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Planck intermediate results. XXXIII. Signature of the magnetic field geometry of interstellar filaments in dust polarization maps

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ABSTRACT

Planck observations at 353 GHz provide the first fully-sampled maps of the polarized dust emission towards interstellar filaments and their back-grounds (i.e., the emission observed in the surroundings of the filaments). The data allow us to determine the intrinsic polarization properties of the filaments and therefore to provide insight on the structure of their magnetic field ($\mathbf{B}$). We present the polarization maps of three nearby (several parsecs long) star forming filaments of moderate column density (N_{H} about 10^{22} cm^{-2}): Musca, B211, and L1506. These three filaments are detected above the background in dust total and polarized emission. We use the spatial information to separate Stokes I , Q , and U of the filaments from those of their backgrounds, an essential step to measure the intrinsic polarization fraction (p) and angle (ψ) of each emission component. We find that the polarization angles in the three filaments (ψ_{fil}) are coherent along their lengths and not the same as in their backgrounds (ψ_{bg}). The differences between ψ_{fil} and ψ_{bg} are 12° and 54° for Musca and L1506, respectively, and only 6° in the case of B211. These differences for Musca and L1506 are larger than the dispersions of ψ , both along the filaments and in their backgrounds. The observed changes of ψ are direct evidence for variations of the orientation of the plane of the sky (POS) projection of the magnetic field. As in previous studies, we find a decrease of several percent of p with N_{H} from the backgrounds to the crest of the filaments. We show that the bulk of the drop in p cannot be explained by random fluctuations of the orientation of the magnetic field within the filaments because they are too small ($\sigma_\psi < 10^\circ$). We recognize the degeneracy between the dust alignment efficiency and the structure of the $\mathbf{B}$ -field in causing variations in p , but we argue that the decrease of p from the backgrounds to the filaments results in part from depolarization associated with the 3D structure of the $\mathbf{B}$ -field: both its orientation in the POS and with respect to the POS. We do not resolve the inner structure of the filaments, but at the smallest scales accessible with *Planck* ($\sim 0.2 \text{ pc}$), the observed changes of ψ and p hold information on the magnetic field structure within filaments. They show that both the mean field and its fluctuations in the filaments are different from those of their backgrounds, confirming that the magnetic field has an active role in the formation of filaments.

Key words. Submillimetre: ISM – Polarization – ISM: dust, magnetic fields, turbulence – Interstellar filaments

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1. Introduction

The interstellar medium (ISM) has been observed to be filamentary for more than three decades. Filamentary structures have been observed in extinction (e.g., [Schneider & Elmegreen 1979](#); [Myers 2009](#)), in dust emission (e.g., [Abergel et al. 1994](#)), in H I (e.g., [Joncas et al. 1992](#); [McClure-Griffiths et al. 2006](#)), in CO emission from diffuse molecular gas ([Falgarone et al. 2001](#); [Hily-Blant & Falgarone 2009](#)) and dense star forming regions (e.g., [Bally et al. 1987](#); [Cambr sy 1999](#)). Filaments are striking features of Galactic images from the far-infrared/submm *Herschel* space observatory ([Andr  et al. 2010](#); [Motte et al. 2010](#); [Molinari et al. 2010](#)). They are ubiquitous both in the diffuse ISM and in star-forming molecular clouds, and the densest ones are observed to be associated with prestellar cores (e.g., [Arzoumanian et al. 2011](#); [Palmeirim et al. 2013](#)). Their formation and dynamical evolution has become a central research topic in the field of star formation (see the review by [Andr  et al. 2014](#), and references therein). In particular, the role played by the magnetic field is a main outstanding question.

The importance of the Galactic magnetic field for the dynamics of molecular clouds is supported by Zeeman measurements, which show that there is rough equipartition between their magnetic, gravitational, and kinetic energies (e.g., [Myers & Goodman 1988](#); [Crutcher et al. 2004](#)). Dust polarization observations provide an additional means to study the structure of the magnetic field. For a uniform magnetic field, the observed polarization angle is perpendicular to the component of the magnetic field on the plane of the sky (POS) in emission and parallel in extinction. The polarization fraction depends on the dust polarization properties and the grain alignment efficiency, but also on the structure of the magnetic field ([Hildebrand 1983](#)). A number of studies have investigated the relative orientation between the magnetic field and filaments in molecular clouds using starlight polarization (e.g. [Goodman et al. 1990](#); [Pereyra & Magalh es 2004](#); [Chapman et al. 2011](#); [Sugitani et al. 2011](#)). Dust polarized emission from the densest regions of molecular clouds, i.e., mainly dense cores and the brightest structures in nearby molecular clouds, has been observed from the ground at sub-mm wavelengths (e.g., [Ward-Thompson et al. 2000](#); [Crutcher et al. 2004](#); [Attard et al. 2009](#); [Matthews et al. 2001, 2009](#)) and more recently using balloon-borne experiments (e.g., [Pascale et al. 2012](#); [Matthews et al. 2014](#)). However, due to the limited sensitivity and range of angular scales probed by these observations, detection of polarization from filaments and their lower column density surroundings has not been achieved. This is a limitation because, as polarization is a pseudo-vector, the polarized emission observed towards a filament depend on those of the background. This effect is all the more important that the contrast between the filament and its background is low.

