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No evidence for an Eddington-ratio dependence of X-ray weakness in BALQSOs

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ABSTRACT

Several works have studied the relation between X-ray, ultraviolet (UV), and wind properties in broad absorption line quasars (BALQSOs), generally concluding that the formation of strong winds is tightly connected with the suppression of the ionizing extreme ultraviolet (EUV)/X-ray emission. The Eddington ratio (λ_{Edd}), which measures the accretion rate, is also known to be related with outflow and emission-line properties in the general quasar population. Moreover, models describing quasar accretion depend on λ_{Edd} , which can thus possibly affect the relative production of accelerating UV and ionizing EUV/X-ray radiation. In this work, for the first time, we investigated whether BALQSO X-ray properties are related with the Eddington ratio. We selected a sample of 30 BALQSOs with accurate measurements of black-hole mass and BAL properties from the literature, and we complemented it with four additional BALQSOs we observed with *XMM-Newton* to populate the low and high Eddington-ratio regimes. We did not find evidence for a strong relation between λ_{Edd} and X-ray suppression, which however shows a significant correlation with the strength of the UV absorption features. These findings are confirmed also by considering a sample of mini-BALQSOs collected from the literature.

Key words: methods: data analysis – galaxies: active – galaxies: nuclei – quasars: absorption lines – X-rays: galaxies.

1 INTRODUCTION

One of the most outstanding pieces of evidence for the existence of active galactic nucleus-driven outflows is the typical broad ($> 2000 \text{ km s}^{-1}$) absorption features visible in the ultraviolet (UV) spectra of broad absorption line quasars (BALQSOs), which account for ~ 15 per cent of optically selected quasars (QSOs) (e.g. Trump et al. 2006; Gibson et al. 2009a). Such absorption features often have complex structures and are blueshifted with respect to the rest-frame line wavelength, implying outflowing velocities up to $\sim 0.2c$ (e.g. Rogerson et al. 2016). Less-extreme features (1000–2000 km s^{-1} in width) are present in optical/UV spectra of the so-called mini-BALQSOs, whose number is comparable to or even greater than the number of BALQSOs, demonstrating the widespread presence of outflows among the whole quasar population (e.g. Ganguly & Brotherton 2008).

The origin of such outflows is thought to be connected to the formation of equatorial winds radiatively driven by UV-line pressure, launched from the accretion disc at $\sim 10^{16-17} \text{ cm}$ (e.g. Proga, Stone & Kallman 2000). The ‘accretion-disc-wind’ model requires the outflowing material not to be overionized, as the line-driving efficiency drops when the ionization state of the wind is too high. Several hypotheses have been proposed to avoid such overionization, spanning from the presence of shielding material (perhaps a failed wind; e.g. Proga & Kallman 2004) located at the base of the wind that absorbs the EUV/X-ray radiation emitted from the inner regions of the disc, to a high density of the wind itself due to radiation-pressure confinement (e.g. Baskin, Laor & Stern 2014), to occasional *intrinsic* (i.e. not due to absorption) EUV/X-ray weakness (e.g. Luo et al. 2013, 2014), as predicted by some accretion models during phases of fast accretion (e.g. Meier 2012; Jiang, Stone & Davis 2018, and references therein).

Some of these scenarios predict an observed X-ray weakness (i.e. a weaker observed X-ray emission than the level expected from the UV luminosity), estimated with the $\Delta\alpha_{\text{ox}} =$

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$\alpha_{ox}(\text{observed}) - \alpha_{ox}(L_{2500\text{\AA}})$ parameter, where $\alpha_{ox}(\text{observed}) = 0.3838 \times \text{Log}(L_{2\text{keV}}/L_{2500\text{\AA}})$ is the slope of a power law connecting the UV at 2500 Å and the observed X-ray at 2 keV. The value of α_{ox} has been found to correlate with $L_{2500\text{\AA}}$ (e.g. Vignali, Brandt & Schneider 2003; Strateva et al. 2005; Steffen et al. 2006, Just et al. 2007; Lusso et al. 2010) up to $z \approx 6$ (Nanni et al. 2017), and $\alpha_{ox}(L_{2500\text{\AA}})$ is thus the expected value inferred from the UV luminosity. The quantity $\Delta\alpha_{ox}$ therefore quantifies the deviation of the observed X-ray luminosity with respect to the expectation.

Indeed, BALQSOs have been generally found to be X-ray weak by up to a factor of ~ 100 ($\Delta\alpha_{ox} \sim -0.75$; e.g. Gibson et al. 2009a). To discriminate absorption from *intrinsic* X-ray weakness as the cause of the *observed* X-ray weakness, emission in rest-frame hard X-rays, which are not affected by low-to-moderate column densities of absorbing material, must be studied. For instance, Luo et al. (2014), using *NuSTAR* data, found a significant fraction of intrinsically X-ray weak BALQSOs in their local sample. Other authors (e.g. Gallagher et al. 2006; Morabito et al. 2014; Liu et al. 2018) accessed high rest-frame energies using samples of high-redshift ($1.4 < z < 2.9$) BALQSOs observed with either *Chandra* or *XMM-Newton*. In particular, Morabito et al. (2014) estimated an average intrinsic X-ray weakness of a factor of ≈ 3 ($\Delta\alpha_{ox} \approx -0.2$). Recently, Liu et al. (2018) found a fraction of intrinsically X-ray weak BALQSOs of $\approx 6 - 23$ per cent among their $z = 1.6 - 2.7$ sample, significantly higher than the $\lesssim 2$ per cent fraction of X-ray weak quasars among the general non-BALQSO population (e.g. Gibson, Brandt & Schneider 2008). However, results based on X-ray spectral analysis in many cases reveal the presence of X-ray absorption (e.g. Gallagher et al. 2002; Grupe, Mathur & Elvis 2003; Shemmer et al. 2005; Giustini, Cappi & Vignali 2008). A number of correlations are known between the X-ray weakness and other observational properties of BALQSOs, such as the minimum and maximum velocity of the outflow, and the strength of the absorption features (e.g. Gallagher et al. 2006; Fan et al. 2009; Gibson et al. 2009a; Wu et al. 2010), suggesting that the level of X-ray emission indeed has material effects in shaping the wind observed in the UV.

