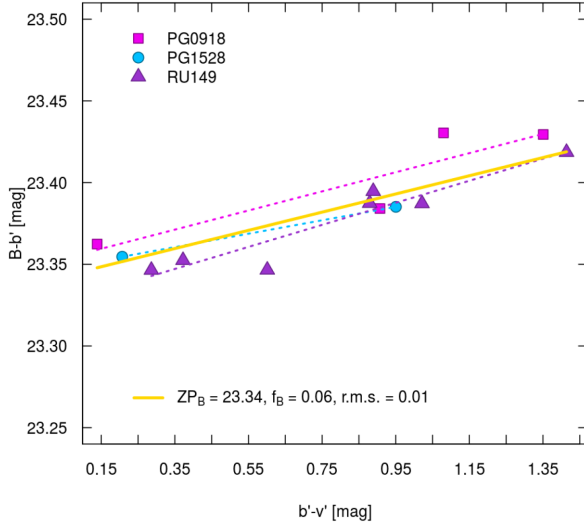


Figure 3. Example of the computation of the colour term f_B and zero-point ZP_B for the San Pedro Mártir observations of 2009 January 28. Each of the three Landolt fields observations are represented as filled symbols of a different colour. The comparison of linear fits for each field separately (coloured dotted lines) allows us to verify that they provide compatible estimates. The global f_B and Z_B for the night are indicated at the bottom of the plot, and represented by a solid line.

description of the adopted procedures can be found in Altavilla et al. (2020); here below we provide a brief summary.

A complete data set for the determination of k_M consists of at least three different Landolt standard fields observed in each of three bands (either *BVR* or *VRI* in our case), with an airmass difference of $\Delta X \geq 0.2$. A data set cannot be useful when two out of three bands do not have useful data, i.e. when k_M is only available for one band. All other cases were considered intermediate: the data are not optimal, but still could be useful. Whenever k_M could be computed for at least two bands, we used its uncertainty to decide whether its determination was good ($\delta k_M \leq 0.03$ mag airmass⁻¹ in all bands), bad ($\delta k_M \geq 0.06$ mag airmass⁻¹ in all bands) or intermediate (all other cases).

A similar approach was followed to assess whether the available data sets were adequate to compute reliable ZP_M and to assess their quality. Here, instead of ΔX we used the time coverage Δt of the standard fields during the night and the colour coverage ΔC of the observed standard stars. The data were considered adequate if $\Delta C \geq 1$ mag and $\Delta t \geq 4$ h. Then, we used the uncertainties on ZP_M to decide upon their quality: if $\delta ZP_M \leq 0.25$ mag in all bands, the data were considered good, if $\delta ZP_M \leq 0.25$ mag for one band only or less, the data were considered bad, and

in all remaining cases the data were considered of intermediate quality.

At that point, we judged a night as photometric if the Landolt data were adequate to compute k_M and ZP_M and if the quality of their determination was good. The night was judged not useful if the data are not adequate to calibrate it (unknown quality) or if they were adequate but provided bad k_M or ZP_M estimates for at least two bands (not photometric). In all other cases the night was judged as relatively good, i.e. still useful to compute absolutely calibrated magnitudes, but to be used with extra care.

3.4 Final absolutely calibrated magnitudes

Once the coefficients k_M , f_M , and ZP_M of equations (2), (3), and (4) were determined using Landolt fields observations, the same equations could be used to obtain M from m and the known coefficients, at least for the nights that passed the QC. For each frame catalogue of aperture magnitudes that passed the QC procedures, we thus obtained absolutely calibrated magnitudes, with their own propagated uncertainties and quality flags (in case the QC was only partially passed).

We then computed the weighted mean and the corresponding weighted standard deviation of the epoch calibrated magnitudes to obtain the final calibrated *BVR(I)* magnitudes for each SPSS. An example of the type of data sets in hand is presented in Fig. 6. In order to reject a handful of very obvious extreme outliers from the weighted mean computation, we first used all data available in a given band for a given SPSS to compute an initial weighted mean, then we rejected all points deviating more than 0.5 mag if $\sigma < 0.5$ mag, or all points deviating more than 1 σ if $\sigma > 0.5$ mag, and finally we re-computed the final weighted mean with the surviving points. The above thresholds were chosen after experimenting with the data, with the goal of removing only measurements that are clearly very different from the remaining ones.

We also noted that when data for a certain SPSS came from a single night, the uncertainty resulting from the weighted average was unrealistically small, because all measurements were very similar to each other. This was not the case when really independent measurements were available, from different observing nights and different facilities. For this reason, when only one observing night was available, we also computed the median of the errors of the individual measurements. The final error for these cases was chosen as the largest between this and the error on the weighted mean.

4 RESULTS AND VALIDATION

The final calibrated magnitudes for the 198 good SPSS candidates are listed in Table 4, which is available electronically. The magnitude

