



Publication Year	2022
Acceptance in OA	2023-06-06T13:08:53Z
Title	Turbulent magnetic field amplification in binary neutron star mergers
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Publisher's version (DOI)	10.1103/PhysRevD.106.023013
Handle	http://hdl.handle.net/20.500.12386/34238
Journal	PHYSICAL REVIEW D
Volume	106

Turbulent magnetic field amplification in binary neutron star mergers

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(Received 17 December 2021; accepted 27 June 2022; published 12 July 2022)

Magnetic fields are expected to play a key role in the dynamics and the ejection mechanisms that accompany the merger of two neutron stars. General relativistic magnetohydrodynamic (MHD) simulations offer a unique opportunity to unravel the details of the ongoing physical processes. Nevertheless, current numerical studies are severely limited by the fact that any affordable resolution remains insufficient to fully capture the small-scale dynamo, initially triggered by the Kelvin-Helmholtz instability, and later sourced by several MHD processes involving differential rotation. Here, we alleviate this limitation by using explicit large-eddy simulations, a technique where the unresolved dynamics occurring at the subgrid scales (SGS) is modeled by extra terms, which are functions of the resolved fields and their derivatives. The combination of high-order numerical schemes, high resolutions, and the gradient SGS model allow us to capture the small-scale dynamos produced during the binary neutron star mergers, as shown in previous works. Here, we follow the first 50 milliseconds after the merger and, for the first time, we find numerical convergence on the magnetic field amplification, in terms of integrated energy and spectral distribution over spatial scales. Among other results, we find that the average intensity of the magnetic field in the remnant saturates at $\sim 10^{16}$ G around 5 ms after the merger. After 20–30 ms, both toroidal and poloidal magnetic field components grow continuously, fed by the winding mechanism that provides a slow inverse cascade, i.e., gradually transferring kinetic into magnetic energy. We find no clear hints for magnetorotational instabilities and no significant impact of the magnetic field on the redistribution of angular momentum in the remnant in our simulations, probably due to the very turbulent and dynamical topology of the magnetic field at all stages, with small-scale components largely dominating over the large-scale ones. Although the magnetic field grows near the rotation axis of the remnant, longer large-eddy simulations are necessary to further investigate the formation of large-scale, helical structures close to the rotational axis, which could be associated to jet formation.

DOI: [10.1103/PhysRevD.106.023013](https://doi.org/10.1103/PhysRevD.106.023013)

I. INTRODUCTION

The breakthrough binary neutron star (BNS) merger event GW170817 marked the first multimessenger observation of a gravitational wave (GW) source and proved the huge scientific potential of these merging systems [1,2]. Besides providing the long-awaited compelling evidence that BNS mergers can produce powerful jets and Short Gamma-Ray Bursts [3–15] as well as a copious amount of heavy r-process elements (e.g., [16–20]; see also Ref. [21]

and Refs. therein), this event allowed for the first GW-based multimessenger constraints on the neutron star (NS) equation of state (EoS) [3,22] and the Hubble constant [23]. Nonetheless, crucial aspects of the merger and postmerger dynamics remain uncertain, including the actual mechanisms behind jet formation and matter ejection (e.g., [24]).

Numerical relativity simulations of merging BNSs represent the ideal approach to unveil the details of the physical processes involved in events like GW170817.

In this context, the last decade has been characterized by a rapid progress towards a higher and higher degree of realism with the inclusion of fundamental ingredients such as magnetic fields, temperature and composition dependent EoS, and neutrino radiation (see, e.g., Refs. [25–29] for recent reviews). In particular, magnetic fields are known to play a key role in the postmerger evolution, in powering relativistic jets, and in shaping the electromagnetic counterpart signals in general (e.g., [28] and Refs. therein). However, magnetohydrodynamics (MHD) increases significantly the complexity of the simulations and poses new computational challenges.

The amplification of magnetic fields during and after merger up to total magnetic energies of the order of 10^{51} erg is due to different mechanisms, including the Kelvin-Helmholtz instability (KHI, e.g., [30,31]), the Rayleigh-Taylor instability (RTI, e.g., [32]) and the magnetorotational instability (MRI, [33–37]), that act on very small scales and cannot be fully captured with the current affordable resolutions. Even the highest resolution (and computationally most expensive) simulations being performed nowadays are far from completely resolving these instabilities along with the associated MHD turbulence [38]. Different approaches have been proposed to overcome the above limitations and incorporate at least in part the effects of unresolved MHD processes.

One of the most common approaches is to impose a very strong initial magnetic field $\geq 10^{14}$ G (e.g., [38–43]), many orders of magnitude larger than the values inferred from current observations [44], in order to compensate for the inability to capture the KHI-induced amplification. However, the quantitative results obtained within this approach might not be fully reliable, since the amplification via KHI is more efficient on the under-resolved small scales and induces a turbulent flow which should not preserve the initial large-scale ordered field. One promising alternative relies on large eddy simulations (LESs), a technique in which the evolution equations are modified to account for the unresolved subgrid-scale (SGS) dynamics (e.g., [45]). Within this approach, the general relativistic MHD (GRMHD) equations are modified by including new terms into the induction equation [46–48]. Although the results of these studies show an effective growth of the magnetic field, they rely on arbitrarily tuning parameters of the extra terms, losing any predictive character. Other approaches have centered their attention on the turbulent viscous effect induced by the magnetic fields during the postmerger phase, evolving viscous hydrodynamics (HD) in substitution of the MHD equations [49–52]. These models mimic small-scale dissipation only; therefore, they are unable to capture the dynamo mechanism (which usually include additional processes, like kinetic-magnetic energy transfer and magnetic inverse cascade) and depend on physical parameters to be calibrated via very high resolution GRMHD simulations (e.g., [53]).

A more sophisticated alternative, based on the so-called gradient SGS model [54,55], has been first extended to compressible MHD [56] and more recently, also to special and general relativistic MHD [57,58]. The gradient SGS model relies on the mathematical Taylor expansion of the nonlinear fluxes of the MHD equations as a function of the resolved fields, with no *a priori* physical assumptions. The inclusion of these SGS terms in the equations allows us to recover, at least partially, the effects that the unresolved subgrid dynamics induce over the resolved scales. Each SGS term has a free normalization of order unity, which needs to be magnified to compensate for the numerical dissipation of the employed numerical scheme. In our scheme, enhancing such normalization for the induction equation SGS term, allows us to improve the convergence of the magnetic amplification excited by the KHI, both in box simulations [57,58] and in binary neutron star mergers [59].

In this paper, we present a set of simulations with and without SGS terms at different resolutions (finest grid spacing of 120, 60, and 30 m) for an equal mass BNS merger with a chirp mass that is consistent with GW17018 and a maximum initial magnetic field strength of 5×10^{11} G. The adopted EoS, a hybrid gamma-law EOS based on a piecewise polytropic approximation of APR4 [60] (as implemented in [61]), leads to a remnant NS which does not collapse to a black hole (BH) within the timespan of the simulations (up to 50 ms postmerger). We study the magnetic field amplification during and after merger and, for the first time, we find convergent results for the magnetic field growth in presence of SGS terms, also consistent with the highest resolution result without SGS terms. We then investigate the impact of magnetic fields on various aspects of the postmerger dynamics, including the evolution of the differential rotation profile of the remnant NS, the prospects for jet formation, matter ejection, and postmerger GW emission.

The paper is organized as follows. Section II introduces our GRMHD LES approach, the numerical methods and setup, the initial data, and a number of useful analysis quantities. In Sec. III, we recall a few fundamental notions that are at the base of our results, which are then presented in detail in Sec. IV. Finally, our concluding discussion is given in Sec. V.

II. NUMERICAL SETUP

A. Evolution equations: GRMHD LES

The concept and the mathematical foundations behind LES with a gradient SGS approach have been extensively explained in our previous works (and references therein) in the context of Newtonian [56] and relativistic MHD [57–59], to which we refer for details and further references. In the present work, we will evolve the full GRMHD equations with gradient SGS terms, exactly as described in

our previous paper [59] (but using a different EoS that will be introduced in Sec. II C).

The spacetime geometry is described by the Einstein equations. The covariant field equations can be written as evolution equations by performing the 3 + 1 decomposition (see, e.g., Ref. [62]), in which the line element can be written as

$$ds^2 = -\alpha^2 dt^2 + \gamma_{ij}(dx^i + \beta^i dt)(dx^j + \beta^j dt), \quad (1)$$

where α is the lapse function, β^i the shift vector, γ_{ij} the induced three-metric on each spatial slice, and $\sqrt{\gamma}$ is the square root of its determinant. In this work, we use the covariant conformal Z4 formulation of the evolution equations [63,64]. A summary of the final set of evolution equations for the spacetime fields, together with the gauge conditions setting the choice of coordinates, can be found in [65].

The GRMHD equations for a magnetized, nonviscous and perfectly conducting fluid [48] provide a set of evolution equations for the conserved variables $\{\sqrt{\gamma}D, \sqrt{\gamma}S^i, \sqrt{\gamma}U, \sqrt{\gamma}B^i\}$. These conserved fields are functions of the rest-mass density ρ , the specific internal energy ϵ , the velocity vector v^i and the magnetic field B^i (primitive fields), namely,

$$D = \rho W, \quad (2)$$

$$S^i = (hW^2 + B^2)v^i - (B^k v_k)B^i, \quad (3)$$

$$U = hW^2 - p + B^2 - \frac{1}{2} \left[(B^k v_k)^2 + \frac{B^2}{W^2} \right], \quad (4)$$

where $W = (1 - v^2)^{-1/2}$ is the Lorentz factor. The pressure p is obtained from the EoS as detailed in Sec. II C.

The full set of evolution equations, including the hyperbolic divergence cleaning via damping of a new field ϕ [65] and all the gradient SGS terms, can be found in [58,59]. Following our previous studies, we include only the SGS term that appears in the induction equation. This is motivated by the assumption that the term in the induction equation is the one most relevant for the magnetic field dynamics, which is the main interest of this work. The evolution equation reads

$$\begin{aligned} \partial_t(\sqrt{\gamma}B^i) + \partial_k[\sqrt{\gamma}(-\beta^k B^i + \beta^i B^k) \\ + \alpha\sqrt{\gamma}(\gamma^{ki}\phi + M^{ki} - \tau_M^{ki})] = \sqrt{\gamma}R_B^i, \end{aligned} \quad (5)$$

where $M^{ki} = B^i v^k - B^k v^i$, while the source term R_B^i is related to the divergence cleaning field (see Ref. [58] for its explicit expression). The SGS tensor is given by

$$\tau_M^{ki} = -C_M \xi H_M^{ki}, \quad (6)$$

where the explicit expressions for the tensor H_M^{ki} in terms of field gradients are quite lengthy and can be found in the Appendix A of [59].

Although the precoefficient C_M is meant to be of order one for a numerical scheme having a mathematically ideal Gaussian filter kernel and neglecting higher-order corrections, the value that best mimics the feedback of small scales onto the large scales in a LES can differ depending partially on the numerical methods employed and on the specific problem, as discussed in [56–59]. A value of $C_M = 8$ has been shown to reproduce the magnetic field amplification more accurately for the cases studied in [58,59], based on comparisons of different values and high resolutions simulations (note that less dissipative numerical schemes would need smaller values of C_M). Clearly, it would be beneficial if a single value of C_M could be used for a wide range of scenarios, thus avoiding expensive calibration. For the test case in this work, we therefore assess the benefits of our scheme using the same value $C_M = 8$.

Hereafter, we refer to this particular choice of SGS terms as LES, as opposed to a standard simulation with no SGS terms (i.e., $C_M = 0$). The coefficient $\xi = \gamma^{1/3} \Delta^2 / 24$ is proportional to the spatial grid-spacing squared—typical for SGS models—and hence, ensures by construction the convergence to the continuous limit.