BALQSOs are generally thought to be powered by fast-accreting SMBHs (e.g. Boroson 2002; Meier 2012), where the accretion rate is measured through the Eddington ratio, defined as $\lambda_{\text{Edd}} = L_{\text{bol}}/L_{\text{Edd}}$, where $L_{\text{Edd}} = 1.26 \times 10^{38} M_{\text{BH}}/M_{\odot} \text{ erg s}^{-1}$. In fact, while BALQSOs have been found to have λ_{Edd} as low as ≈ 0.1 , the fraction of quasars showing BAL features increases with λ_{Edd} (Ganguly et al. 2007). However, as the accretion rate increases, a larger amount of ionizing EUV radiation is produced according to standard accretion models (e.g. Shakura & Sunyaev 1973). One possibility to avoid overionization of the outflowing material in fast-accreting BALQSOs (i.e. $\lambda_{\text{Edd}} \approx 1$) is that suppression (either intrinsic or due to absorption) of the EUV-to-X-ray emission, responsible for ionization, depends on the Eddington ratio. In this case, one may expect an anticorrelation between $\Delta\alpha_{ox}$ and λ_{Edd} , i.e. a change of the typical observed (and perhaps intrinsic) spectral shape of BALQSOs approaching the Eddington limit. Hints for such a scenario have been derived by, e.g. Lusso et al. (2010, 2012) by studying the dependence of α_{ox} and the quasar bolometric correction on λ_{Edd} (but see also, e.g. Plotkin et al. 2016). From a theoretical point of view, the Shakura & Sunyaev (1973) accretion mode cannot be in place for Eddington ratios exceeding or even approaching unity. Several models have been proposed to describe Eddington-limited accretion flows, some of which predict an intrinsic suppression of X-ray photon production (e.g. Meier 2012; Jiang et al. 2018, and references

therein; but see also, e.g. Castelló-Mor et al. 2017). We additionally note that the UV part of quasar SEDs, which is responsible for line-pressure acceleration, may also depend on the accretion rate. Increased UV line pressure may compete against EUV/X-ray ionization in the shaping of quasar wind properties (e.g. Krucek et al. 2011; Richards et al. 2011), although no significant evidence for a strong variation of the optical/UV part of quasar SEDs for different regimes of λ_{Edd} has been derived observationally (e.g. Scott & Stewart 2014).

The Eddington ratio is considered one of the fundamental parameters driving observable quasar properties (e.g. Shen & Ho 2014), and it is indeed closely related with the quasar ‘Eigenvector 1’ (e.g. Boroson & Green 1992), i.e. a preferred direction in the quasar multidimensional parameter space along which quasar emission-line properties are aligned. BALQSOs appear to follow the same relations with λ_{Edd} as the overall quasar population (e.g. Yuan & Wills 2003). Moreover, outflow properties (e.g. velocity) in quasars (e.g. Marziani & Sulentic 2012) and, in particular, BALQSOs (e.g. Ganguly et al. 2007) have been found to correlate with λ_{Edd} . However, a possible dependence of the X-ray properties of BALQSOs on accretion rate has never been investigated. In this work, we made use of both archival and proposed X-ray observations of a sample of 34 high-redshift ($1.5 \lesssim z \lesssim 2.2$) SDSS BALQSOs with accurate measurements of black-hole mass to study the dependence of the *observed* X-ray weakness on Eddington ratio. We used an $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.3$, and $\Omega_{\Lambda} = 0.7$ Λ CDM cosmology.

2 SAMPLE SELECTION AND ANALYSIS

The goal of this work is to study the observed X-ray emission level relative to the UV luminosity, in terms of $\Delta\alpha_{ox}$, as a function of λ_{Edd} for a sample of high-redshift BALQSOs, where the redshift range ($1.5 \lesssim z \lesssim 2.2$) was chosen such that both the Mg II and C IV emission lines are included in the SDSS spectral coverage, the former to derive SMBH masses, and the latter to detect the BAL features. By imposing quality cuts on the signal-to-noise ratio (SNR) of the observed SDSS spectra, we limited our study to those objects with securely identified BAL features (i.e. which cannot be ascribed to noisy spectra) and accurate measurements of black-hole mass and BAL properties (e.g. absorption-line strength). In this section, we describe the sample of BALQSOs observed in the X-rays we collected from the literature, and the sample of four BALQSOs we observed with *XMM-Newton*.

2.1 Selection of the BALQSO sample from the literature

Fan et al. (2009), Gibson et al. (2009a), and Morabito et al. (2014) presented the X-ray properties of three samples of 41, 73, and 18 BALQSOs, respectively, for a total of 108 unique objects, covered by *Chandra* or *XMM-Newton* observations. We matched them with the catalogue of virial black-hole masses and bolometric luminosities for SDSS DR7 QSOs of Shen et al. (2011). In order to study a homogeneous sample of objects, representative of the majority of the BALQSO population, and to avoid additional complexity due to different ionization properties of the outflowing material, we considered only objects flagged as high-ionization BALQSOs (HiBALQSOs), thus discarding nine objects classified as low-ionization BALQSOs (7) or even non-BALQSOs (2) in Shen et al. (2011) (who used more recent SDSS spectra than Gibson et al. 2009a; Fan et al. 2009; Shen et al. 2011).