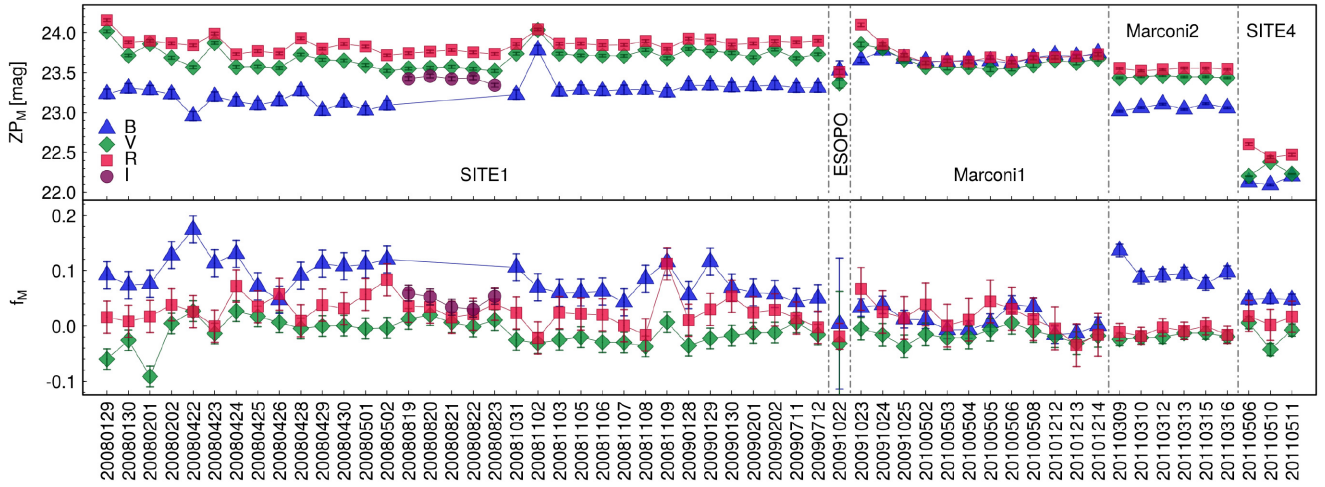


Figure 4. Temporal evolution of the zero points ZP_M and colour terms f_M (equation 4) as measured with the 1.5 m telescope at the San Pedro Mártir Observatory from 2008 January to 2011 May. The names of the five CCDs mounted at the La Roca imager during this period are shown.

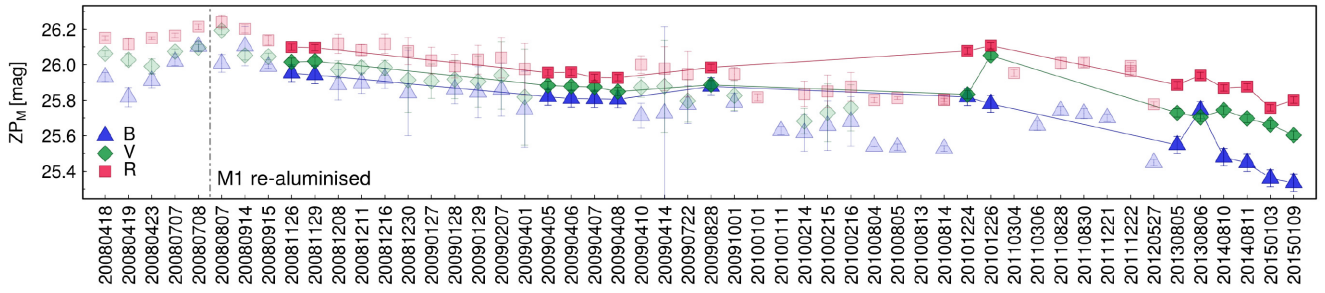


Figure 5. Temporal evolution of the zero points ZP_M as measured with the NTT telescope at the ESO La Silla Observatory from 2008 November to 2015 January. Light coloured symbols represent archival ESO data (see the text for details), while full coloured symbols show our measurements.

measurements for 30 SPSS that were rejected or do not have spectra of sufficient quality (see Section 2) are presented separately, in Table 5, along with the motivation for the rejection. The distributions of the entire sample in magnitude and colour are presented in Fig. 7, where the large colour baseline and magnitude range can be fully appreciated. In the following, we compare our measurements with various literature sources, most notably the collection of photoelectric and CCD photometry by Landolt (Section 4.1) and the spectra of the CALSPEC collection (Section 4.2), finding a good agreement within the uncertainties, i.e. of the order of 1 per cent.

4.1 Comparison with Landolt photometry

While our data are calibrated on the original set of photometric standard stars defined by Landolt (1992a), there are several papers by the same author and collaborators, providing photoelectric and CCD magnitudes reported as accurately as possible on the original photoelectric system by Landolt (1992a). The collection is useful to validate our work, thus we selected measurements from Landolt (1973, 1983, 1992a, b), Landolt & Uomoto (2007), Landolt (2007, 2009, 2013), and Bohlin & Landolt (2015). Small inconsistencies and non-linear relations between different instruments and especially between photoelectric and CCD magnitudes were corrected by the listed authors with a series of ad hoc transformations and piecewise polynomials, depending on the data set (see e.g. Landolt 2007). The internal consistency of the entire set of magnitudes was estimated to be of the order of 1 per cent. We merged the data by keeping the

most recent measurement available for each star, and created a unique catalogue with $\simeq 1650$ stars, that we will refer to in the following as ‘Landolt collection’.

We excluded from any comparison the rejected candidate SPSS (see Table 5); the final sample of SPSS in common with the Landolt collection contains 51 stars (the stars used are labelled in Table 4). The results of the comparison are shown in Fig. 8, in the top sub-panels of each of the *B*, *V*, *R*, and *I* panels. As it can be seen, while the mean offsets are generally smaller than the uncertainties, there are offsets of about 1 per cent between our SPSS magnitudes and the ones in the Landolt collection. The offset is consistently positive, i.e. our magnitudes are consistently fainter than the ones in the Landolt collection, but it varies a lot from one band to the other. For example, the *I* band has a 0.001 offset while the *V* band has an offset of 0.019 mag. Although contained within uncertainties, these offsets are non-negligible compared to our original requirement on the SPSS flux tables (spectra calibrated to 1–3 per cent) for the external flux calibration of *Gaia* data.

We thus considered another useful photometric data set, published by Clem & Landolt (2013, 2016), to look further into this matter. The full data set, that we will refer to as ‘Clem collection’, contains a much larger number of sources than the Landolt collection, but only 10 sources in common with our SPSS set. Their magnitudes were calibrated as accurately as possible on to the Landolt (1992a) set and on the full Landolt collection, using ad hoc techniques similar to the ones used in the Landolt collection. As shown by Landolt (2007) before, the basic problem is that the diversity of detectors and