*Planck*¹ has produced the first all-sky map of the polarized emission from dust at sub-mm wavelengths ([Planck Collaboration I 2015](#)). The *Planck* maps of polarization angle, ψ , and fraction, p , encode information on the magnetic field structure ([Planck Collaboration Int. XIX 2015](#)). The observations have been compared to synthetic polarized emission maps computed from simulations of anisotropic magnetohydrodynamic

ical turbulence assuming simply a uniform intrinsic polarization fraction of dust grains ([Planck Collaboration Int. XX 2015](#)). In these simulations, the turbulent structure of the magnetic field is able to reproduce the main statistical properties of p and ψ that are observed directly in a variety of nearby clouds, dense cores excluded (see also [Falceta-Gon alves et al. 2008, 2009](#)). [Planck Collaboration Int. XX \(2015\)](#) concludes that the large scatter of p at N_H smaller than 10^{22} cm^{-2} in the observations is due mainly to fluctuations in the magnetic field orientation along the line of sight (LOS), rather than to changes in grain shape and/or the efficiency of grain alignment. They also show that the large-scale field orientation with respect to the LOS plays a major role in the quantitative analysis of these statistical properties.

The *Planck* maps of total intensity, as well as polarized intensity, display the filamentary structure of the ISM ([Planck Collaboration XI 2014](#); [Planck Collaboration Int. XIX 2015](#); [Planck Collaboration X 2015](#)). [Planck Collaboration Int. XXXII \(2014\)](#) identify interstellar filaments over the intermediate latitude sky, and present a statistical analysis of their orientation with respect to the component of the magnetic field on the POS ($\mathbf{B}_{\text{POS}}$). In the diffuse ISM, filaments are preferentially aligned with $\mathbf{B}_{\text{POS}}$. Towards nearby molecular clouds the relative orientation changes progressively from preferentially parallel to preferentially perpendicular from the lowest to the highest column densities ([Planck Collaboration Int. XXXV 2015](#)).

In this paper, we make use of the *Planck* polarization data to study the structure of the magnetic field within three fields comprising the archetype examples of star forming filaments of moderate column density: B211, L1506, and Musca. Characterizing the magnetic field structure in such filaments, and its connection with that of the surrounding cloud, is a step towards understanding the role of the magnetic field in their formation and evolution. Stellar polarization data in these fields have been reported by several authors ([Goodman et al. 1990](#); [Pereyra & Magalh es 2004](#); [Chapman et al. 2011](#)). With *Planck* we have now access to fully-sampled maps of the dust polarized emission of both the filaments and their surrounding environment. The spatial information allow us to derive the polarization properties intrinsic to the filaments after subtracting the contribution of the surrounding background to the Stokes I , Q , and U maps. We relate the results of our data analysis to the structure of the magnetic field.

The paper is organized as follows. The *Planck* data at 353 GHz and the relations used to derive the polarization parameters from the Stokes I , Q , and U maps are presented in Sect. 2. In Sect. 3, we present the I , Q , and U maps of the three filaments and their profiles perpendicular to their axes. In Sect. 4 we quantify the variations of the polarization angle and fraction from the background to the filaments, and within the filaments. Section 5 discusses possible interpretations of the observed decrease of p from the background to the filaments. Section 6 summarizes the results of our data analysis and presents perspectives to further studies. In Appendix A, we present a two-component model that applies as a first approximation to the polarized emission from interstellar filaments and their backgrounds.

2. Planck observations

Planck observed the sky in nine frequency bands from 30 to 857 GHz in total intensity, and in polarization up to 353 GHz ([Planck Collaboration I 2014](#)). Here, we only use the intensity and polarization data at 353 GHz, which is the highest frequency *Planck* channel with polarization capabilities and the one with best signal-to-noise ratio (S/N) for dust polarization ([Planck Collaboration Int. XXII 2015](#)). The in-flight performance of the

¹ *Planck* (<http://www.esa.int/Planck>) is a project of the European Space Agency (ESA) with instruments provided by two scientific consortia funded by ESA member states and led by Principal Investigators from France and Italy, telescope reflectors provided through a collaboration between ESA and a scientific consortium led and funded by Denmark, and additional contributions from NASA (USA).

Table 1. Observed properties of the filaments. Column 3 gives the length along the filament crest. Column 4 gives the filament full width at half maximum (FWHM) derived from a Gaussian fit to the total intensity radial profile. The values given are for the observations, i.e., without beam deconvolution. The outer radius (given in Column 5) is defined as the radial distance from the filament axis at which its radial profile amplitude is equal to that of the background (without beam deconvolution). Columns 6 and 7 give the observed column density values at the central part of the filament ($r = 0$) and at $r = R_{\text{out}}$, respectively. The latter corresponds to the mean value of the background. Column 8 gives the mass per unit length estimated from the radial column density profiles of the filaments. Column 9 gives the position angle (PA) of the segment of the filament that is used to derive the mean profile. The PA (measured positively from North to East) is the angle between the Galactic North (GN) and the tangential direction to the filament crest derived from the I map.