Table 1. Summary of the number of X-ray sources collected from the literature surviving after each selection step (as described in Section 2.1), starting from the parent sample of 108 unique objects included in Fan et al. (2009), Gibson et al. (2009a), and Morabito et al. (2014).

Parent sample	108
HiBAL	99
Radio undetected	82
$\text{SNR}_{\text{C IV}} > 5$	72
Spectral coverage of Mg II	54
$\text{SNR}_{\text{Mg II}} > 5$ and $\chi^2_{\text{Mg II}} < 1.2$	30

The X-ray emission produced at the base of the jets in radio-detected QSOs is known to be comparable to or even dominant over the disc/corona-linked X-ray emission (e.g. Miller et al. 2011), which is the physical mechanism of interest in this study. An additional X-ray contribution from the jets would thus artificially increase the observed X-ray flux/luminosity leading to biased estimates of α_{ox} and $\Delta\alpha_{\text{ox}}$. Disentangling the two contributions (corona versus jets) requires a careful spectral analysis, which is prevented by the small number (up to few tens, with a median number of counts of 7) of X-ray counts for the sources considered in this work. Excluding quasars detected in large-area radio surveys from our sample avoids this bias. We therefore discarded 15 radio sources detected in the FIRST radio catalogue (White et al. 1997), and 2 QSOs not covered by the FIRST survey, as flagged in Shen et al. (2011), resulting in a parent sample of 82 sources.

Spectral noise can sometimes mimic the absorption features affecting the C IV emission line used to define BALQSOs. In order to select a clean sample of BALQSOs, we imposed a quality cut on the SDSS spectra, requiring an SNR at wavelengths close to the C IV emission line of $\text{SNR}_{\text{C IV}} > 5$ (10 objects discarded). This requirement also ensures an accurate measurement of the balnicity index (BI; see Section 3), an indicator of the absorption strength, which we use later in the analysis together with the Eddington ratio to investigate the dependencies of the X-ray weakness.

The reliability of the Eddington-ratio estimates is strongly dependent on the accuracy of the measured black-hole mass. Single-epoch virial black-hole masses are usually estimated through scaling relations with the FWHM of the Balmer ($\text{H}\alpha$ and $\text{H}\beta$), Mg II, and C IV emission lines, in order of reliability (see the detailed discussion in Shen 2013; see also, e.g. Shen et al. 2011; Kozłowski 2017). The use of the Balmer emission-line series is precluded to us by the need for spectral coverage of the C IV line, necessary to detect the BAL features. The same absorption lines can affect strongly the shape of the C IV emission lines, and thus the measurement of the FWHM, preventing the use of the C IV emission line to estimate black-hole masses for our sample. We therefore use virial black-hole masses derived from the Mg II emission line consistently for all of our sample. The required simultaneous spectral coverage of the Mg II and C IV lines restricts the redshift range of this work to $1.5 \lesssim z \lesssim 2.2$, thus discarding an additional 18 BALQSOs for which Mg II-based black-hole masses are not available.

We finally impose quality cuts on the Mg II line detection ($\text{SNR}_{\text{Mg II}} > 5$) and fit ($\chi^2_{\text{Mg II}} < 1.2$) to include only sources with accurate measurements of black-hole mass, further restricting the sample to 30 BALQSOs. We report in Table 1 a summary of the number of sources surviving each of the selection steps, and in Table 2 the properties of the final 30 selected sources. Our conclusions below hold if more conservative quality cuts are applied (e.g. $\text{SNR}_{\text{C IV}} > 10$ and $\text{SNR}_{\text{Mg II}} > 10$), at the cost of greatly reducing the sample size, as discussed in Section 3.

We computed the monochromatic UV luminosities from the flux at (rest-frame) 2500 Å derived by Shen et al. (2011) through spectral fitting, and homogeneously applied the Steffen et al. (2006) calibration, considering $L_{2500\text{\AA}}$ as the independent variable:

$$\alpha_{\text{ox}} = -0.137 \times \log L_{2500\text{\AA}} + 2.638 \quad (1)$$

Steffen et al. (2006) derived $\alpha_{\text{ox}}(L_{2500\text{\AA}})$ for a sample of optically selected quasars. Since ours is an SDSS-selected sample, we preferred Steffen et al. (2006) over Lusso et al. (2010), who applied an X-ray selection. However, the two calibrations return almost exactly the same results for our sample. We also retrieved the observed luminosities at 2 keV ($L_{2\text{keV}}$) provided by the original works to compute $\alpha_{\text{ox}}(\text{observed})$.

Most of the selected BALQSOs are included in the Gibson et al. (2009a) sample, and a few of them are in common with either Fan et al. (2009) or Morabito et al. (2014). Two BALQSO are selected from the Fan et al. (2009) compilation only, while none is included in the Morabito et al. (2014) sample only (see the last column of Table 2). When X-ray luminosities for a quasar are provided by more than one author, we consistently assumed the value reported by Gibson et al. (2009a), from which the majority of the sample is selected. X-ray luminosities are not corrected for absorption. The general paucity of counts ($\lesssim 80$, with a median value of 7) prevents a detailed spectral analysis, which would be required to estimate with acceptable accuracy the intrinsic luminosities of these sources. In fact, complex absorption models (e.g. with ionized or partially covering absorption) may be suitable descriptions of BALQSO X-ray spectra (e.g. Gallagher et al. 2002), and cannot be well constrained with the available small number of counts.