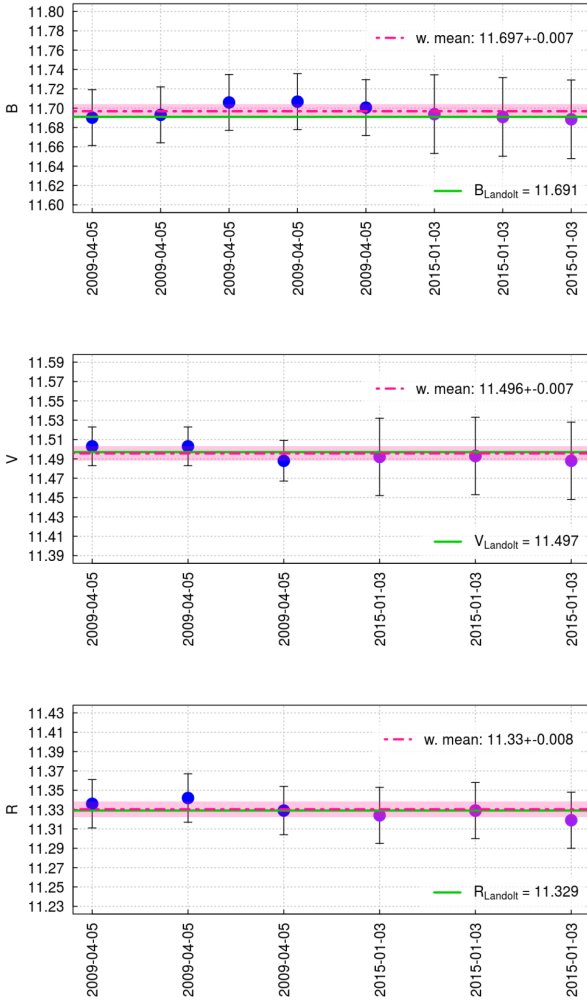


Figure 6. Example of checkplots for the computation of the combined calibrated magnitude of SPSS 012 (LTT 4364). Each panel shows the magnitude measured in a given band, as indicated, versus the corresponding date. Each observation is plotted as a blue circle in case of photometric nights (Section 3.3) or a purple one in case of intermediate quality nights. The weighted average is reported as a red line with a shaded strip representing the error, while the Landolt magnitude (Section 4) as a green line.

filters employed in the various studies implies a certain minimum degree of uncertainty (see Clem & Landolt 2013, for an in-depth discussion), that can be quantified as being of the order of 1 per cent with current technology. The corrections applied by Clem & Landolt (2013, 2016) bring their measurements on to the original Landolt system to about 0.5 per cent on average across the five bands. We show this comparison in the bottom sub-panels of Fig. 8 for each of four bands used in this study. As it can be seen, the Clem collection is also consistently fainter than the Landolt collection, similarly to what happens to the SPSS magnitudes, but with a smaller offset: on average ≈ 0.5 per cent rather than ≈ 1 per cent, depending on the band. As a result, the SPSS magnitudes agree generally slightly better with the Clem collection than with the Landolt one, as shown in the middle sub-panels of Fig. 8. We observe from Fig. 8 that the spread of our measurements is generally comparable to or even smaller than the spreads of the Landolt and Clem samples, perhaps because of the careful exclusion of variable stars with amplitude larger than ± 5 mmag from our sample (Marinoni et al. 2016).

Table 4. Calibrated magnitudes for the 198 good SPSS candidates. The full table is available online and at the CDS.

Column	Units	Description
SPSS ID	–	The internal SPSS ID (001-399)
SPSS name	–	The SPSS adopted name
R.A. (J2000)	hh:mm:ss.ss	Right ascension [†]
Dec (J2000)	dd:mm:ss.s	Declination [†]
B	mag	B calibrated magnitude
V	mag	V calibrated magnitude
R	mag	R calibrated magnitude
I	mag	I calibrated magnitude
δB	mag	Uncertainty on B
δV	mag	Uncertainty on V
δR	mag	Uncertainty on R
δI	mag	Uncertainty on I
N_B	–	Number of nights for B
N_V	–	Number of nights for V
N_R	–	Number of nights for R
N_I	–	Number of nights for I
P_B	–	Number of measurements for B
P_V	–	Number of measurements for V
P_R	–	Number of measurements for R
P_I	–	Number of measurements for I
Flag $_B$	–	1 if no fully photometric nights
Flag $_V$	–	1 if no fully photometric nights
Flag $_R$	–	1 if no fully photometric nights
Flag $_I$	–	1 if no fully photometric nights
Notes	–	Annotations*

Notes. *Pancino et al. (2012) and references therein.

[†]Including the availability of photometry in the Landolt or Clem collections and of CALSPEC flux tables.

4.2 Comparison with CALSPEC spectrophotometry

Another fundamental reference set for flux calibrations is the CALSPEC¹⁸ set of spectrophotometric standards (Bohlin et al. 2014). It currently contains about 95 stars with complete coverage of the *Gaia* wavelength range (and beyond), observed with the *Hubble Space Telescope* (*HST*), and calibrated in flux to an accuracy of about 1 per cent (on the reference system), although recent revisions altered the flux of individual stars by up to 2.5 per cent (Bohlin et al. 2019). All spectra are calibrated on three primary calibrators, the pure hydrogen white dwarfs GD 71, GD 153, and G 191–B2B and on theoretical spectra (Bohlin et al. 2017).

We computed synthetic magnitudes for 24 CALSPEC spectra that correspond to good SPSS candidates. We only considered CALSPEC spectra covering the entire *Gaia* wavelength range, and we did not include rejected SPSS (Table 5) in the comparison (the stars used are labelled in Table 4). We selected the latest and most complete spectra in the CALSPEC data base at the time of writing plus the model spectra for the three CALSPEC primary calibrators (Bohlin, Hubeny & Rauch 2020). We used the passbands by Bessell & Murphy (2012) and as reference spectrum the same high-fidelity Kurucz model of Vega used by CALSPEC (alpha_lyr_mod_004) and Vega magnitudes given by Casagrande & VandenBerg (2014) and references therein. We then compared the synthetic CALSPEC magnitudes with our measurements, as illustrated in Fig. 9. Our measurements agree with the synthetic photometry obtained from the CALSPEC spectra within 1–2 per cent. In the B band, a colour dependence is apparent, in the

¹⁸<https://www.stsci.edu/hst/instrumentation/reference-data-for-calibration-and-tools/astronomical-catalogs/calspec>

Table 5. Calibrated magnitudes (M) and uncertainties (δM) of rejected SPSS candidates, with motivation of the rejection.