B. Numerical methods

As in our previous works, we use the code MHDUET, generated by the platform SIMFLOWNY [66,67] and based on the SAMRAI infrastructure [68,69], which provides the parallelization and the adaptive mesh refinement. The code has been deeply tested for different scenarios [58,65,70,71], including basic tests of MHD and GR. In short, it uses fourth-order-accurate operators for the spatial derivatives in the SGS terms and in the Einstein equations (the latter are supplemented with sixth-order Kreiss-Oliger dissipation); a high-resolution shock-capturing (HRSC) method for the fluid, based on the Lax-Friedrich flux splitting formula [72] and the fifth-order reconstruction method MP5 [73]; a fourth-order Runge-Kutta scheme with sufficiently small time step $\Delta t \leq 0.4\Delta$ (where Δ is the grid spacing); and an efficient and accurate treatment of the refinement boundaries when subcycling in time [74,75]. A complete assessment of the implemented numerical methods can be found in [65,70].

The binary is evolved in a cubic domain of size $[-1204, 1204]$ km. The inspiral is fully covered by seven fixed mesh refinement (FMR) levels. Each consists of a cube with twice the resolution of the next larger one. In addition, we use up to two adaptive mesh refinement (AMR) levels. Within those, the refinement criterion is simply based on density, increasing the resolution within regions where the density is above $5 \times 10^{12} \text{ g cm}^{-3}$. This choice leads to a uniform resolution throughout the shear layer. We compare simulations with 0–2 AMR levels,

TABLE I. *Parameters of the simulations:* different resolutions, mesh refinement setup (with the finest grid spacing $\Delta_{\min}$ covering a region of size $\Delta L_{\min}$), and values of C_M . Each setup is adopted at the merger time, while the inspiral phase is common to all of them and is run under the LR configuration. The domain of the finest AMR grid for the MR and HR cases changes with time, so that the values indicated here are only approximated. We have also included a LES with MR and no magnetic fields (MR B0) for comparison purposes.

Case	C_M	Refinement levels	$\Delta L_{\min}$ (km)	$\Delta_{\min}$ (m)
LR	0	7 FMR	$[-28, 28]$	120
MR	0	7 FMR +1 AMR	$[-13, 13]$	60
HR	0	7 FMR +2 AMR	$[-11, 11]$	30
LR LES	8	7 FMR	$[-28, 28]$	120
MR LES	8	7 FMR +1 AMR	$[-13, 13]$	60
HR LES	8	7 FMR +2 AMR	$[-11, 11]$	30
MR B0	8	7 FMR +1 AMR	$[-13, 13]$	60

labeled LR,MR,HR, but same FMR grid. This setup allows us to study the convergence in the bulk region, which is our main interest, while saving resources in the outer envelope. With this grid structure, we achieve a maximum resolution of $\Delta_{\min}$ in a domain $\Delta L_{\min}$ covering at least the most dense region of the remnant. The specific values of these grid parameters, for the different resolutions considered here, can be found in Table I.

Finally, we apply the SGS terms only in regions where the density is higher than $6 \times 10^{13} \text{ g cm}^{-3}$. One reason is to avoid potential spurious effects during the inspiral near the stellar surface and in the atmosphere. More importantly, our grid setup allows us to study the convergence only in the dense region. Since the remnant's maximum density is above $10^{15} \text{ g cm}^{-3}$, the SGS model is still applied to a considerable volume covering the bulk of the remnant. Thus, the setup still allows us to capture the MHD instabilities leading to a strong amplification of the magnetic field soon after the merger.

C. EoS and conversion to primitive variables

We consider a hybrid EoS during the evolution, with two contributions to the pressure. For the cold part, we use a tabulated version of the piecewise polytrope fit to the APR4 zero-temperature EoS [60], with a modification to prevent superluminal speeds [61]. The contributions of thermal effects are modeled by the gamma-law $p_{\text{th}} = (\Gamma_{\text{th}} - 1)\rho\epsilon$, with adiabatic index $\Gamma_{\text{th}} = 1.8$.

The conversion from the evolved or conserved fields to the primitive or physical ones is performed by using the robust procedure introduced in [76]. Following a common practice in GRMHD simulations, the surrounding regions of the neutron stars are filled with a relatively tenuous, low-density *atmosphere*, which is necessary to prevent the failure of the HRSC schemes usually employed to solve the MHD equations. To minimize unphysical states of the

conserved variables outside the dense regions, produced by the numerical discretization errors of the evolved conserved fields, we enforce a minimum density in the atmosphere of $6 \times 10^5 \text{ g cm}^{-3}$, while setting the velocity to zero and the magnetic field to its previous value in these regions.

D. Initial conditions

The initial data are created with the LORENE package [77], using the APR4 zero-temperature EoS described above. We consider an equal-mass BNS in quasicircular orbit, with an irrotational configuration, a separation of 45 km and an angular frequency of 1775 rad s^{-1} . The chirp mass $M_{\text{chirp}} = 1.186 M_{\odot}$ is the one inferred in the refined analysis of GW170817 [22], implying a total mass $M = 2.724 M_{\odot}$ for the equal mass case.

Each star initially has a purely poloidal dipolar magnetic field that is confined to its interior, calculated from a vector potential $A_{\phi} \propto R^2(P - P_{\text{cut}})$, where P_{cut} is a hundred times the pressure of the atmosphere, and R is the distance to the axis perpendicular to the orbital plane passing through the center of each star. The maximum magnetic field (at the centers) is $5 \times 10^{11} \text{ G}$. This is orders of magnitude lower than the large initial fields used in other simulations (e.g., [31,38–42]) and not too far from the upper range of expectations for old NSs (e.g., [78]). Such values are also at the lower border of computational feasibility, since the accurate evolution for too small ratios of magnetic-to-kinetic pressure is hampered by discretization errors. Nevertheless, the initial topology is quickly forgotten after merging: acting only as a seed for the KHI, it has a negligible effect on the final magnetic field configuration of the remnant, as long as the initial values are not too large ($B \lesssim 10^{13} \text{ G}$ for a medium resolution), as we show in an accompanying paper [79].

E. Analysis quantities

Below, we introduce definitions of several integral quantities that we use to monitor the dynamics in different regions. For instance, we compute suitable averages of the magnetic field strength; the fluid angular velocity $\Omega \equiv \frac{d\phi}{dt} = \frac{u_{\phi}}{u^t}$ [where $u_a \equiv W(-\alpha, v_i)$ denotes the fluid four-velocity]; and the plasma beta parameter, $\beta = \frac{2p}{B^2}$. The averages for a given quantity q over a certain region $\mathcal{N}$ will be denoted generically by

$$\langle q \rangle_a^b = \frac{\int_{\mathcal{N}} q d\mathcal{N}}{\int_{\mathcal{N}} d\mathcal{N}}, \quad (7)$$

where $\mathcal{N}$ stands for a volume V , a surface S , or a line ℓ , and the integration is restricted to regions where the mass density is within the range $(10^a, 10^b) \text{ g/cm}^3$. If b is omitted, it means no upper density cut is applied. In particular, we define averages over the bulk of the remnant as $\langle q \rangle_{13}$ and averages over the envelope as $\langle q \rangle_{10}^{13}$. Surface

integrals are carried out over a cylinder S with axis passing through the center of mass¹ and orthogonal to the orbital plane. Line integrals are carried out along circles ℓ around the same axis. In cylindrical coordinates (R, ϕ, z) , the relevant surface and line elements are, respectively,

$$dS = \sqrt{\gamma_{zz}\gamma_{\phi\phi} - \gamma_{z\phi}^2} d\phi dz,$$

$$d\ell = \sqrt{\gamma_{\phi\phi}} d\phi.$$

We also compute global quantities, integrated over the whole computational domain, such as the total baryonic mass E_{bar} , magnetic energy E_{mag} , thermal energy E_{th} and rotational kinetic energy E_{rot} , defined by

$$E_{\text{bar}} = \int \rho W \sqrt{\gamma} dx^3, \quad (8)$$

$$E_{\text{mag}} = \frac{1}{2} \int B^2 \sqrt{\gamma} dx^3, \quad (9)$$

$$E_{\text{th}} = \int \rho W (\epsilon - \epsilon_{\text{cold}}) \sqrt{\gamma} dx^3, \quad (10)$$

$$E_{\text{rot}} = \frac{1}{2} \int \Omega T_{\phi}^t \sqrt{\gamma} dx^3, \quad (11)$$

where T_{ϕ}^t are just the time-azimuthal components of the stress-energy tensor for a perfect fluid.

An informative way to analyze the results is by computing the distribution of the kinetic and magnetic energies over the spatial scales, simply called spectra hereafter, and defined respectively as

$$\mathcal{E}_k(k) = \frac{L^3 4\pi}{(2\pi)^3 N^6} \langle k^2 |\widehat{\rho\vec{v}}|^2(\vec{k}) \rangle_k, \quad (12)$$

$$\mathcal{E}_m(k) = \frac{L^3 4\pi}{(2\pi)^3 N^6} \langle k^2 |\hat{B}|^2(\vec{k}) \rangle_k, \quad (13)$$

where $L = 32$ km is the size of a dominion containing the densest part of the remnant over which we perform the fast Fourier transform (indicated here by the wide hat), $k \in [2\pi/L, \pi/\Delta]$ is the radial wave number, $\langle \rangle_k$ is the average over the spherical surface in the Fourier space corresponding to a fixed radial wave number $k_r = k$, and $N = L/\Delta$ is the number of points per each direction (ensuring the correct normalization). For the magnetic spectra, we also calculate the poloidal and toroidal contributions separately. Further details of the numerical procedure to calculate the spectra can be found in [58,59,70]. Note that in those works, the spectra were calculated taking into account only

¹The center of mass is calculated using the nonrelativistic formula.

the bulk of the remnant, by setting to zero the fields below a certain threshold density. Here, in order to preserve the large wavelength modes and to include at least partially the solution in the outer envelope, we decided to not modify the fields in any way. This choice comes at the price of not having periodic boundary conditions in our domain, which will induce a artificial pileup of energy at very high wave numbers. With these spectrum distributions we can define the spectra-weighted average wave number,

$$\bar{k} \equiv \frac{\int_k k \mathcal{E}(k) dk}{\int_k \mathcal{E}(k) dk}, \quad (14)$$

with an associated length scale $\delta R = 2\pi/\bar{k}$, which represents the typical coherent scale of the structures present in the field.

Although it is not the main goal of this article, we also compute the ejected mass and the GWs emitted by the system. The ejected mass is estimated from the flux of unbound mass crossing a sphere of radius r far away from the source, namely,

$$\dot{M}_{ej} = \int \alpha J^r r^2 \sqrt{\gamma} d\Omega, \quad J^r = \rho W \left(v^r - \frac{\beta^r}{\alpha} \right). \quad (15)$$

The gravitational radiation is described in terms of the Newman-Penrose scalar Ψ_4 , which can be expanded in terms of spin-weighted $s = -2$ spherical harmonics [80,81], namely,

$$r\Psi_4(t, r, \theta, \phi) = \sum_{l,m} C_{l,m}(t, r) Y_{l,m}^{-2}(\theta, \phi). \quad (16)$$

The coefficients $C_{l,m}$ are extracted from spherical surfaces at different extraction radii $r_{\text{ext}} = (150, 300, 450)$ km. The angular frequency of each gravitational-wave mode can be calculated easily from

$$\omega_{l,m} = -\Im \left(\frac{\dot{C}_{l,m}}{C_{l,m}} \right). \quad (17)$$

We recall that the angular frequencies ω_{src} of remnant oscillations are related to the resulting GW components by $\omega_{l,m} = m\omega_{\text{src}}$.