Fig. 1 presents the observed X-ray weakness as a function of Eddington ratio for these 30 sources as circles. A Spearman's ρ test and a generalized Kendall's τ test¹ return a probability in favor of a correlation between $\Delta\alpha_{\text{ox}}$ and λ_{Edd} of 0.9977 and 0.9983, respectively. These values are a hint for a possible correlation, but the sample does not populate the extreme tails of the Eddington-ratio distribution; i.e. $\lambda_{\text{Edd}} \lesssim 0.1$ and, especially, $\lambda_{\text{Edd}} \approx 1$, preventing an accurate assessment of a possible relation.

True uncertainties on the estimated black-hole masses are due to a complex combination of factors, like the measurement of the line profile and width, and the continuum luminosity. Shen et al. (2011) report errors on black-hole masses that include these observational measurement errors. However, the dominant uncertainty factor is the scatter of the calibration between black-hole mass and Mg II line width, which is ≈ 0.35 dex (e.g. Shen et al. 2011). In Fig. 1 we use this value to estimate the uncertainty on λ_{Edd} . We also show the median error on $\Delta\alpha_{\text{ox}}$ derived from the statistical uncertainties on the X-ray counts only. We note that the non-parametric statistical tests we used are based on point ranking, and thus are not nominally sensitive to the error bars, although their statistical power decreases in the case of large uncertainties.

2.2 Selection of our XMM–Newton targets, data reduction, and analysis

In order to increase the number of BALQSOs with low and high values of Eddington ratio, thus allowing us to determine with high significance if the $\Delta\alpha_{\text{ox}}-\lambda_{\text{Edd}}$ correlation exists, during AO16 we

¹We used the ASURV v1.2 package (http://www.astrostatistics.psu.edu/statcodes/sc_censor.html), which accounts for censored data.

Table 2. Main properties of the sample of BALQSOs selected from the literature and BALQSOs newly observed in X-rays.

SDSS ID	z	$\log(L_{\text{bol}})$	$\log(M_{\text{BH}}/M_{\odot})$	$\log\lambda_{\text{Edd}}$	$\Delta\alpha_{\text{ox}}$	$\frac{\text{BI}_0}{\text{km s}^{-1}}$	Ref.
Sources studied in previous works							
011227.60 – 011221.7	1.76	47.01	9.51	−0.60	−0.70	2150	G09
020230.66 – 075341.2	1.72	46.60	9.12	−0.62	< −0.24	208	F09
024304.68+000005.4	1.99	46.95	9.70	−0.85	−0.10	325	F09, G09
083104.90+532500.1	2.07	47.40	10.00	−0.70	−0.51	556	G09
084538.66+342043.6	2.15	47.59	10.27	−0.79	−0.18	2638	G09
092138.44+301546.9	1.59	46.85	9.34	−0.59	−0.51	1	F09, G09
093514.71+033545.7	1.82	47.54	9.35	+0.09	−0.38	5	G09, M14
094309.55+481140.5	1.81	46.77	9.17	−0.50	< −0.33	52.2	G09,F09
094440.42+041055.6	1.98	46.71	8.88	−0.27	< −0.34	1104	F09
095944.47+051158.3	1.60	46.52	9.71	−1.29	−0.15	150	G09
100711.80+053208.9	2.10	47.81	10.43	−0.72	−0.27	4263	G09, M14
110637.15+522233.3	1.84	46.58	9.33	−0.85	−0.26	588.0	G09
120522.18+443140.4	1.92	46.63	9.48	−0.95	−0.23	1059.1	F09, G09
120626.17+151335.5	1.63	46.79	9.30	−0.61	−0.47	1429	G09
121125.48+151851.5	1.96	46.75	9.45	−0.80	−0.41	5137	G09
121440.27+142859.1	1.62	47.14	9.37	−0.33	< −0.62	3301	G09
121930.95+104700.0	1.62	47.09	9.44	−0.44	−0.49	3288	G09
122637.02+013016.0	1.55	46.86	9.58	−0.82	−0.27	3159.7	G09
130136.12+000157.9	1.78	47.16	9.83	−0.77	−0.42	4522	G09
142620.30+351712.1	1.75	46.7	9.31	−0.71	0.02	245.2	G09
142640.83+332158.7	1.54	46.34	9.36	−1.12	−0.31	101.5	G09
142652.94+375359.9	1.81	46.54	9.56	−1.13	−0.26	239.5	G09,F09
143031.78+322145.9	2.21	46.46	9.6	−1.24	<0.16	308.8	G09
143117.93+364705.9	2.1	46.84	9.42	−0.68	−0.05	426.1	G09
143411.23+334015.3	1.79	46.48	9.5	−1.12	−0.03	70.7	G09
143513.90+484149.2	1.89	46.74	9.62	−0.98	0.01	314.2	G09
143752.75+042854.5	1.92	47.05	9.97	−1.02	< −0.42	2663	G09, M14
143853.36+354918.7	1.55	46.51	9.04	−0.63	−0.14	1079.8	G09
155338.20+551401.9	1.64	46.72	9.69	−1.07	−0.22	18	G09
235253.51 – 002850.4	1.62	46.83	9.35	−0.62	< −0.82	4307	G09
Newly observed sources							
0938+3805	1.828	47.51	9.4	0.01	−0.08	167	This work
1112+0053	1.687	47.07	10.2	−1.22	−0.09	440	This work
1252+05273	1.900	47.42	9.5	−0.21	0.12	95	This work
1644+4307	1.715	47.28	10.1	−0.96	−0.14	85	This work