SPSS ID	SPSS name	RA (J2000) (hh:mm:ss)	Dec (J2000) (dd:mm:ss)	B (mag)	V (mag)	R (mag)	I (mag)	δB (mag)	δV (mag)	δR (mag)	δI (mag)	Notes
018	BD +284211	21:51:11.02*	+28:51:50.4*	10.202	10.539	10.695	10.893	0.022	0.025	0.013	0.023	‡,§,1
020	BD +174708	22:11:31.37*	+18:05:34.2*	9.895	9.474	9.164	8.853	0.012	0.009	0.031	0.024	‡,§,2
029	SA 105-448	13:37:47.07*	−00:37:33.0*	9.386	9.149	8.998	—	0.033	0.035	0.022	—	‡,3
034	1740346	17:40:34.68*	+65:27:14.8*	12.745	12.578	12.473	—	0.024	0.016	0.012	—	3,§
051	HD 37725	05:41:54.37*	+29:17:50.9*	8.501	8.328	8.340	—	0.021	0.011	0.125	—	3,§
131	WD 1327-083	13:30:13.64*	−08:34:29.5*	12.395	12.335	12.414	—	0.017	0.019	0.021	—	1
150	WD 2126+734	21:26:57.70†	+73:38:44.4†	12.888	12.863	12.910	—	0.026	0.017	0.024	—	4
152	G 190-15	23:13:38.82*	+39:25:02.6*	11.685	11.051	10.606	10.192	0.018	0.046	0.038	0.046	5
160	WD0104-331	01:06:46.86*	−32:53:12.4*	18.232	17.051	16.292	—	0.030	0.031	0.034	—	6
190	G 66-59	15:03:49.01†	+10:44:23.3†	13.867	13.167	12.763	—	0.042	0.046	0.036	—	7
212	WD 2256+313	22:58:39.44*	+31:34:48.9*	—	13.988	—	11.803	—	0.054	—	0.071	8
216	WD 0009+501	00:12:14.80*	+50:25:21.4*	14.812	14.373	14.090	13.785	0.004	0.011	0.014	0.044	1
227	WD 0406+592	04:10:51.70*	+59:25:05.0*	14.511	14.716	14.809	—	0.025	0.009	0.025	—	9
232	LP 845-9	09:00:57.23†	−22:13:50.5†	16.196	14.623	—	—	0.038	0.046	—	—	8
240	WD 1121+508	11:24:31.41†	+50:33:31.6†	15.601	14.910	14.516	—	0.031	0.040	0.019	—	8
243	WD 1232+479	12:34:56.20†	+47:37:33.4†	14.832	15.325	14.556	—	0.472	0.293	0.028	—	10
265	WD 2010+310	20:12:22.28†	+31:13:48.6†	—	14.833	14.821	15.015	—	0.031	0.022	0.040	8
286	WD 0205-304	02:07:40.71†	−30:10:57.6†	15.732	15.750	15.826	—	0.024	0.019	0.017	—	8
290	WD 1230+417	12:32:26.18†	+41:29:19.2†	15.644	15.726	15.818	—	0.024	0.028	0.014	—	8
293	WD 1616-591	16:20:34.75†	−59:16:14.2†	15.105	14.998	15.034	—	0.023	0.006	0.004	—	11
294	WD 1636+160	16:38:40.40†	+15:54:17.0†	15.744	15.652	15.700	—	0.028	0.032	0.015	—	8
297	PG 0924+565	09:28:30.52†	+56:18:11.6†	16.540	16.464	16.079	—	0.189	0.252	0.017	—	8
316	SDSS13028	16:40:24.18*	+24:02:14.9*	15.510	15.275	15.120	—	0.015	0.012	0.019	—	3
317	SDSS15724	20:47:38.19*	−06:32:13.1*	15.354	15.125	14.946	—	0.292	0.207	0.168	—	12
318	SDSS14276	22:42:04.17*	+13:20:28.6*	14.515	14.313	14.204	—	0.051	0.052	0.041	—	3
322	SDSS12720	12:22:41.66*	+42:24:43.7*	15.526	15.372	15.136	—	0.252	0.175	0.154	—	3
325	SDSS03932	00:07:52.22*	+14:30:24.7*	15.401	15.086	14.880	—	0.018	0.021	0.020	—	3
329	GJ 207.1	05:33:44.81†	+01:56:43.4†	13.066	11.523	10.447	—	0.020	0.024	0.024	—	13
330	GJ 268.3	07:16:19.77†	+27:08:33.1†	12.403	10.875	9.810	—	0.005	0.004	0.009	—	14
350	LTT377	00:41:30.47*	−33:37:32.0*	12.000	10.565	9.640	—	0.010	0.009	0.027	—	15

Note. *Pancino et al. (2012) and references therein; †2MASS All-Sky Catalogue of Point Sources (Cutri et al. 2003; Skrutskie et al. 2006); ‡Literature data from Landolt available (see Section 4); § CALSPEC spectrum available (see Section 4); 1 - suspected variable (Marinoni et al. 2016); 2 - long-term variability (Bohlin & Landolt 2015; Marinoni et al. 2016); 3 - variable (Marinoni et al. 2016); 4 - binary star (Farihi, Becklin & Zuckerman 2005); 5 - suspected long term variable (Marinoni et al. 2016); 6 - discordant coordinates in Wegner 1973 and Chavira 1958; 7 - double-lined spectroscopic binary (Latham et al. 1992); 8 - too faint; 9 - close red companions; 10 - radial velocity variable (Saffer, Livio & Yungelson 1998); 11 - high PM star, now too close to another faint star; 12 - variable star (Abbas et al. 2014); 13 - Wachmann variable, flare Star (Luyten & Hoffleit 1954); 14 - spectroscopic binary (Jenkins et al. 2009); 15 - suspected variable (Samus' et al. 2017; Jayasinghe et al. 2019).

form of a curved trend with a maximum difference around $B - V = 0.0$ – 0.3 mag. A similar but less pronounced trend can be observed for the V and R bands, while the I band data are too sparse to draw any conclusion. These trends were not present in the comparisons with the Landolt and Clem collections, but they were observed by Bohlin & Landolt (2015) in their comparison of CALSPEC synthetic photometry with Landolt photometry. They mitigated the trend by applying small wavelength shifts to the Bessell & Murphy (2012) passbands used to obtain their CALSPEC photometry, which are the same that we used. A similar procedure was applied by Stritzinger et al. (2005) to remove similar colour trends in the comparison between their synthetic magnitudes and literature data. Along those lines, Bessell (1990) suggested that ‘optimum passbands’ may be recovered by minimizing the differences between synthetic and standard magnitudes. It is extremely interesting that Clem & Landolt (2013, 2016) also found similar colour trends in their comparison with the original Landolt collection, that they corrected with empirical methods, as described in the previous section.