III. THE BIG PICTURE

The dynamics during the merger and postmerger is very rich, so one could expect several MHD processes operating to amplify and sustain the magnetic field in timescales up to hundreds of milliseconds. These processes have been analytically studied under idealized conditions: however, since our scenario is very nonlinear and highly dynamical, it is not easy to clearly distinguish them. First, the shear layer that forms when the surfaces of the NSs touch is

subject to the KHI. The Rayleigh-Taylor instability (RTI) could also play a role, and together they can generate a turbulent state, that can lead to a small-scale dynamo. Secondly, the MRI [33,34] can also amplify the magnetic field and maintain a turbulent state in the remnant, as suggested by global numerical simulations [35–37]. In addition, the differential rotation tends to wind up the magnetic field lines. Here, we review some of the relevant aspects.

- (i) Kelvin-Helmholtz instability (or dynamical shear instability): in a shear layer of thickness d between two fluids moving with opposite directions, all the modes with wavelength $\lambda > d$ are going to be unstable and produce vortexes with a growth rate given by (see, e.g., Refs. [30,82])

$$\sigma = \frac{\pi \Delta v}{\lambda}, \quad (18)$$

where Δv is the jump in velocity across the shear layer. As a result of this vortex motion, magnetic fields are wound, and their strength are amplified in an exponential manner within a timescale given by

$$t_{\text{KHI}} \sim \sigma^{-1} \sim 10^{-3} \text{ ms} \left(\frac{\lambda}{1 \text{ km}} \right) \left(\frac{0.5c}{\Delta v} \right), \quad (19)$$

which is much smaller than the characteristic timescale of the system. Note that smaller wavelengths grow faster, inducing a turbulent state that further amplifies the magnetic energy via small-scale dynamo processes.

- (ii) Rayleigh-Taylor instability: it operates on the interface between two fluids where the density gradient is misaligned with the direction of the local gravitational field. The instability characteristically evolves with rising bubbles of less dense fluid and sinking spikes of more dense fluid that propagate away from the interface. The nonlinear interaction of the bubbles and the spikes induces a region of turbulent mixing. It has been recently proposed [32] that the small-scale dynamo driven by RTI turbulence might help to explain the observed magnetic energy amplification, on the timescale of microseconds, developing in the outer regions of the remnant, which would act complementary to amplification by the KHI observed mostly in the core.
- (iii) Magnetorotational instability (MRI, or magnetic shear instability): originally studied for disks [33], it requires a differential rotation, $\partial_R \Omega < 0$, e.g., in a Keplerian disk, $\Omega = \Omega_K \sim R^{-3/2}$. Assuming idealized condition of a very smooth large-scale magnetic field (usually uniform in the vertical or azimuthal direction, or dipolar), some modes can quickly grow at the expenses of the rotational energy. These

modes consist of adjacent channels having different angular momentum and magnetic fluxes, with a spatial width corresponding to the fastest growing MRI modes. At the end of the first exponential growth phase, the instability saturates and the channels dissolve into a turbulent flow featuring a complex magnetic field topology. These channel-flow structures (and the subsequent turbulent state, which increases the effective viscosity of the fluid) redistribute angular momentum from internal regions to external ones. The characteristic timescale and wavelength for the fastest growing mode may be estimated (see, e.g., Ref. [83]) by

$$t_{\text{MRI}} = 2 \left| \frac{\partial \Omega}{\partial \ln R} \right|^{-1} \approx \frac{4}{3 \Omega} \approx 0.1 \text{ ms} \left(\frac{10 \text{ rad/ms}}{\Omega} \right) \quad (20)$$

$$\lambda_{\text{MRI}}^i \approx \frac{2\pi}{\Omega} v_A^i \approx 600 \text{ m} \left(\frac{10 \text{ rad/ms}}{\Omega} \right) \times \left(\frac{\bar{B}^i}{10^{16} \text{ G}} \right) \left(\frac{10^{15} \text{ g/cm}^3}{\bar{\rho}} \right)^{\frac{1}{2}}, \quad (21)$$

where $v_A^i = \bar{B}^i / \sqrt{4\pi\bar{\rho}}$ is the Alfvén speed in the direction x^i , and we have assumed a Keplerian profile. Here, $\bar{B}^i, \bar{\rho}$ represent the mean values (i.e., in space and time) of the magnetic field and the density. Note that in a turbulent flow $\bar{B}^i = 0$ and the previous estimates are meaningless for two reasons. The first one is that it is necessary to introduce an effective Alfvén speed, as we will discuss later. The second one is that the fundamental assumption of the linear analysis leading to the instability phase requires idealized, very smooth (i.e., over length scales much larger than λ_{MRI}) and static (i.e., over timescales much longer than t_{MRI}) background magnetic fields. As we will show, this condition is very hardly satisfied in the BNS postmerger scenario, consisting since the very beginning of a very dynamical, small-scale dominated magnetic field. Although the MRI could still play a role, the quantitative estimations of the fast growing modes λ_{MRI} are in general not reliable.

- (iv) Winding up effect: for axisymmetric configurations it is easy to show (see, e.g., Ref. [83]), using the induction equation and the solenoidal constraint, that the toroidal magnetic field $B^T \equiv R B^\phi$ will grow linearly as

$$|B^T| = tR \left| B^R \frac{\partial \Omega}{\partial R} \right| \approx \frac{3}{2} \Omega t |B^R|, \quad (22)$$

where we have assumed again a Keplerian profile to obtain the last relation. The twisting of the magnetic fields increases its tension, which will grow until

it can eventually brake the fluid motion, approximately when the toroidal magnetic energy $B_T^2/(4\pi)$ reaches the rotational energy $\rho R_*^2 \Omega^2$ (R_* being the typical radius of the remnant). Using the expression Eq. (22) for B^T , the magnetic braking occurs in a timescale given by

$$t_{\text{brake}} \sim \frac{R_*}{v_A} \approx 15 \text{ ms} \left(\frac{R_*}{15 \text{ km}} \right) \times \left(\frac{10^{16} \text{ G}}{B} \right) \left(\frac{\rho}{10^{15} \text{ g/cm}^3} \right)^{\frac{1}{2}}. \quad (23)$$

Note that most of the previous estimates are performed under the linear analysis of a background smooth, idealized magnetic field topology (e.g., purely vertical or toroidal) and fluid flow. This does not necessarily apply to the situation after merger. For example, the vorticity field of the disk studied in [84] is quite irregular. The MRI and the winding estimates use the Alfvén speed, which implies a mean magnetic field $\bar{B}^i$ coherent in spatial and timescales much larger than those of the instabilities. In turbulent flows, the magnetic field is small scale, randomly oriented, meaning that $\bar{B}^i = 0$. In such flows, the waves can not propagate, at least during a relatively long timescale, in any specific direction. Nevertheless, one can still define an effective Alfvén velocity. For instance, one can assume that the linear analysis is valid in a size given by the length of the characteristic vortices of the turbulent magnetic field [38]. A more restrictive condition is to consider that the perturbations undertake a random walk. In both cases, the effective Alfvén velocity can be written in the same generic way,

$$v_A^i = \frac{\bar{B}^i}{\sqrt{4\pi\rho}} \left(\frac{\delta R}{R_*} \right)^n, \quad (24)$$

with $n = 1$ for the mean values valid in the characteristic spatial scale of the turbulent magnetic field δR and $n = 2$ for the random walk estimate. By considering values $\delta R \approx 750 \text{ m}$, we obtain that v_A is modified by a factor

0.05–0.0025, depending on the value of n . This means that the modified t_{brake} is extended by 1 or 2 orders of magnitude, indicating that the winding will fully develop in much longer timescales of hundreds of milliseconds. Along the same lines, it would imply also that the λ_{MRI}^i is decreased by the same factor, making it even more challenging to resolve it. Even in that case, t_{MRI} does not depend on the Alfvén velocity. Therefore, if the field moves in shorter timescales, the MRI can not fully develop. These considerations imply that the MRI could act only if the field is not too turbulent and is well organized at large scales. We will further discuss these issues by comparing with the results of our simulations in the conclusions.

IV. RESULTS

Here we present a set of simulations of the equal-mass BNS initial data described before, with and without SGS terms for three different resolutions, as specified in Table I.

A. Qualitative dynamics

The stars perform roughly five orbits before merging. By inspecting the density profiles in the equatorial plane, we observe that after the first contact, the merging cores of the two stars perform radial bounces with a period of roughly 1 ms, embedded within a common envelope. The cores perform roughly ten damped oscillations before settling down into a slow-varying, approximately axisymmetric fluid configuration. Based on the density and angular velocity profiles, one can roughly separate the remnant into a high-density *bulk*, which extends for $\rho \geq 10^{13} \text{ g/cm}^3$, and an *outer envelope* (also known as a disk) with densities $10^{13} \text{ g/cm}^3 \geq \rho \geq 5 \times 10^{10} \text{ g/cm}^3$, which is initially torus-shaped and orbits close to Keplerian velocity. These regions quickly evolve with time, as shown in Fig. 1 for some representative snapshots during the first 10 ms of the evolution. The bulk soon settles into a roughly ellipsoidal shape, with strong differential rotation, and an approximate equatorial radius of 15 km. Similarly, the outer envelope region is very irregular and dynamical after the merger, but becomes more axisymmetric and ellipsoidal-shaped at later

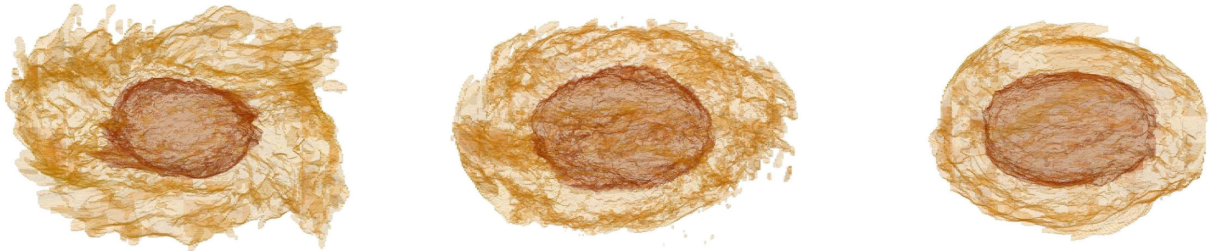


FIG. 1. *Surfaces of constant density in the remnant.* From left to right, we show representative times $t = (4, 6, 9) \text{ ms}$ after the merger. The collision produces a rotating massive remnant that eventually settles down into a spinning neutron star surrounded by an extended torus or outer envelope. The inner surface, at $\rho = 10^{13} \text{ g/cm}^3$, shows the transition between the bulk and envelope. The outer surface, at $\rho = 10^{12} \text{ g/cm}^3$, displays (partially) the shape of the envelope.