Notes:

IDs, redshifts, bolometric luminosities, and SMBH masses are from Shen et al. (2011). Bolometric luminosities are computed from the rest-frame 3000Å or 1350Å luminosities at $z < 1.9$ and $z > 1.9$, respectively. Virial SMBH mass estimates are derived from the Mg II emission line. See Shen et al. (2011) for details. We computed the Eddington ratios using the bolometric luminosities and black-hole masses reported in this table. Values of $\Delta\alpha_{\text{ox}}$ are computed as described in Section 2.1 for sources with previous X-ray observations and in Section 2.2 for newly observed sources. Values of the balnicity indices (BI_0) are collected from Gibson et al. (2009a). The last column reports the reference paper for the X-ray observations (F09: Fan et al. 2009; G09: Gibson et al. 2009a; M14: Morabito et al. 2014).

obtained *XMM-Newton* observations of four BALQSOs (see Table 3). They were selected among the BALQSOs included in the Gibson et al. (2009a) catalogue with black-hole mass from Shen et al. (2011) satisfying the quality cuts described in Section 2.1, with the additional requirement to have $\log\lambda_{\text{Edd}} \approx 1$ or $\log\lambda_{\text{Edd}} \approx 0.1$ to sample better these accretion regimes (see Table 2). X-ray data were reduced and analyzed following standard SAS² procedures. Periods of high background levels (count rates > 0.4 cts s^{−1} for the PN camera and > 0.35 cts s^{−1} for the MOS cameras) were filtered out. Table 3 reports the filtered exposure times. Our sources have ≈ 160 –2000 net counts in the 0.5–10 keV band, considering the three *XMM-Newton* cameras.

To be consistent with the derivation of the observed X-ray weakness in Gibson et al. (2009a), and also to avoid making strong assumptions about the X-ray spectra (e.g. neutral absorption), we performed a spectral analysis assuming a broken power-law model (*wabs*×*bknpowerlaw* in XSPEC), with break energy fixed at rest-frame 2 keV. Best-fitting parameters are reported in Table 4. For J164452.70+430752.20 we could not constrain the low-energy photon index, which hit the hard low boundary of the allowed parameter range (i.e. $\Gamma = -3$). We therefore fixed it to that value, which hints at a significant level of absorption. X-ray monochromatic luminosities are derived as observed (i.e. no correction for absorption has been applied), similarly to Gibson et al. (2009a). Hereafter, we will use these observed values (squares in Fig. 1) for consistency with the sample collected from the literature. The utilized model describes the effective (i.e. observed) shape of the X-ray spectrum, and the resulting observed luminosities are thus not strongly dependent on

²<https://www.cosmos.esa.int/web/xmm-newton/sas-threads>

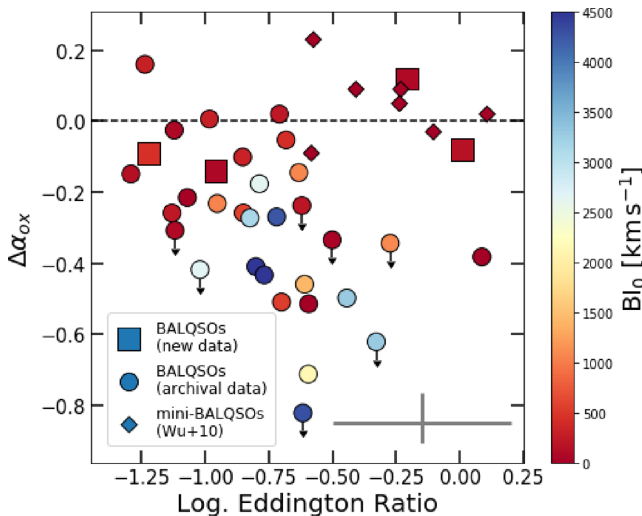


Figure 1. Observed X-ray weakness ($\Delta\alpha_{ox}$) as a function of Eddington ratio for the sample of BALQSOs collected from the literature (circles), our four targets of X-ray observations (squares), and the sample of mini-BALQSOs of Wu et al. (2010, small diamonds). Downward-pointing arrows represent upper limits (1σ confidence level). Symbols are colour-coded according to their BI_0 (see Section 3). The horizontal dashed line marks the locus of quasars with normal levels of X-ray emission (i.e. $\Delta\alpha_{ox} = 0$). The median uncertainties are shown as grey error bars in the bottom-right corner of the plot, and account only for the dominant error factors; i.e. the scatter in the M_{BH} – $FWHM_{Mg II}$ (≈ 0.35 dex; e.g. Shen et al. 2011) relation for λ_{Edd} , and the statistical uncertainties on the X-ray counts for $\Delta\alpha_{ox}$.

the true intrinsic spectral parameters (e.g. photon index and column density, which for low-to-moderate numbers of counts are strongly degenerate), nor the physical state of the possible absorbing material (e.g. neutral versus partly ionized).

2.2.1 Estimating the intrinsic luminosity

The number of net counts we detected for our targets (see last two columns of Table 3) allowed us to perform a simple spectral analysis assuming a power-law model with both Galactic and intrinsic neutral absorption (model `wabs × zwabs × powerlaw` in `XSPEC`³ v12.9.0n; Arnaud 1996) to estimate their intrinsic photon indices Γ , column densities, and luminosities. Best-fitting parameters are reported in Table 5. The best-fitting photon indices for two sources are flatter than the common values found for quasars, probably due to their photon-counting statistics ($\approx 160 - 230$ net counts; see Table 3) not being sufficiently high to break the degeneracy between (likely complex) absorption and flat photon index. For these objects, we repeated the fit fixing the photon indices to $\Gamma = 1.9$. Table 5 reports also the intrinsic (i.e. absorption-corrected) X-ray monochromatic luminosities, used to compute the $\Delta\alpha_{ox}$ values, which are thus estimates of the intrinsic X-ray weakness. We note that J164452.70+430752.20 shows the largest intrinsic column density in the sample, as expected from its very hard effective spectrum (see the previous section).