To test the idea, we repeated the comparison, this time applying the same wavelength shifts employed by Bohlin & Landolt (2015) to the Bessell & Murphy (2012) passbands. The applied shifts were -20 Å for the B and the V bands, -31 Å for the R band, and -27 Å

for the I band. The results are shown in Fig. 10. As it can be observed, the residuals becomes flatter in the colour range $-0.4 \lesssim B - V \lesssim 0.6$, i.e. the one covered by Bohlin & Landolt (2015), but the comparison gets significantly worse for redder objects. The worsening of the comparison for red sources is confirmed by the V and R bands results. For this reason, we think that a wavelength shift of the passbands is not sufficient to fully repair the discrepancy. The results in Figs 9 and 10 do not change significantly using as reference spectrum for the synthetic photometry the one chosen for the *Gaia* photometric system (Carrasco et al. 2016), i.e. a Kurucz/ATLAS9 model (Buser & Kurucz 1992) for the Vega spectrum (CDROM 19) with $T_{\text{eff}} = 9400$ K, $\log g = 3.95$ dex, $[M/H] = -0.5$ dex, and $v_{\text{micro}} = 2$ km s $^{-1}$, scaled to fit STIS data (over the interval 5545–5570 Å) (Bohlin & Gilliland 2004).

As extensively discussed in the cited literature and in the previous section, the original Landolt system was defined using a 1P21 photomultiplier (Landolt 1973), while the following literature used a variety of systems, including different photomultipliers, CCD cameras, optical filters, telescopes, and detectors. The original Landolt system provided a standard system that is used to calibrate the vast majority of Johnson–Kron–Cousins observations, but modern CCD detectors and manufactured filters provide slightly different

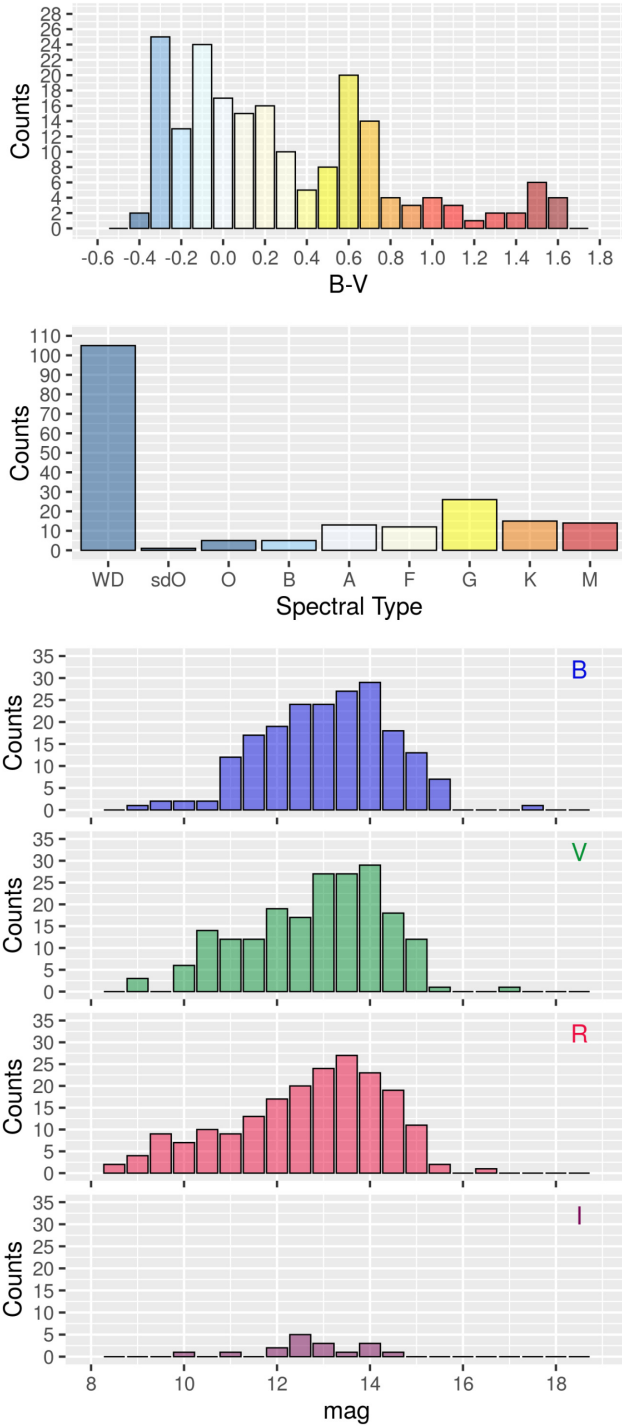


Figure 7. Distribution of the SPSS candidates as a function of colour and spectral type (multicoloured histograms, top panels) and of the *BVR* magnitudes (single-colour histograms, remaining panels).

responses. To adhere as much as possible to the Landolt original system, authors in the cited literature applied empirical, ad hoc non-linear corrections to their measurements. By accurately calibrating our observed magnitudes on the original Landolt (1992a) system, we observe no significant trend between our SPSS results and the Landolt or Clem magnitude collections. However, the CALSPEC spectra were calibrated in a completely independent way, without applying any particular empirical re-calibration on the Landolt original

reference system. This type of discrepancy between contemporary equipment and the original Landolt one cannot be repaired by a simple wavelength shift in the passbands, at least when the colour range covered is as large as the one of the *Gaia* SPSS candidates presented here. It would be necessary to re-compute the photometric passbands so that their shape adequately takes into account the typical deviation of modern CCDs and filter systems from the Landolt one. Among the passbands provided in the literature, we found that the Bessell & Murphy (2012) ones provide the best results, but they are apparently still not sufficiently accurate for some equipment.