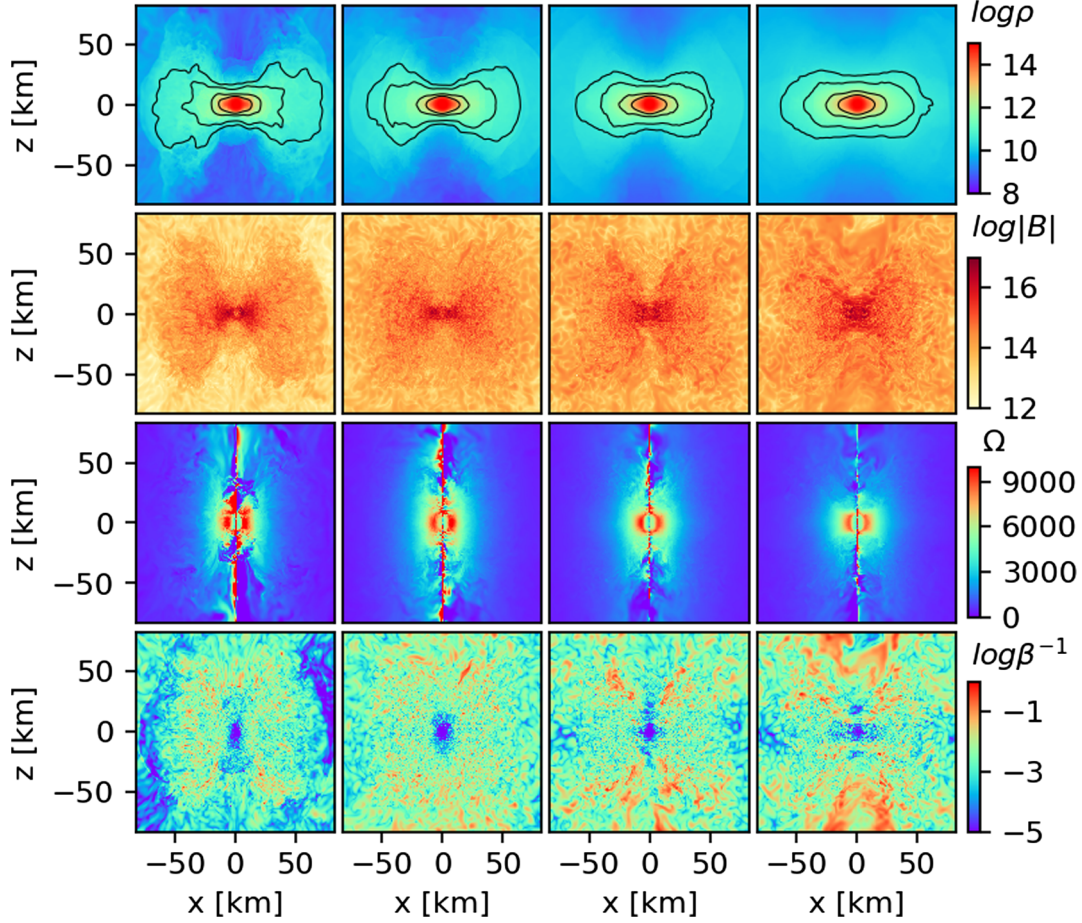


FIG. 2. *Evolution of relevant quantities of the remnant in a meridional plane.* The rows show, from top to bottom, the rest-mass density in g/cm^3 , magnetic field intensity in Gauss, angular velocity of the fluid Ω in rad/s , and inverse of β factor, at $t = (5, 10, 30, 50)$ ms after the merger, for the medium resolution LES simulation. In the rest-mass density plots (first row), black solid lines represent constant density surfaces at $\rho = (5 \times 10^{10}, 10^{11}, 10^{12}, 10^{13}) \text{ g/cm}^3$.

times, covering a region that extends approximately to a radii of 50 km in the equatorial plane.

A general overview of the dynamics can be obtained from the various fields displayed in Fig. 2, showing the meridional $y = 0$ plane. The first row shows the mass density distribution: soon after the merger, the remnant is surrounded by a torus-shaped distribution of marginally bound matter. At later times, the fluid in the torus expands in the polar directions, polluting the region near the z axis. The magnetic field (second row) is amplified quickly in the few ms after the merger, and then it is spread by the fluid flow. The angular velocity of the fluid (third row) shows strong differential rotation near the transition between the bulk and the envelope, along both the cylindrical radial (R) and vertical (z) directions. Neither the shape nor the values of this quantity change significantly during the timescale of our simulations. Finally, the evolution of β^{-1} (fourth row) shows how the magnetic pressure gradually acquires importance compared to the fluid one. The pressure is always dominated by the fluid, except at late times near the

rotational axis where they are comparable, suggesting the formation of a magnetically dominated region.

Let us now focus on how the magnetic field amplification works in the first 10 ms after the merger, along the lines of our previous discussion in Sec. III. The main features of the magnetic field evolution can be observed in Fig. 3, where the field intensity and isodensity contours at $\rho = (10^{13}, 5 \times 10^{14}) \text{ g/cm}^3$, identifying the transition between dense core, bulk, and envelope, are displayed in the orbital plane for our highest-resolution run. A thin, rotating shear layer is produced at the time of the merger between the colliding cores that move in opposite directions. This is the perfect premise to develop the KHI, manifested by the typical curly structures at small scales. The fastest-growing modes are expected to be the ones with a wavelength similar to the layer thickness, which might be much thinner (possibly, submeter scale) than any currently achievable resolution. Our simulation is accurate enough to capture the formation of very small eddies (measuring a few numerical points, see the finest details in color scale the Fig. 3).

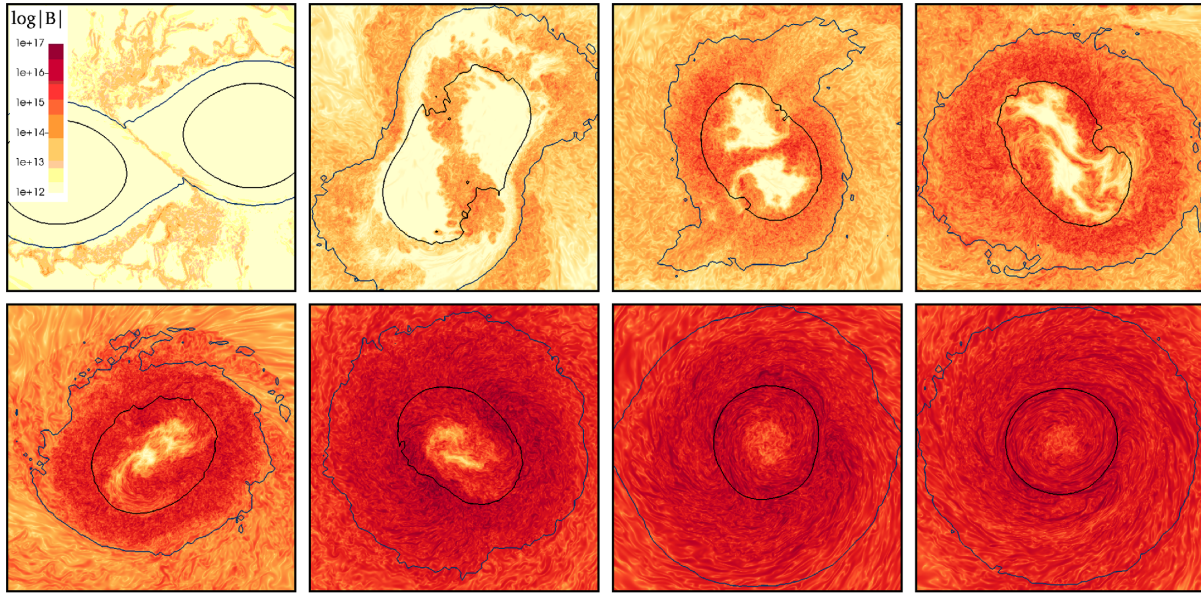


FIG. 3. *Evolution of the magnetic field intensity in the orbital plane.* Snapshots at $t = (0.5, 1.5, 2, 2.5, 3.5, 5, 10, 15)$ ms after the merger, displaying the magnetic field strength in Gauss, together with constant density contours at $\rho = (10^{13}, 5 \times 10^{14})$ g/cm³ showing the transition region between the bulk and envelope of the remnant, as well as the location of very high dense regions. The amplification is mostly driven by the KHI, possibly with contributions from the RTI in the initial stages in the envelope (see top left plot). They induce a turbulent small-scale dynamo, generated mostly near the shear layer, that is quickly advected by the fluid motions and diffuses throughout both the bulk and the envelope.

In agreement with the general expectation, the nonlinear interaction of these growing modes, with different scales, produces a turbulent dynamics with a direct energy cascade, where the kinetic energy is transferred from large to small scales. These small eddies twist and stretch the magnetic field of the remnant, increasing quickly the magnetic energy at the expenses of the kinetic one. As we will show later, this energy transfer is more efficient at small scales and acts as a powerful turbulent dynamo. There is also a significant growth of the magnetic field occurring at the surface of the stars during the merger, possibly due to a small-scale turbulence excited by the RTI or the KHI (i.e., see the top left panel in Fig. 3).

After few milliseconds, the maximum intensity of the magnetic field lies not in the plane between the cores, but in the region separating bulk and outer envelope. The fluid mixing induced by the complex fluid flow during and after merger is able to spread very efficiently the turbulent state of fluid and magnetic fields to most of the remnant in a short timescale. After reaching a peak, about 5 ms after the merger, the magnetic field intensity is advected through the remnant, but it does not show any significant amplification during the first 20 ms after the merger. From that time until the end of our simulation, the dynamics develop larger and more coherent magnetic field structures whose intensity grow linearly with time, possibly due to the winding mechanism.

B. Energetics evolution

In order to provide a more quantitative global analysis, we now discuss the evolution of the integrated energies and

averaged fields in the remnant. The total rotational kinetic, thermal, and magnetic energies are displayed in Fig. 4 for all our magnetized simulations.

We observe that, around ~ 10 ms after the merger, the rotational kinetic energy stabilizes at $E_{\text{rot}} \sim 3 \times 10^{53}$ ergs. At this time, the remnant has settled down into a slowly varying fluid configuration approaching axial symmetry. The thermal energy is of a similar order and slowly increases in time. This is likely due to shock heating, first in the merging stars, and later in the envelope, which is perturbed by the oscillating remnant. For comparison, the total baryonic mass (which is conserved up to 0.7% during the time span by our simulations) corresponds to an energy of about $E_{\text{bar}} \sim 5 \times 10^{54}$ ergs.

A comparison between different resolutions shows that in the low-resolution case (blue curves) a significant part of the heating comes from the intrinsic dissipation of the numerical scheme (as one can infer from the faster increase). For the other cases (LES and standard simulations), the differences are minor, indicating that (i) they are in the convergence regime and (ii) the LES approach with the SGS gradient model does not introduce spurious heating in the fluid evolution. On the other hand, the magnetic energy evolution shows significant differences between the two groups of simulations. Both high-resolution simulations (LES and standard) and the medium-resolution LES all present a sharp increase in the first few milliseconds after the merger. After 5 ms, the magnetic energy reaches a peak $E_{\text{mag}} \sim 3 \times 10^{50}$ ergs, 3 orders of magnitude below the

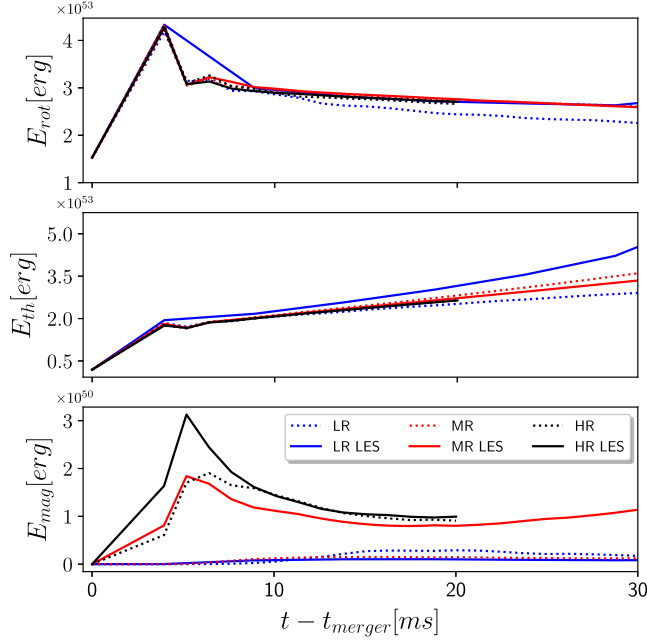


FIG. 4. *Evolution of the energies.* The panels show the rotational, thermal, and magnetic energies, integrated over the full domain. Colors identify the different resolutions, for LES (solid lines) and standard simulations (dashed). Note that these quantities are computed in a postprocessing step from saved 3D data, which is available only every few ms for some portions of the simulations. This leads to an uneven time resolution of the curves, especially for the cases with less output like LR LES.

thermal and rotational energy. During the next 15 ms, the magnetic field energy slightly decreases and saturates roughly at 10^{50} ergs. Then it increases again, following a quadratic function, and reaching $E_{\text{mag}} \sim 2 \times 10^{50}$ ergs towards the end of our longest simulation, at 50 ms after the merger. In contrast, the low-resolution simulations (LES and standard) and the medium-resolution standard simulation are incapable of capturing the instability that induces this magnetic field amplification. At this point, we would like to recall that the SGS terms are not being applied in the outer envelope, so our results demonstrate the benefits only in the bulk region.