We stress that here we make a strong assumption considering the obscuring material neutral and fully covering, and thus for the rest of the analysis, consistently with the sample selected from the literature, we use the observed luminosities and $\Delta\alpha_{ox}$ values derived from

the broken power-law model in the previous section. As expected, since here we apply a correction for absorption, the luminosities and $\Delta\alpha_{ox}$ values reported in Table 5 are slightly higher than the observed values (Table 4), although the difference is smaller than the typical $\Delta\alpha_{ox}$ uncertainties. Therefore, the use of observed or intrinsic luminosities for our four sources does not affect significantly the results.

3 RESULTS AND DISCUSSION

In Section 3.1, we describe the results of our investigation of a putative anticorrelation between $\Delta\alpha_{ox}$ and λ_{Edd} . In Section 3.2, we study the relation between Eddington ratio and BAL strength, as parametrized by the BI. In Section 3.3, we include in our investigation a sample of mini-BALQSOs that satisfy our selection requirements, in order to expand the analysis to objects with weaker absorption features. Finally, in Section 3.4, we discuss and interpret the results.

3.1 $\Delta\alpha_{ox}$ versus λ_{Edd}

Adding our targets with low and high Eddington ratios to the sample retrieved from the literature does not confirm the putative $\Delta\alpha_{ox}$ – λ_{Edd} anticorrelation. In fact, the probability of a correlation decreases to 0.966 and 0.982, according to Spearman’s ρ and Kendall’s τ tests, respectively. This is largely due to the two sources with $\lambda_{Edd} \approx 1$ showing a level of X-ray emission close to expectation (i.e. $\Delta\alpha_{ox} = 0$) and much higher than other BALQSOs with similar or slightly lower λ_{Edd} . We therefore conclude that there is no clear and simple dependence of X-ray weakness on Eddington ratio in BALQSOs.

3.2 $\Delta\alpha_{ox}$ versus BAL strength

Several authors have investigated correlations between $\Delta\alpha_{ox}$ and the physical parameters of the outflow in BALQSOs, including the outflow velocity and absorption equivalent width (e.g. Gallagher et al. 2006; Gibson et al. 2009a; Wu et al. 2010), finding that $\Delta\alpha_{ox}$ is more negative in BALQSOs with stronger absorption features. We therefore investigated whether our targets follow this trend, and if the Eddington ratio plays a secondary role in driving the X-ray weakness. As a measure of BAL strength, we used the extended balnicity index (BI_0), defined by Gibson et al. (2009a) as

$$BI_0 = \int_0^{25000} \left(1 - \frac{f_v}{0.9}\right) C dv, \quad (2)$$

where f_v is the ratio of the observed spectrum to the continuum model as a function of the velocity v , and C is a constant set to unity if the spectrum is at least 10 percent below the continuum model for velocity widths of at least 2000 km s^{-1} and zero otherwise.

Following Gibson et al. (2009a), BALQSOs have $BI_0 > 0 \text{ km s}^{-1}$. We collected the values of BI_0 for our sample from Gibson et al. (2009a). Symbols in Fig. 1 are colour coded according to their balnicity indices. Fig. 2 presents the X-ray weakness as a function of BI_0 . Objects in our sample with strong BAL features ($BI_0 > 1000 \text{ km s}^{-1}$) are indeed typically X-ray weak ($-\Delta\alpha_{ox} = 0.2 - 0.8$). Sources with lower values of BI_0 show a large scatter of X-ray weakness. Gibson et al. (2009a) do not report uncertainties on BI_0 , which are dominated by the continuum emission measurement. We estimated its uncertainty from Filiz Ak et al. (2013), who studied a subsample of Gibson et al. (2009a), and used the median value to approximate the uncertainties on BI_0 in Fig. 2.

³heasarc.gsfc.nasa.gov/xanadu/xspec/

Table 3. Summary of *XMM-Newton* observations of our BALQSO targets. Net counts are computed following appendix A3 of Weisskopf et al. (2007). Exposure times are derived after filtering for background flares.

SDSS ID	OBSID <i>XMM-Newton</i>	Date	T_{EXP} ks	0.5 – 2 keV cts PN/MOS1/MOS2	2 – 10 keV cts PN/MOS1/MOS2
093846.80+380549.8	0801790401	2017-05-01	10.6/15.7/14.5	$172^{+14}_{-13}/90^{+10}_{-10}/124^{+12}_{-11}$	$57^{+9}_{-8}/22^{+5}_{-5}/34^{+7}_{-6}$
111249.70+005310.10	0801790101	2017-05-28	5.0/11.5/11.5	$55^{+8}_{-7}/39^{+7}_{-7}/36^{+7}_{-6}$	$47^{+8}_{-7}/18^{+5}_{-4}/31^{+6}_{-6}$
125216.60+052737.70	0801790601	2017-06-18	18.2/26.8/26.8	$656^{+26}_{-26}/246^{+16}_{-16}/270^{+17}_{-16}$	$160^{+14}_{-13}/390^{+21}_{-20}/438^{+22}_{-21}$
164452.70+430752.20	0801790301	2017-07-13	5.0/7.5/7.5	$48^{+8}_{-7}/18^{+5}_{-4}/31^{+6}_{-5}$	$35^{+7}_{-6}/14^{+4}_{-4}/20^{+5}_{-5}$

Table 4. Best-fitting spectral parameters assuming a broken power-law emission. The luminosity at rest-frame 2 keV is observed (i.e. not corrected for absorption).