In conclusion, the trends observed between the SPSS and the synthetic magnitudes obtained from CALSPEC spectra were observed in several previous studies. They are not caused by specific problems in the SPSS presented here, but by differences in the CALSPEC equipment with respect to the original Landolt equipment, that have not been explicitly corrected for, unlike in photometric studies. Apart from the trends, the 1–2 per cent offset we found with respect to the CALSPEC synthetic magnitudes is similar in amplitude to the one observed with the Landolt collection, which in turn is larger than the one observed with the Clem collection. The offset goes in the same direction in all comparisons, suggesting that the SPSS absolutely calibrated magnitudes presented here, while statistically compatible with the literature measurements, are systematically overestimated by a small quantity that varies in the range 1.0 ± 0.5 per cent, depending on the comparison sample and on the passband.

5 DISCUSSION AND CONCLUSIONS

We have presented accurately calibrated magnitudes for 228 stars, 198 SPSS candidates, and 30 rejected SPSS candidates. Photometry will be used to validate the SPSS spectrophotometry, especially for those SPSS observed in non-optimal conditions. Comparison with literature photometry and spectrophotometry suggests that our magnitudes are systematically overestimated by a small quantity that varies in the range 1.0 ± 0.5 per cent. The systematic offset is within statistical uncertainties and, what is most important, is comparable to the current, state-of-the-art accuracy as estimated by extensive comparisons among the Landolt, Clem, and CALSPEC collections. However, in the case of space missions like *Gaia*, the actual internal uncertainties on the integrated photometry are much smaller than the external uncertainty that is achievable using existing systems of standard stars. The internal uncertainties of *Gaia* are estimated to be well below the millimagnitude level in the $6 < G < 16$ range and ~ 10 millimag at the bright ($G \simeq 3$) and faint ($G \simeq 20$) ends (Evans et al. 2018). So the question is: how can we move towards such small uncertainties in the external calibration of *Gaia* data as well?

Indeed, with current detectors, it is feasible to obtain at least 1 per cent precision in the determination of the physical energy distribution of stars, as well as better than 1 per cent precision in laboratory reference standard flux measurements (Brown, Eppeldauer & Lykke 2006). Nevertheless, the direct comparison between laboratory irradiance standard sources (usually blackbodies and tungsten lamps of known flux) and standard stars fluxes has not been equally developed. The early works by Oke & Schild (1970) and Hayes (1970) and their subsequent revisions and improvements (Hayes, Latham & Hayes 1975; Tüg, White & Lockwood 1977; Hayes 1985; Megessier 1995 and references therein) on measuring the absolute flux of the primary ground-based standard star Vega with respect to terrestrial standard sources, represent the pillars of this effort. A proper comparison requires the standard source to be far enough from a ground based telescope in order to simulate a stellar point source with a collimated beam. These measurements are complicated by