C. Convergent magnetic field amplification: The effects of KHI, winding, and MRI

To get a more fine-grained picture of the magnetic amplification, we now study the averages in the bulk and the outer envelope separately. In Fig. 5, we show the magnetic field intensity for all the simulations, averaged either in the bulk or in the envelope. In the bulk, the averaged intensities differ by up to 2 orders of magnitude between the lowest and the highest resolutions. For all of the cases, magnetic fields are amplified by at least 3 orders of magnitude in a short timescale lasting about 5 ms. This amplification phase is followed by a saturation phase where

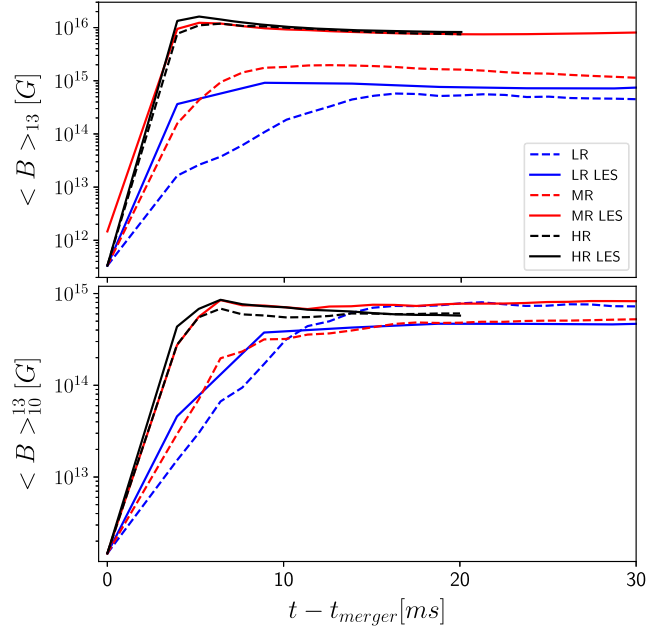


FIG. 5. *Evolution of the average magnetic field.* Volume average of the magnetic field intensity either in the bulk (top) or in the envelope (bottom) of the remnant. These averages are calculated for all the resolutions (identified by colors), both for the LES (solid lines) and for the standard simulations (dashes). Clearly, the averages in the bulk calculated with LES converge to a well-defined value.

the intensity is nearly constant for tens of milliseconds. The standard simulations display the lack of convergence commonly found already in the literature; as the resolution is increased, so does the saturation level reached by the averaged magnetic field.

The LES with the gradient SGS model behave in a completely different manner. For the first time, to our knowledge, we found convergence in the evolution of the averaged magnetic field: the medium resolution LES already grows and saturates at the same quantitative level, approximately of 10^{16} G, as the high-resolution LES. Interestingly, this value is almost identical to the one achieved by the standard high resolution simulation, suggesting that the magnetic field already converged also in this case. Unfortunately, the computational cost of standard simulation with even higher resolution prevented us of performing additional tests to confirm this result. By using LES with the gradient model, the simulations are apparently able to capture most of the effects of the small-scale, unresolved dynamics during the turbulent stage. Note that even with the LES, high resolution and high-order numerical schemes are required in order to reach a faithful saturation level.

In the envelope, all the simulations reach similar values $\sim 5 \times 10^{14} - 10^{15}$ G at saturation. However, we stress that in most of the envelope the resolution is fixed and the SGS terms are disabled for all these cases. We recall that the

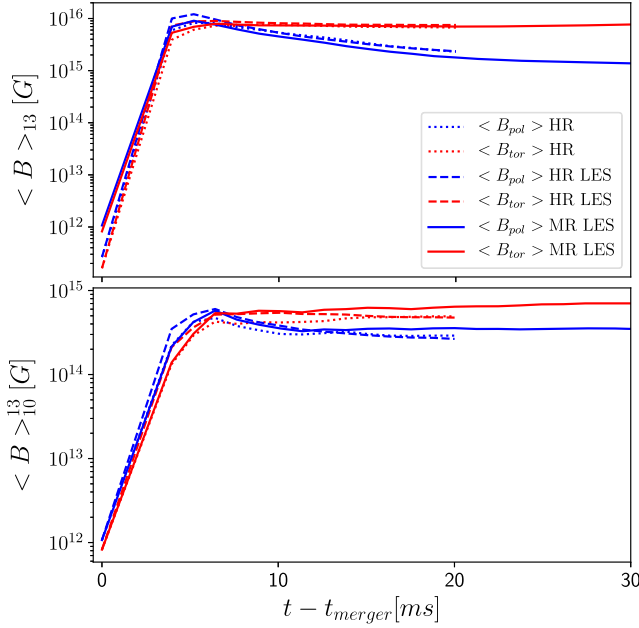


FIG. 6. Evolution of the average poloidal and toroidal magnetic field components. Contributions of the poloidal (blue) and toroidal (red) components to the magnetic field intensity, volume averaged in the bulk (top) or in the envelope (bottom), for the medium resolution LES and the high-resolution simulations (line styles).

focus of our study is to test the convergence of the magnetic field amplification within the bulk. The differences in the envelope are mainly caused by the differences within the bulk. We find that the latter is not causing large differences in the envelope. The aforementioned limitations (i.e., fixed resolution and no SGS terms) prevent us from drawing further conclusions about convergence of the magnetic field within the envelope, which may be subject of future studies.

As a side remark, we note that our results technically only apply to the use of SGS in conjunction with divergence cleaning, since we did not compare to other options such as vector potential evolution. We did however monitor the ratio between the magnetic field strength and the residual divergence, and observed little difference with and without SGS terms. We take this as an indication that there is no significant interaction between SGS and divergence cleaning terms.

In Fig. 6, we illustrate the poloidal and the toroidal contributions to the average magnetic field, for the high-resolution simulations and the medium resolution LES. First, note that these three simulations approach the same solution, which shows that the numerical dissipation does not dominate the dynamics, and demonstrates that solution obtained with medium-resolution LES is already a good approximation to the high-resolution one. During the kinematic phase, i.e., while the magnetic field's feedback on the fluid is dynamically irrelevant, both components grow exponentially at a similar rate. This is a strong indication that such amplification is due to small-scale

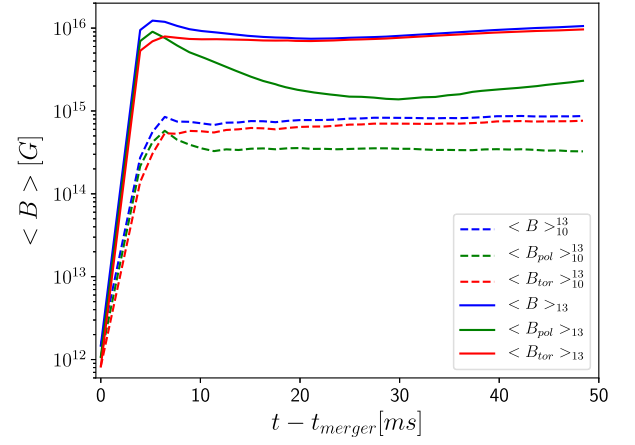


FIG. 7. Evolution of the average magnetic field (and components) in long timescales. Averaged magnetic field intensity and its components, considering the bulk (solid) or the envelope (dashes), for the medium resolution LES. After the amplification growth, both components are comparable, the expected outcome for the saturation state in isotropic turbulence. The poloidal component decreases until $t \sim 30$ ms while the toroidal one remains constant. At later times, both components grow linearly (i.e., the toroidal component growth 2 times faster than the poloidal one), probably due to the winding mechanism.

turbulent dynamo induced by the KHI (and possibly the RTI), which is naturally isotropic, providing amplified magnetic fields in random directions. This stage ends when the magnetic fields are strong enough to backreact significantly on the fluid, leading to a quasistationary state (in average) at saturation. During this last stage, the toroidal magnetic field, averaged in the bulk, remains roughly constant at values $\sim 10^{16}$ G until 20 ms, and then it starts to grow linearly. The poloidal component, however, decreases almost by an order of magnitude until 30 ms. This qualitative behavior is also reproduced in the envelope, although the difference between both components is less significant (i.e., just a factor of a few) in that region.

After validating the medium resolution accuracy via comparisons between resolutions, we have continued the medium-resolution LES up to timescales much longer than feasible with the high resolution. The total averaged magnetic field and its components are displayed in Fig. 7 up to 50 ms, showing the main features described before. After 30 ms, the poloidal component also grows within the bulk. Although there can be a partial contribution from the MRI, the linear growth in both magnetic field components strongly suggest that it can be mostly attributed to the winding mechanism, acting more efficiently in the spherical-shaped region of strong differential rotation. Interestingly, the toroidal component grows at a rate 2 times faster than the poloidal one.

As a complementary perspective, Fig. 8 shows the (cylindrical) radial profiles of the toroidal and poloidal components of the magnetic field, averaged on cylinder

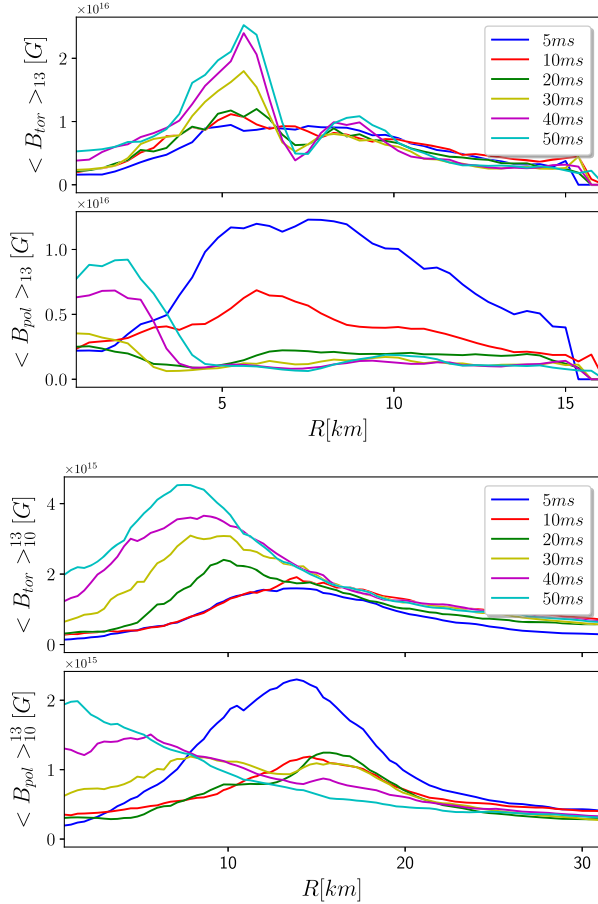


FIG. 8. Evolution of the (cylindrical) radial distribution of the magnetic field components. The toroidal and poloidal components of the magnetic field, averaged at different cylindrical surfaces R either in the bulk (top) or in the envelope (bottom), for the medium-resolution LES. At later times, both components grow in regions $R \lesssim 6$ km in the bulk and $R \lesssim 15$ km in the envelope.

surfaces (i.e., in the azimuthal and vertical directions), at different times. Again, we perform these averages separately in the bulk and in the envelope. As it was observed in the volume average, both components grow in a broad spatial region to values $\mathcal{O}(10^{16})$ G in the bulk and $\mathcal{O}(10^{15})$ G in the envelope during the first 5 ms after the merger, likely due to the KHI amplification and the fluid mixing of the turbulent state. Then, in the next 15 ms, the poloidal component decreases and get flattened, while that the toroidal component remains almost unaltered. In the following 30 ms, there is a growth of the toroidal component in the bulk around $R \sim 6$ km and in the envelope around $R \sim 10$ km. This roughly linear growth is followed, with a time delay of approximately 10 ms, by a similar one of the poloidal component in the interior of the peak developed by the toroidal component.