SDSS ID	Γ_1	Γ_2	$F_{0.5-2\text{ keV}}$ $10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$	$L_{\nu, 2\text{ keV}}$ $10^{27} \text{ erg s}^{-1} \text{ Hz}^{-1}$	$\Delta\alpha_{\text{ox}}$
093846.80+380549.8	$-0.91^{+0.70}_{-0.81}$	$1.63^{+0.08}_{-0.08}$	3.50	1.22	− 0.08
111249.70+005310.10	$0.67^{+0.22}_{-0.24}$	$1.80^{+0.27}_{-0.25}$	2.36	0.61	− 0.09
125216.60+052737.70	$2.06^{+0.17}_{-0.18}$	$2.11^{+0.05}_{-0.05}$	7.80	3.48	0.12
164452.70+430752.20	− 3.00 fixed	$1.25^{+0.15}_{-0.09}$	2.29	0.62	− 0.14

Table 5. Best-fitting spectral parameters assuming power-law emission absorbed by neutral material. Luminosities are intrinsic.

SDSS ID	Γ	N_H 10^{22} cm^{-2}	$F_{0.5-2\text{ keV}}$ $10^{-14} \text{ erg cm}^{-2} \text{ s}^{-1}$	$L_{2-10\text{ keV}}$ $10^{45} \text{ erg s}^{-1}$	$L_{\nu, 2\text{ keV}}$ $10^{27} \text{ erg s}^{-1} \text{ Hz}^{-1}$	$\Delta\alpha_{\text{ox}}$
093846.80+380549.8	$1.90^{+0.13}_{-0.13}$	$1.4^{+0.4}_{-0.3}$	3.59	1.51	1.81	− 0.01
111249.70+005310.10	$1.39^{+0.16}_{-0.15}$	$0.7^{+0.6}_{-0.4}$	2.35	0.96	0.73	− 0.06
	1.90 fixed	$2.2^{+0.7}_{-0.5}$	2.60	1.14	1.35	0.04
125216.60+052737.70	$2.12^{+0.06}_{-0.05}$	< 0.1	7.81	2.48	3.50	0.12
164452.70+430752.20	$1.63^{+0.23}_{-0.21}$	$2.4^{+1.1}_{-0.9}$	2.32	1.11	1.04	− 0.05
	1.90 fixed	$3.4^{+0.8}_{-0.7}$	2.42	1.23	1.47	0.00

3.3 Expanding the sample to mini-BALQSOs

Our four targets happened to have quite weak BALs, as measured by the balnicity indices ($\text{BI}_0 \approx 100 \text{ km s}^{-1}$) and are placed in the weak-BAL regime, where the X-ray weakness shows a large scatter. It is therefore worth extending the parameter space to related objects with even weaker features. We thus considered the sample of mini-BALQSOs of Wu et al. (2010) that satisfy the quality cut described in Section 2.1. These objects are defined to have $\text{BI}_0 = 0 \text{ km s}^{-1}$ and absorption index $\text{AI} > 0 \text{ km s}^{-1}$, where

$$\text{AI} = \int_0^{29000} (1 - f_\nu) C' d\nu, \quad (3)$$

and $C' = 1$ when the velocity width is at least 1000 km s^{-1} and the absorption trough falls at least 10 per cent below the continuum; $C' = 0$ otherwise. Mini-BALQSOs thus represent an intermediate class of objects between BALQSOs and narrow absorption line QSOs (NALQSOs). The Wu et al. (2010) mini-BALQSOs show normal levels of X-ray emission (i.e. $\Delta\alpha_{\text{ox}}=0$; Fig. 2), restricting the scatter of $\Delta\alpha_{\text{ox}}$ at low values of BI_0 . They are also characterized by high accretion rates ($\log\lambda_{\text{Edd}} = [-0.6, 0.2]$), and indeed occupy the same region of the $\Delta\alpha_{\text{ox}}-\lambda_{\text{Edd}}$ plane as our two targets of rapidly accreting BALQSOs with low BI_0 (Fig. 1), thus reinforcing our conclusion that the X-ray weakness is not apparently driven by the Eddington ratio. In fact, repeating Spearman's ρ and Kendall's τ tests with the addition of this sample of mini-BALQSOs returns even lower probabilities in favor of a correlation between λ_{Edd} and $\Delta\alpha_{\text{ox}}$; i.e.

0.343 and 0.07, respectively. On the other hand, the anticorrelation between $\Delta\alpha_{\text{ox}}$ and BI_0 is confirmed with high significance (>0.999 for both tests).

3.4 Discussion

According to Fig. 2 and the statistical tests run in the previous section, prominent BAL features are good proxies of X-ray weakness in BALQSOs, irrespective of their Eddington ratio. While the fraction of BALQSOs appears to depend on the Eddington ratio (e.g. Ganguly et al. 2007), the lack of a clear correlation between $\Delta\alpha_{\text{ox}}$ and λ_{Edd} suggests that the observable X-ray-to-UV relative emission does not depend on the accretion rate. Since the optical/UV SEDs of quasars do not show evidence for a strong variation with Eddington ratio (e.g. Scott & Stewart 2014), this means that also the X-ray part of the SED does not vary strongly, at least for optically selected BALQSOs. Our entire sample of 34 BALQSOs spans a relatively narrow range of luminosity ($46.3 < \log L_{\text{bol}} \lesssim 47.8$; see Table 2), and thus we do not expect strong evolution in luminosity to affect this result.