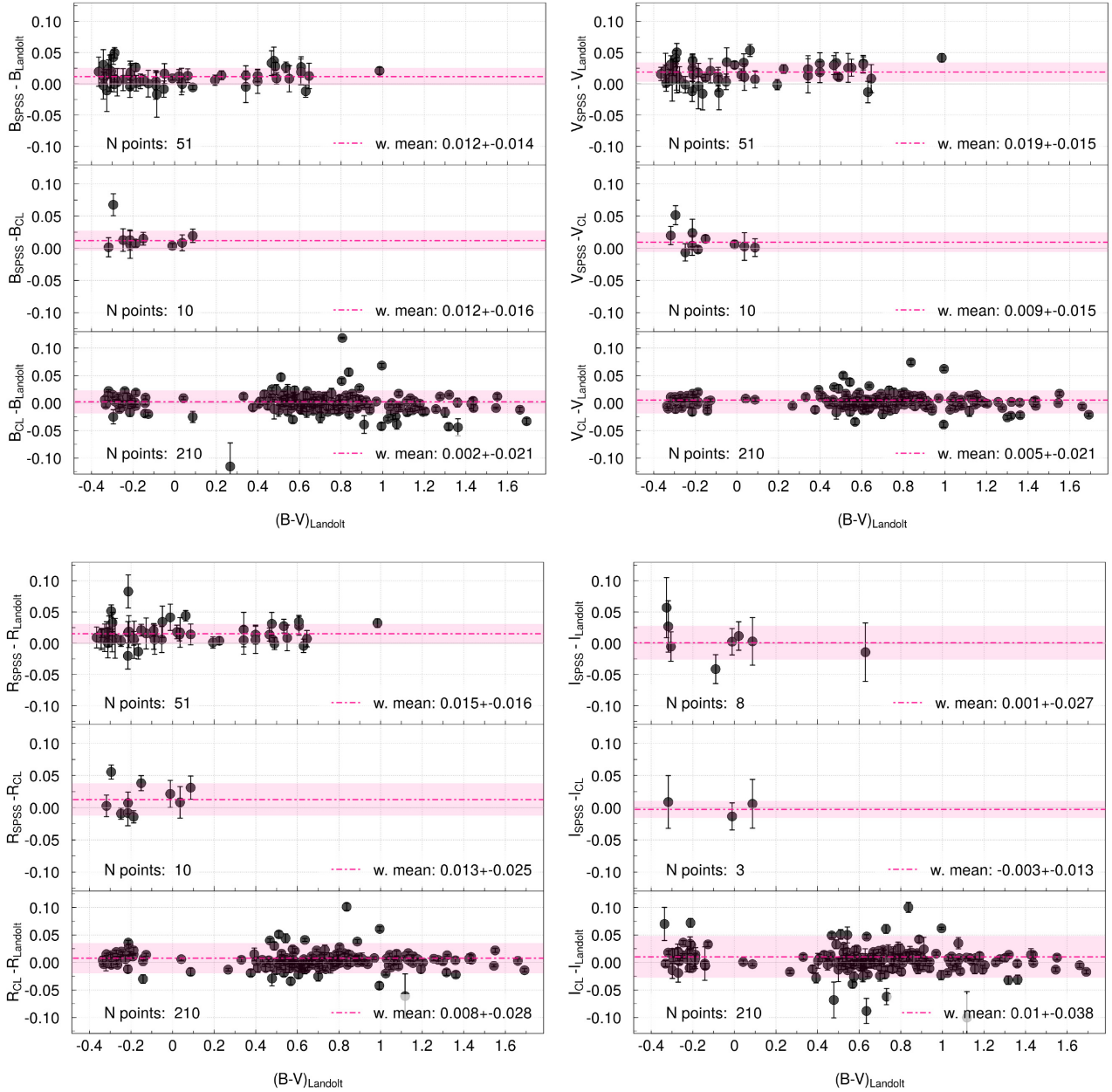


Figure 8. Comparison among the magnitudes of the SPSS, the Landolt, and the Clem collection (see Section 4.1 for details). Each of the four panels shows the results of one photometric band as a function of the $B - V$ colour. In each panel, the top graph shows the comparison between the SPSS and Landolt collections, the middle one between the SPSS and Clem collections, and the bottom one between the Clem and Landolt collections. The weighted averages are reported in each sub-panel, along with the number of stars in common between each pair of collections. One star lies outside the vertical limits in the bottom graph of the BVR band panels and two stars lie outside the limits in the bottom graph of the I band panel because we used the same limits as in Fig. 9.

many effects such as the differential atmospheric absorption between the standard lamp and the standard star light (whose correction requires a precise knowledge of the atmospheric transmission as a function of wavelength), the brightness difference between the two sources and the need to characterize the telescope/detector throughput. Early results have not been followed by many modern comparisons of laboratory standards to stars (Bohlin et al. 2014), even if new methods have been proposed (Smith et al. 2009), and this technique has been superseded by different approaches, nicely described in Stubbs & Brown (2015), based on calibrated detectors or on theoretical knowledge of the physics of hydrogen. In fact, as mentioned in Zimmer et al. (2016), over the last decades the

National Institute for Standards and Technology¹⁹ put aside emissive standards in favour of detector standards, such as silicon and InGaAs photodiodes (Larason, Bruce & Cromer 1996; Yoon et al. 2003), that have been calibrated against primary optical standards (Brown et al. 2006; Smith et al. 2009).

On the other hand, the flux distributions of spectrophotometric standard stars are currently based on model atmosphere calculations, as in the *HST* CALSPEC archive of flux standards, that rely on the calculated model atmospheres of three pure hydrogen white dwarfs

¹⁹<https://www.nist.gov/>

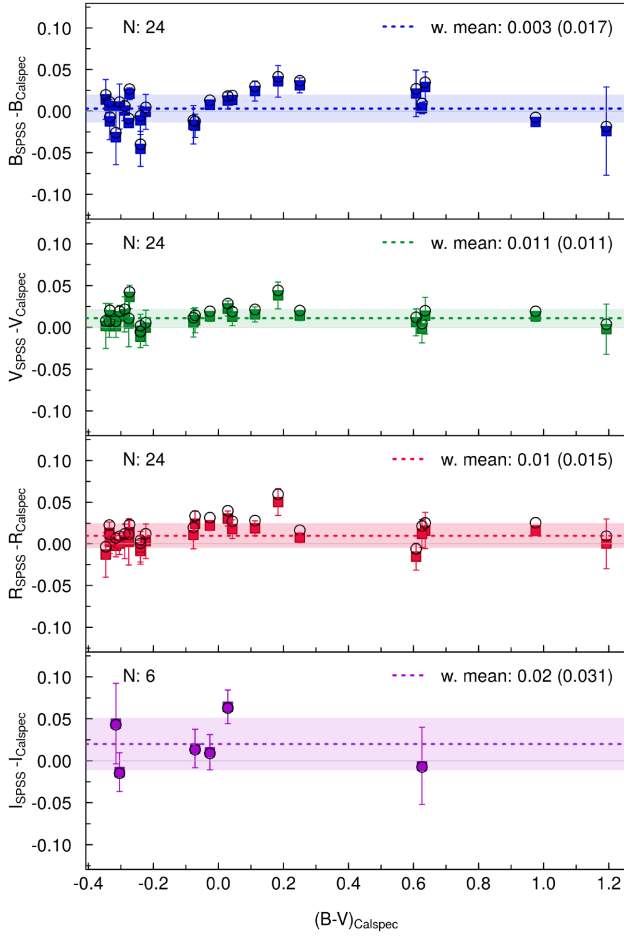


Figure 9. Comparison between the SPSS photometry and the synthetic photometry computed on the corresponding CALSPEC spectra using the passbands by Bessell & Murphy (2012). The filled and empty symbols correspond to the synthetic photometry computed using as reference star the Vega spectrum by CALSPEC or the one adopted for the *Gaia* photometric system, respectively (see Section 4.2). Each panel represents a different passband, as annotated, and the weighted mean of the differences (computed on the filled symbols) is reported in each panel and marked with a dotted line.

star normalized to an absolute flux level based on visible and IR absolute measurements (Bohlin 2007; Bohlin et al. 2014). In this case the uncertainties on model atmospheres must be accounted for, but there is good evidence that relative fluxes from the visible to the near-IR are currently accurate to ~ 1 per cent for the primary reference standards (Bohlin 2020). Once the standard stars are established, they can be used for absolute optical calibration under photometric conditions. In this lucky case the issue is no longer if the night is photometric but becomes how photometric it is, because subtle unnoticed atmospheric variations may affect the observations as well as other issues such as filters or instrumental mismatches. All these small effects can make it very difficult to reach an absolute calibration accuracy better than the current 1 per cent.