Note that the magnetic field amplification occurs in regions where MRI cannot be excited because $d\Omega/dR > 0$. These two features strongly suggest that this growth is

indeed produced by the winding mechanism, acting near the transition between the bulk and the envelope, where the differential rotation displays a maximum. By combining the profiles from both components is clear that the magnetic field is evolving towards a helical configuration similar to those present in magnetically dominated jets.

D. Spectral distribution

A more comprehensive information of the energy distribution over the spatial scales can be obtained from the power spectrum. The kinetic and magnetic spectra [Eqs. (12) and (13)] for the high resolution simulations and the medium-resolution LES are displayed in Fig. 9 at times $t = (5, 10, 20)$ ms. Here, we can observe some of the features described before, like the isotropic turbulent state driven by the KHI that produces a similar spectra of the poloidal and toroidal components at 5 ms. The magnetic energy approaches equipartition with the kinetic one at high wave numbers k .²

The kinetic spectra are well represented by the Kolmogorov power law $k^{-5/3}$, the typical direct cascade of isotropic kinetic turbulence. The magnetic field at low wave numbers follow the Kazantsev power law $k^{3/2}$, as expected for nonsaturated small-scale turbulent MHD dynamo. At later time, the overall poloidal spectra decrease slightly, as we already noticed in the averages described previously. The spectra of the toroidal component increase, with a clear transfer from large wave numbers to small ones (i.e., from small to large scales), indicating the presence of an inverse energy cascade. It is very important to stress that, already in these short timescales, the peak of the magnetic field spectra moves to lower wave numbers. The fact that the toroidal component is the most affected indicates again that the winding is probably the responsible for this energy transfer.

We have followed the evolution of the kinetic and magnetic spectra at later times for the medium resolution simulations with and without SGS terms, as shown in Fig. 10. Even on longer timescales up to 50 ms, the kinetic energy spectra remains mostly unchanged for both simulations. However, there are significant differences in the magnetic spectra. In the medium-resolution LES, the peak of the magnetic energy spectra moves from high to intermediate wave numbers (i.e., from small to intermediate spatial scales). The magnetic energy distribution, as time progresses, maintains roughly the Kazantsev power law on large scales and the Kolmogorov power law at small ones.

We also calculate, for each case, the spectra-weighted average wave number $\bar{k}$ and its associated length scale

²Note that at the highest wave numbers, spectra are damped by the numerical dissipation of the HRSC numerical scheme. In that region, there is also a pileup of magnetic energy due to the nonperiodic boundary conditions of the domain where the spectra are calculated.

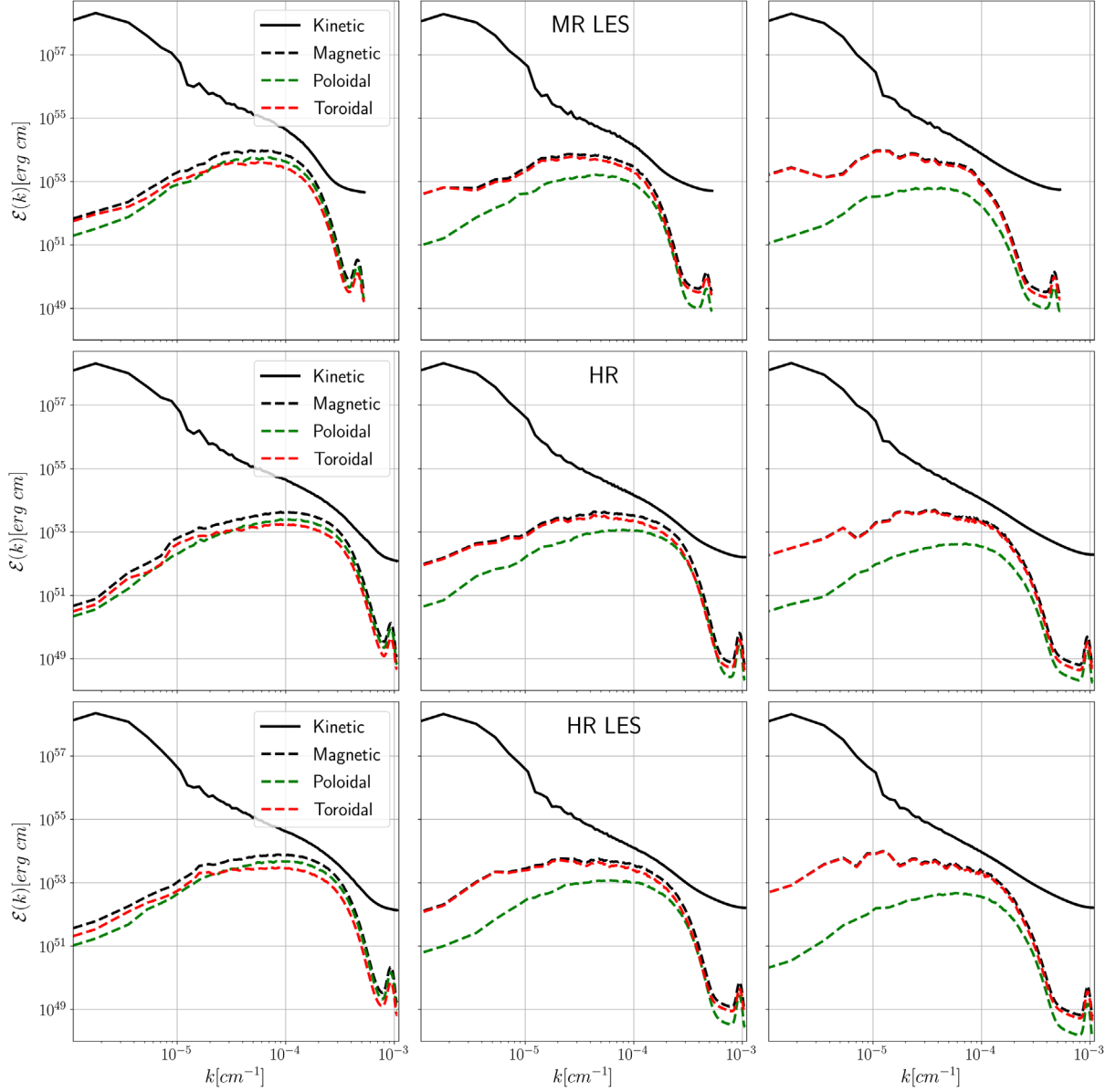


FIG. 9. *Evolution of the energy spectra.* Spectra of the kinetic (solid) and magnetic energy (dashed) at $t = (5, 10, 20)$ ms, for the medium resolution LES and the high-resolution simulations. The kinetic and magnetic energies almost reach equipartition at high wave numbers (i.e., before the decay induced by numerical dissipation, which is much more prominent in the magnetic spectra). Note that the high-resolution simulations agrees very well with the medium resolution LES. We caution that the power at low wave numbers is based only on few points in discrete 3D Fourier space and corresponds to a small fraction of the total energy. Therefore, it might be subject to stronger fluctuations.

$\delta R = 2\pi/\bar{k}$, which roughly represents the distance at which the field is not randomly oriented but tends to show a defined direction. For the medium resolution LES, δR of the magnetic energy moves from 0.7 km to 2 km during the 50 ms of the simulation. On the other hand, δR of the kinetic energy varies only from 12 km to 17 km. The standard medium resolution simulation share roughly the same qualitative behavior, but with a magnetic energy spectra much more flattened and many orders of magnitude smaller.

E. Differential rotation and relevant profiles near the rotation axis

Here we turn our attention to a more detailed analysis of the differential rotation profile present in the remnant, comparing the simulations with the same medium resolution, standard, and LES. In order to disentangle the effects from the magnetic field, we also performed a standard simulation with no magnetic field. The radial profiles of density $\rho(R)$ and angular velocity $\Omega(R)$, for two different times $t = (10, 50)$ ms after merger, are displayed

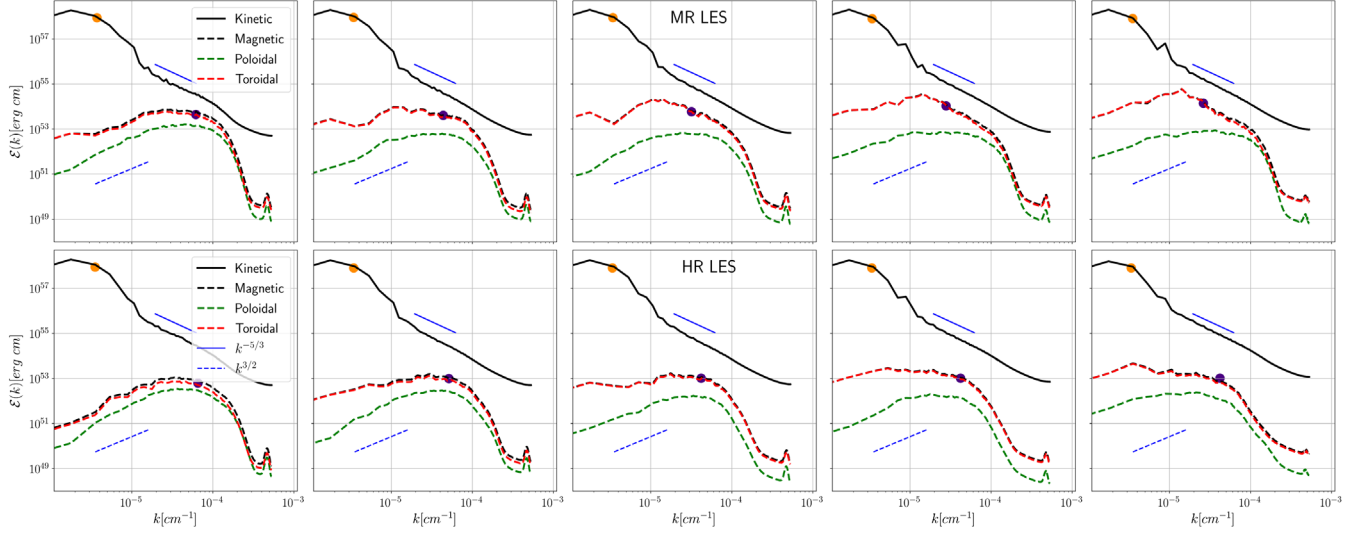


FIG. 10. *Evolution of the energy spectra at late times.* Kinetic and magnetic spectra for the medium resolution cases at $t = (10, 20, 30, 40, 50)$ ms. The standard medium resolution simulation is only qualitatively similar to the medium resolution LES. As expected in turbulence with low magnetization, at $t = 10$ ms, the kinetic energy spectra show the standard Kolmogorov power law $k^{-5/3}$ (short solid blue line) in the inertial range, while the magnetic energy follows the Kazantsev power law $k^{3/2}$ (short dashed blue line) at low wave numbers. At late times, the magnetic energy spectra follow the Kolmogorov slope at intermediate and high wave numbers. The weighted-average wave numbers $\bar{k}$ are represented by orange and black dots, corresponding to the typical coherent scales of fluid and magnetic structures.

in Fig. 11. These profiles are extracted by computing the azimuthal averages within the orbital plane (i.e., along a circle in the $z = 0$ plane). The first observation is that the density profile barely changes after the remnant has settled down into a roughly axisymmetric shape. The differences between the three different simulations are minor, indicating that magnetic field effects on the density profile are rather small. The angular velocity, at 10 ms postmerger, shows in all three cases a radial profile with values $\approx 6000 \text{ rad s}^{-1}$ near the orbital axis, increasing up to $\approx 10000 \text{ rad s}^{-1}$ at $R \approx 7.5 \text{ km}$. At larger distances it decreases, with falloff behavior approaching that of Keplerian profiles (represented for comparison with a green dashed line in the plot). As time evolves, the profiles get more flattened, with the maximum $\Omega(R)$ decreasing to $\approx 8500 \text{ rad s}^{-1}$ at 50 ms postmerger. Comparing the three cases, we find that the amplified magnetic fields do not seem to have a significant impact on the removal of differential rotation.