We note that sources with strong BAL features ($\text{BI}_0 > 1000 \text{ km s}^{-1}$) show a hint of an anticorrelation between $\Delta\alpha_{\text{ox}}$ and λ_{Edd} : Spearman's ρ test and the generalized Kendall's τ test return a probability of anticorrelation of ≈ 0.94 and ≈ 0.96 , respectively, considering only the 14 BALQSOs with $\text{BI}_0 > 1000 \text{ km s}^{-1}$, although, the small sample size and the narrow λ_{Edd} regime ($-1 \lesssim \log\lambda_{\text{Edd}} \lesssim -0.4$) spanned prevents us from drawing solid conclusions. Most

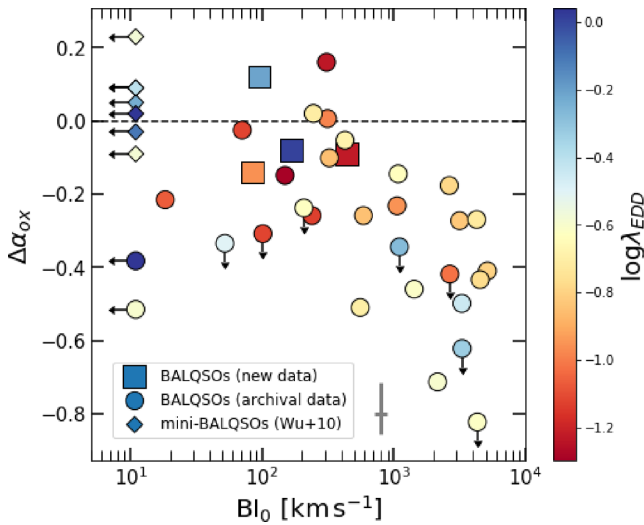


Figure 2. Observed X-ray weakness ($\Delta\alpha_{ox}$) as a function of BI_0 . Symbols are the same as in Fig. 1 and are colour-coded according to their Eddington ratio. The x-axis is in logarithmic units for visual purposes. Mini-BALQSOs (which have $BI_0 = 0 \text{ km s}^{-1}$ by definition) and BALQSOs with $BI_0 < 10 \text{ km s}^{-1}$ are plotted as upper limits on BI_0 (symbols with leftward-pointing arrows). The horizontal dashed line marks the locus of quasars with normal levels of X-ray emission (i.e. $\Delta\alpha_{ox} = 0$). The median uncertainties are shown as grey error bars in the bottom-right corner of the plot. We used a 10 per cent uncertainty for BI_0 (e.g. Filiz Ak et al. 2013), and the statistical uncertainties on the X-ray counts for $\Delta\alpha_{ox}$, which is its dominant factor of uncertainty.

of the scatter in Fig. 1 is indeed due to BALQSOs with low BI_0 . We speculate that the putative anticorrelation may thus be in place for BALQSOs with powerful and efficient outflows. To check this hypothesis, larger samples of BALQSOs with strong BAL features and accurate measurements of SMBH mass must be observed in X-rays. Weaker and less-massive winds may instead be present even if the X-ray emission is not significantly suppressed along the line of sight (see also, e.g. Gibson et al. 2009b; Hamann et al. 2013). For instance, stochastic events, such as a local overdensity of the disc or the intervening of a dense gas cloud, may provide the needed screening against the ionizing radiation to locally allow the acceleration of a wind, which would thus be detected through absorption features much weaker than in the case of global, massive outflows, but would not cause significant X-ray absorption along the line of sight.

In order to check if our results are sensitive to the particular quality cuts we imposed in Section 2.1, we repeated the analysis with a more conservative selection requiring $\text{SNR}_{\text{MgII}} > 10$ and $\text{SNR}_{\text{CIV}} > 10$. This conservative sample consists of 19 BALQSOs, including our 4 newly observed sources. The results hold, although with lower significance, due to the smaller sample size.

Finally, we note that the observed scatter of any intrinsic relation can be increased by orientation effects. In fact, orientation is known to play a non-negligible role in the determination of physical properties of quasars (e.g. Jarvis & McLure 2006; Shen & Ho 2014; Matthews et al. 2016), and, in particular, of black-hole virial mass estimates (e.g. Runnoe et al. 2013). Similarly, observational properties of BALQSOs, such as the strength and velocity of the absorption features, may differ along different lines of sight (e.g. Filiz Ak et al. 2014).

4 SUMMARY

We investigated the existence of a possible relation between the observed X-ray weakness ($\Delta\alpha_{ox}$) and the Eddington ratio λ_{Edd} in a sample of 34 BALQSOs. Such a trend could help alleviate the overionization of outflowing material necessary to produce a disc wind, if line-driven radiation pressure is the main accelerating mechanism. Moreover, both theoretical and observational findings suggest a change of the level of X-ray production in quasars approaching the Eddington limit. However, we did not find evidence for a strong anti-correlation between $\Delta\alpha_{ox}$ and λ_{Edd} . Instead, the strength of the BAL features appears to be a better tracer of $\Delta\alpha_{ox}$ than the Eddington ratio. Our results are confirmed also by considering a sample of mini-BALQSOs collected from the literature. Future X-ray observations of larger samples of BALQSOs with strong absorption features and accurate measurements of black-hole mass are needed to check if the anticorrelation between $\Delta\alpha_{ox}$ and λ_{Edd} is in place at least in the subpopulation with strong and massive winds, for which a stronger suppression of the X-ray emission may be required to accelerate the outflows efficiently.

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