Nowadays detector and instrument capabilities probably have the potential to attain even a sub-percent accuracy, but their full exploitation requires techniques for monitoring the actual throughput of the telescopes (Stubbs et al. 2007; Regnault et al. 2009; Doi et al. 2010) and for monitoring the atmospheric layers above the ground-based telescope with a more accurate and complete spatial and temporal sampling than the classical weather stations. This ap-

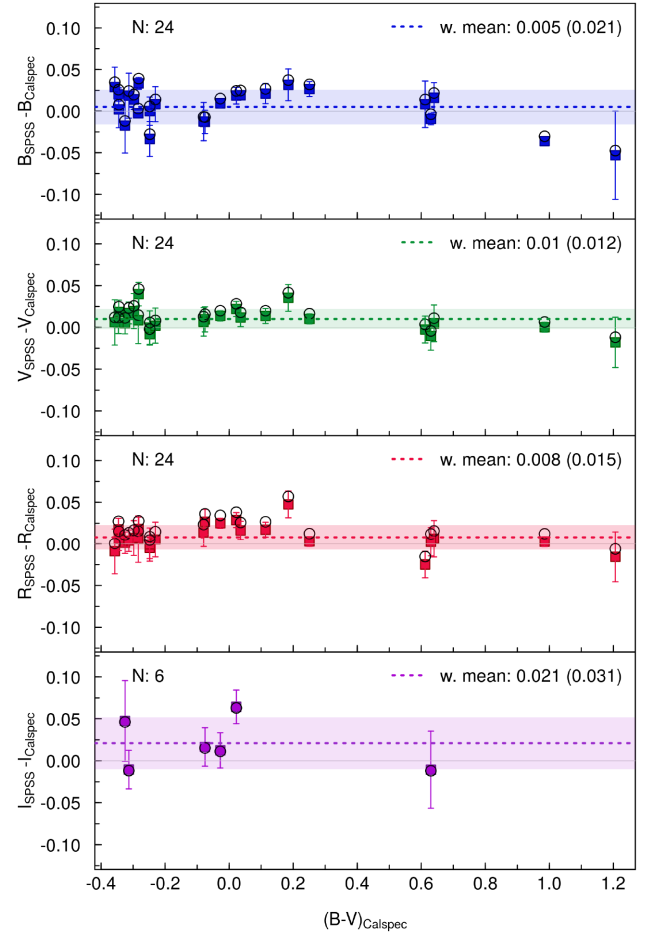


Figure 10. Same as Fig. 9, but applying the wavelength shifts proposed by Bohlin & Landolt (2015) to the Bessell & Murphy (2012) passbands.

proach, conceptually similar to the adaptive optics (AO) philosophy, should be able to provide photometric measurement corrections for direction-, wavelength-, and time-dependent astronomical extinction, as described in McGraw et al. (2010), Zimmer et al. (2010, 2016), pursuing the development of what we may call ‘Adaptive Photometry’, something similar to AO, but in the photometric regime. In this way, photometric observations can be corrected in real time, taking into account the actual transmission of the column of air through which calibrations are being made. Many researchers are focusing their efforts in developing methods of real-time direct atmosphere monitoring, but the details are beyond the scope of this paper. Nevertheless we note that the atmospheric calibration system for the Vera C. Rubin Observatory (previously known as LSST) is moving in this direction, including a 1.2 m dedicated atmospheric calibration telescope and a set of instrumentation to monitor precipitable water vapour and cloud cover (Sebag et al. 2014). All measurements by the atmospheric calibration telescope will be combined with MODTRAN²⁰ atmospheric models to characterize and monitor the night-time atmospheric properties, while a sun monitoring system will measure the atmospheric aerosols during daytime.

Free from atmospheric disturbances, rockets or balloon experiments can also boost the accuracy of stars absolute calibration.

²⁰MODerate resolution atmospheric TRANsmision, <http://modtran.spectral.com/>.

The Absolute Color Calibration Experiment for Standard Stars (ACCESS) rocket experiments (Kaiser et al. 2005, 2018) aims at an absolute spectrophotometric calibration accuracy of 1 per cent in the 0.35–1.7 μm range, but due to the short flight time outside the atmosphere, observations are limited to a few bright ($\lesssim 10$ mag) stars. High altitude balloons can provide long-term astronomical observations with virtually no atmospheric disturbance, but a suitable star tracking and image stabilization may be challenging (Fesen 2006). Satellites and small stratospheric balloons can also be used to lift a calibrated source above the atmosphere in order to use it as a standard source to determine the atmospheric transmission, as tested with the Cloud Aerosol Lidar and Infrared Pathfinder Satellite Observations (CALIPSO; Winker et al. 2009) or as devised by the Airborne Laser for Telescopic Atmospheric Interference Reduction (ALTAIR) project (Albert et al. 2016).

For the moment, however, the 1 per cent accuracy limit appears as the best that can be achieved with current equipment, and the SPSS magnitudes presented here are the best that can be done to assist the external calibration of *Gaia*, within the current framework. In the future, when more sophisticated solutions will become available, it will be certainly possible to recalibrate *Gaia* data starting from publicly available data.

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DATA AVAILABILITY

All relevant data generated during this study and not already available in this article and in its online supplementary material, will be made public through the SSDC *Gaia* Portal²⁸ with the final release of flux tables, that should correspond to the *Gaia* fourth release.²⁹

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²¹<https://aladin.u-strasbg.fr/>

²²<https://ui.adsabs.harvard.edu/>

²³<https://www.r-project.org/>

²⁴<https://sites.google.com/cfa.harvard.edu/saoimages9>

²⁵<https://www.astromatic.net/software/sextractor>

²⁶<http://simbad.u-strasbg.fr/simbad/>

²⁷<https://www.astro.princeton.edu/~rhl/sm/>

²⁸<http://gaiaportal.ssdsc.asi.it/>

²⁹<https://www.cosmos.esa.int/web/gaia/release>

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SUPPORTING INFORMATION

Supplementary data are available at *MNRAS* online.

Table 4. Calibrated magnitudes for the 198 good SPSS candidates.

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