In order to monitor the formation of magnetically dominated regions, we use the averages of β^{-1} , which estimate the relative importance of the magnetic pressure with respect to the fluid pressure. Figure 12 shows the volume averages in the bulk and in the envelope, for the high-resolution and the medium-resolution LES. On average, the magnetic pressure reaches about 1% of the fluid pressure within the bulk, and 10 times less within the envelope. Again, the high-resolution simulations show a very similar behavior.

We also calculate the averages of this quantity over cylindrical surfaces, as a function of time, to better

understand the dynamical evolution. The field β^{-1} averaged in the bulk, shown in the top panel of Fig. 13, reaches a peak at $t = 5 \text{ ms}$ after the merger in the region $R \sim 11 \text{ km}$. As time progresses, the profile gets flattened, however, decreasing by almost an order of magnitude. This is probably related to the decrease of the poloidal magnetic

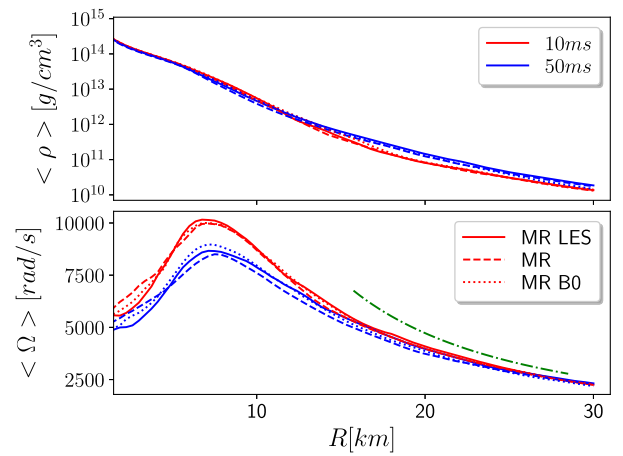


FIG. 11. *Evolution of the radial distribution of density and angular velocity.* Profile of the density and Ω in the orbital plane, averaged over the azimuthal direction. Two different times (colors), $t = (10, 50) \text{ ms}$ are represented for the medium resolution LES (solid) and the standard simulation (dashed). We also include the nonmagnetized case MR B0 (dotted) and show the falloff behavior (green) $\Omega_K \sim R^{-3/2}$ of Keplerian disks for comparison.

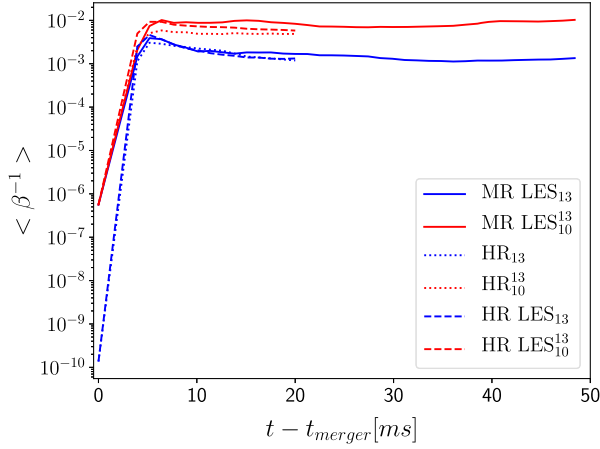


FIG. 12. *Evolution of the inverse of plasma beta.* Volume-averaged inverse of plasma beta, $\langle \beta^{-1} \rangle = \langle B^2 / (2P) \rangle$, within the bulk and within the envelope, for the medium resolution LES and the high-resolution simulations.

field, due to rotation, once the saturation stage is achieved. Interestingly, the magnetic pressure becomes more relevant at later times in the envelope. At $t = 5$ ms, there is a broad distribution with $\beta^{-1} \sim 0.01$, almost flat for $R \sim 11$ km, but monotonically decreasing to zero at smaller radii. At $t = 30$ ms after the merger, a bump appears in the profile around $R \sim 11$ km. Although the peak of this bump is only a factor of 2 larger than the value in the flat region, it evolves towards smaller radii, increasing significantly the relevance of magnetic pressure near the z axis. This is another indication that magnetic field is growing near the rotation axis of the remnant.

Near the rotation axis there are additional effects which might actually prevent the formation of magnetically dominated structures. Figure 14 displays the density in a meridional plane for the three medium resolution simulations: LES, standard, and without magnetic field. There is a clear trend; the larger the magnetic field, the more dense is the region near the rotation axis. This effect can be quantified by computing the mass distribution in a solid angle of 15° near the axis, as a function of the distance from the center, as it is displayed in Fig. 15. Despite starting from a similar distribution at $t = 5$ ms after the merger, the mass distribution in the envelope increases faster for stronger magnetic fields, leading to a difference of approximately a factor of 3 between the medium resolution LES and the nonmagnetized simulation. This enhanced baryon contamination near the z -axis due to magnetic fields makes the possible emergence of a jet less likely [40,41].

F. Gravitational waves and ejecta

Finally, we discuss some aspects related to matter ejection and GW emission by the remnant. Ejected matter can be split in two categories. The dynamical ejecta are launched during merger, as a result of tidal interactions and

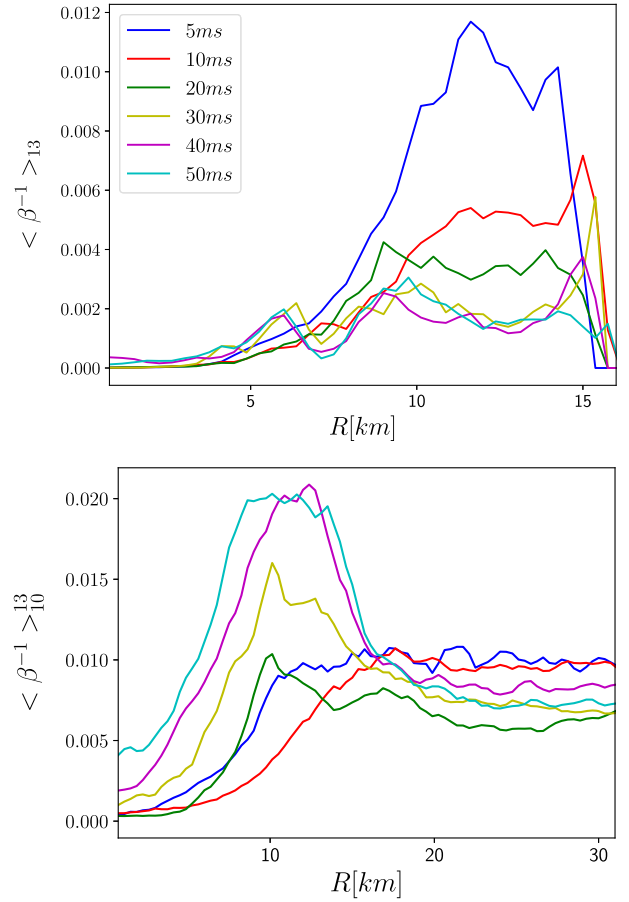


FIG. 13. *Evolution of the radial distribution of β^{-1} .* The profile of the inverse of beta, averaged at different cylindrical surfaces R either in the bulk (top) or in the envelope (bottom), for the medium-resolution LES. At later times, the magnetic pressure becomes more relevant in the envelope for $R \leq 15$ km.

shocks formed in the neutron stars. Perturbations of the remnant can also liberate matter within tens of milliseconds after merger. The secular ejecta are emitted from the outer layers of the remnant on longer timescales by effects such as effective magnetic viscosity, magnetic pressure, neutrino radiation, or nuclear heating. The flux of unbound mass observed at different distances is shown in the top panel of Fig. 16. By integrating this flux in time, we obtain an estimate for the total ejected mass $M_{ej} \approx 0.025 M_\odot$. As one can see, the ejecta in our simulations are dynamical, whereas the secular ejecta contribution is negligible. However, a further substantial mass outflow may be expected at later times. In Ref. [85], the authors studied the magnetically driven baryon-loaded wind launched in the postmerger for a similar BNS model (although with much lower resolution), finding a massive outflow emerging around the time of saturation of the magnetic energy growth (≈ 50 ms) and lasting up to 200 ms. We also note that the mass outflow may be partially hampered by the braking effect of the floor density in the atmosphere.

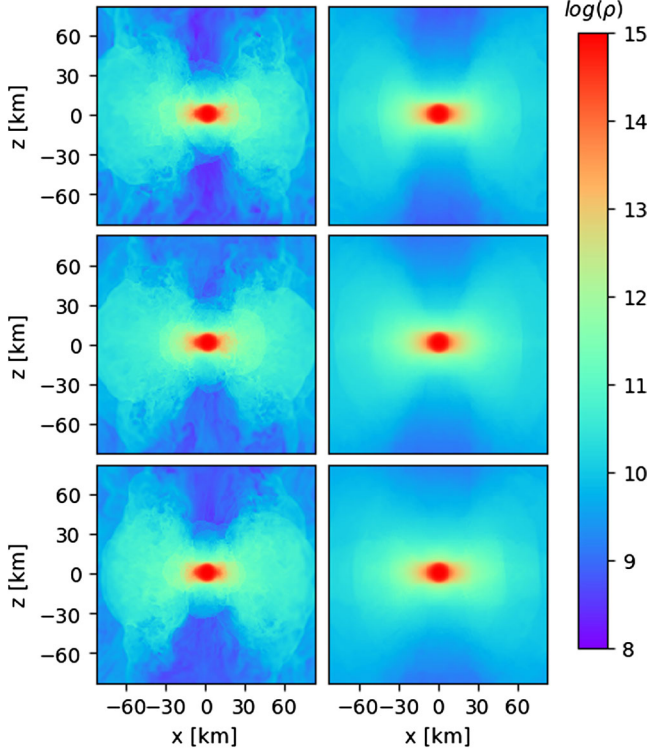


FIG. 14. *Density in a meridional plane.* Density at $t = 5$ ms (left panels) and 50 ms (right) after the merger, for the medium resolution simulations: (top) without magnetic field, (middle) standard simulation, and (bottom) LES including the SGS terms. Clearly, stronger magnetic fields increase the matter contamination of the funnel region near the orbital axis.

To assess the error caused by extraction at finite radii, we compare the total ejected mass for three different radii. The differences obtained are smaller than 3% of the total value.

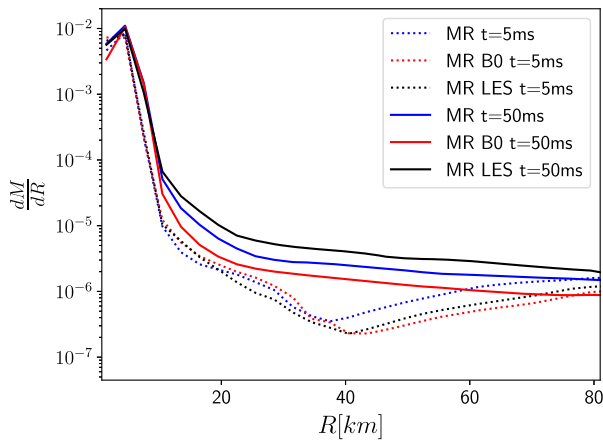


FIG. 15. *Distribution of density in a solid angle near the axis.* The mass contained in a solid angle of 15° around the z axis, for the medium resolutions at $t = 5$ ms and $t = 50$ ms after the merger. This plot represents how the radial distribution of the mass increases with the magnetic field.

The dominant gravitational wave component is displayed in the bottom panel of Fig. 16 for the medium resolution LES. To assess the error due to finite extraction radius, we show the signal calculated at three different extraction radii, demonstrating good agreement. During the first 15 ms, the gravitational wave signal exhibits a rich structure typical for merger remnants, with strongly varying frequency and amplitude. As the remnant settles down, the signal relaxes to a simple decaying oscillatory function. At the end of our simulation, at $t = 50$ ms, the signal is almost zero.

The merger of an equal-mass binary leads naturally to a quadrupole (i.e., $m = 2$) deformation in the mass distribution of the remnant. As it has been found in previous works (see, e.g., Refs. [86–89]), a nonaxisymmetric instability induces a $m = 1$ mode, which develops soon after the merger, and at late times, it might dominate over the $m = 2$ one. The claim in those works is that this $m = 1$ mode induces a strong spiral arm in the remnant, which transports angular momentum and contributes to unbind the outer layers of the envelope. One way to analyze the impact of the magnetic fields on the development of this spiral mode is by comparing the $m = 1$ mode of the gravitational waves, displayed in the top panel of Fig. 17 for all the medium resolution simulations, either magnetized or unmagnetized. No significant differences are observed in the postmerger signal for the $m = 1$ mode and only moderate ones in the $m = 2$ mode. We can conclude that no significant effects are introduced by the magnetic fields on these spiral modes in these timescales, probably because these magnetic fields are not organized yet in large-scale structures.

Finally, one might ask if the presence of strong magnetic fields changes other observable features of the gravitational

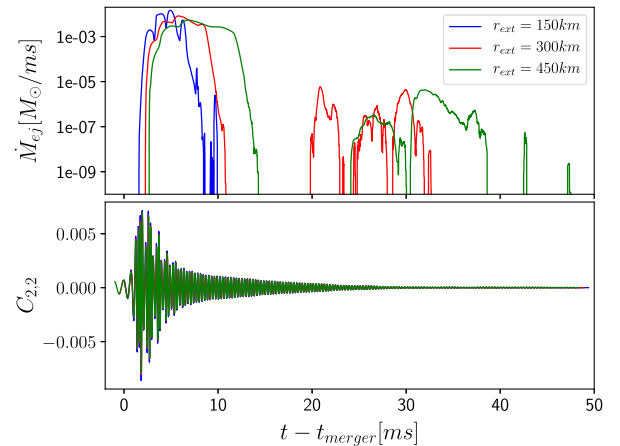


FIG. 16. *Unbound mass flux and gravitational waveform at different extraction surfaces.* Flux of unbound mass (top) and dominant mode (i.e., $l = m = 2$) of the Newman-Penrose Ψ_4 (bottom), as a function of time. Both quantities are computed at the three spherical surfaces located at $r_{\text{ext}} = (150, 300, 450)$ km.

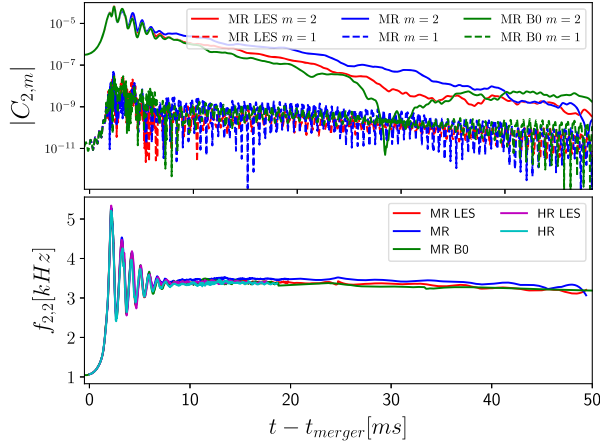


FIG. 17. *Evolution of gravitational wave modes.* Top: The module $|C_{l=2,m}|$ of the Ψ_4 modes $m = 1$ and $m = 2$, for the medium resolution simulations. The $m = 1$ mode is persistent for all the cases (i.e., LES vs no LES, and magnetized vs unmagnetized). Bottom: Instantaneous frequency of the $l = m = 2$ gravitational wave mode for the medium and the high-resolution simulations.

waves. The amplitudes and instantaneous frequencies of the GW main mode (i.e., $l = m = 2$) are displayed in Fig. 17, for all the medium and high resolution simulations. The amplitudes of the unmagnetized and the LES cases matches very well, with a slightly larger deviation of the standard simulation. In the frequencies, only a very small shift is observed in the medium resolution standard simulation with respect to the unmagnetized and to the magnetized LES, confirming that the effect of magnetic fields on these timescales is rather small.

V. DISCUSSION

The combination of high-order numerical schemes, high-resolution and LES techniques with the gradient SGS model, allow us to describe accurately small-scale dynamo effects in magnetized neutron star mergers. Our simulations demonstrate that the numerical methods are able to capture the magnetic field amplification within the bulk of the remnant, and the corresponding final saturation level. These results suggest that LES, combined with the gradient SGS model, can be interpreted as a method to increase the effective resolution of the simulations by at least a factor of 2 (and possibly higher). In our scenario, SGS allows us to achieve numerical convergence for moderately high resolutions that are still within our reach, in contrast to the standard scheme. Let us also note that, although our numerical setup is not suitable to investigate the convergence in the low density envelope, the results in the bulk are encouraging, and we expect benefits also in this regime.

We have considered magnetized neutron stars with realistic magnetic field strength of 10^{11} G, an intensity small enough not to alter the topology of the remnant's

amplified field. These values represent a tiny fraction of the total energy of the system and are much smaller than commonly used in numerical simulations.

Our simulations show that, shortly after the merger, the main magnetic field amplification process is the KHI. A shear layer between the stars, at the time of contact, is prone to unstable modes that develop vortexes at all scales. The RTI might also act in the outer regions of the stars in even shorter timescales, contributing to the development of turbulence. However, it is hard to distinguish such contribution from the rest of the rich dynamics. Then, small-scale dynamo effects driven by these two instabilities amplifies the magnetic field, that is redistributed throughout the remnant by the fluid flow. A turbulent, quasistationary state, is achieved after approximately 5 ms. The average magnetic field strength at the saturation phase is approximately 10^{16} G. As expected from an isotropic turbulence, the poloidal and toroidal components of the magnetic field are comparable at saturation. At later times, the magnetic field grows linearly due to the winding mechanism, reaching at $t = 50$ ms magnetic energies of 2×10^{50} ergs (and still growing). Such a magnetic energy value should be considered as a lower bound for the magnetization level reached after BNS mergers with sufficiently long-lived remnant.

This behavior can also be observed in the spectra, which shows also that the magnetic spectrum density almost reaches a equipartition with the kinetic one in the small scales. The kinetic energy spectra follow the expected Kolmogorov power law $k^{-5/3}$ in the inertial range, while that the typical structure scale of 12 km. On the other hand, the magnetic energy spectra display the expected Kazantsev power law $k^{3/2}$ for large scales, but the typical coherent size is much smaller, $\delta R \sim 700$ m. During the 50 ms after the merger covered by our longest simulations, the kinetic energy spectra remains mainly unchanged. However, the distribution of the magnetic energy spectra shifts to larger scales, keeping the Kazantsev power law for small wave numbers but switching to the Kolmogorov power law for intermediate ones. This change in the distribution is very interesting for several reasons: (i) it indicates the presence of an inverse cascade, with magnetic energy being transferred from small to large scales, (ii) the typical scale of the structures of the magnetic field energy moves from $\delta R \sim 700$ m to larger scales of $\delta R \sim 2$ km and (iii) the magnetic energy spectra mimics the kinetic one (i.e., not far from a Kolmogorov power law) at small scales.

These larger magnetic structures can be observed also in the averaged (cylindrical) radial distribution. They show that the toroidal component remains constant during the first 20 ms, but then it start to grow by a factor of a few in the region near the angular velocity peak. The poloidal component, on the other side, decrease initially during the first 20 ms, but then started to grow in the inner region ≤ 10 km. We believe that the winding is responsible for the

growth of the toroidal and poloidal magnetic fields, in combination with small-scale dynamo processes.

It is important to stress that we observe no significant redistribution of the differential rotation in the first 50 ms after the merger. This is in agreement with the fact that the MRI is apparently not operating in our simulations. Both things might be explained by the small-scale, randomly oriented structure of the magnetic field during turbulence: the effective Alfvén velocity is reduced by a large factor, which depends on the typical sizes δR where the mean magnetic field has a well-defined direction and within which the angular momentum is effectively transported. More fundamentally, since the KHI-triggered magnetic field is turbulent and very dynamical, there is no static, large-scale background field over which one can define an unstable perturbation like the MRI. Our expectation is that, as large-scale magnetic fields develop, they can become more efficient on redistributing angular momentum from the bulk to the outer envelope. This could happen via MRI if, at later stages, the magnetic field could acquire a topology clearly dominated by almost stationary large scales in the region where the angular velocity decreases with radius.

We want to emphasize that, despite our encouraging results about the convergence in the bulk, further studies are needed in order to fully understand the impact of magnetic fields on the remnant’s dynamic. Further convergence tests,

where the SGS terms are active also in the envelope and where the resolution in the latter is not kept fixed, will be needed to ascertain whether the method can capture the small-scale MHD processes occurring in all of the remnant and follow their development until, ultimately, the possible formation of a magnetically dominated jet.

ACKNOWLEDGMENTS

This work was supported by European Union FEDER funds, the Ministry of Science, Innovation and Universities and the Spanish Agencia Estatal de Investigación Grant No. PID2019–110301 GB-I00. R. C. acknowledges support from the Project No. PRIN-INAF 2019 “Short gamma-ray burst jets from binary neutron star mergers.” JVK kindly acknowledges the CARIPARO Foundation for funding his Ph.D. fellowship within the Ph.D. School in Physics at the University of Padova. DV is funded by the European Research Council (ERC) Starting Grant IMAGINE (Grant Agreement No. [948582]) under the European Union’s Horizon 2020 research and innovation programme. The authors thankfully acknowledge the computer resources at MareNostrum and the technical support provided by Barcelona Supercomputing Center (BSC) through Grant project Long-LEBNS by the 22th PRACE regular call (Proposal No. 2019215177, P. I. CP and DV).

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