Filament	d [pc]	Length [pc]	Width [pc]	R_{out} [pc]	$N_{\text{H}}^{\text{fil}}$ [10^{21} cm^{-2}]	N_{H}^{bg} [10^{21} cm^{-2}]	M_{line} [$M_{\odot} \text{ pc}^{-1}$]	PA [deg]
Musca	200	10	0.75	1	8	2.2	30	30
B211	140	2.6	0.33	0.5	17	3	47	90
L1506	140	3	0.35	0.5	7	2.3	26	55

High Frequency Instrument (HFI) is described in [Planck HFI Core Team \(2011\)](#) and [Planck Collaboration II \(2014\)](#). We use a *Planck* internal release data set (DR3, delta-DX9) at 353 GHz, presented and analysed in [Planck Collaboration Int. XIX \(2015\)](#), [Planck Collaboration Int. XX \(2015\)](#), [Planck Collaboration Int. XXI \(2015\)](#), and [Planck Collaboration Int. XXXII \(2014\)](#). We ignore the polarization of the CMB, which at 353 GHz is a negligible contribution to the sky polarization towards molecular clouds ([Planck Collaboration Int. XXX 2014](#)). The I , Q , and U maps at the resolution of $4'8$ analysed here have been constructed using the gnomonic projection of the HEALPix² ([Górski et al. 2005](#)) all-sky maps. The regions that we study in this paper are within the regions of high S/N, which are not masked in [Planck Collaboration Int. XIX \(2015\)](#).

Stokes I , Q , and U parameters are derived from *Planck* observations. Stokes I is the total dust intensity. The Stokes Q and U parameters are the two components of the linearly polarized dust emission resulting from LOS integration and are related as

$$Q = Ip \cos(2\psi), \quad (1)$$

$$U = Ip \sin(2\psi), \quad (2)$$

$$P = \sqrt{Q^2 + U^2}, \quad (3)$$

$$p = P/I, \quad (4)$$

$$\psi = 0.5 \arctan(U, Q). \quad (5)$$

where P is the total polarized intensity, p is the polarization fraction (see Eq. 6), and ψ is the polarization angle given in the IAU convention (see [Planck Collaboration Int. XIX 2015](#)). The $\arctan(U, Q)$ is used to compute $\arctan(U/Q)$ avoiding the π ambiguity. The POS magnetic field orientation (χ) is obtained by adding 90° to the polarization angle ($\chi = \psi + 90^\circ$). In the paper we show the Stokes parameter maps as provided in the HEALPix convention, where the *Planck* U Stokes map is given by $U = -Ip \sin(2\psi)$. Due to the noise present in the observed Stokes parameter maps, P and p are biased positively and the errors on ψ are not Gaussian ([Planck Collaboration Int. XIX 2015](#); [Montier et al. 2015](#)). We debias P and p according to the method proposed by [Plaszczynski et al. \(2014\)](#), by taking into account the full noise covariance matrix of the *Planck* data.

3. The filaments as seen by *Planck*

In the following, we present the *Planck* I , Q , and U maps of three filaments in two nearby molecular clouds: the Musca fil-

ament, and the Taurus B211 and L1506 filaments. The angular resolution of *Planck* ($4'8$) translates into a linear resolution of 0.2 pc and 0.3 pc at the distances of the Taurus and the Musca clouds, 140 and 200 pc respectively ([Franco 1991](#); [Schlaflly et al. 2014](#)). Table 1 summarizes the main characteristics of the three filaments. We describe each of them in the following sections.

3.1. The Musca filament

Musca is a 10 pc long filament located at a distance of 200 pc from the sun, in the North of the Chamaeleon region ([Gregorio Hetem et al. 1988](#); [Franco 1991](#)). The mean column density along the crest of the filament is $8 \times 10^{21} \text{ cm}^{-2}$ as derived from the *Planck* data ([Planck Collaboration Int. XXIX 2014](#)). The magnetic field in the neighbourhood of the Musca cloud has been traced using optical polarization measurements of background stars by [Pereyra & Magalhães \(2004\)](#). *Herschel* SPIRE images show *hair-like* striations of matter perpendicular to the main Musca filament and aligned with the magnetic field lines.

Figure 1 shows the *Planck* 353 GHz Stokes parameter maps of the Musca cloud. The filament is well detected in total intensity and polarization. To quantify the polarized intensity observed towards the filament we derive radial profiles perpendicular to its axis. The crest of the filament is traced using the DisPerSE algorithm ([Sousbie 2011](#); [Arzoumanian et al. 2011](#)). Cuts perpendicular to the axis of the filament are then constructed at each pixel position along the filament crest. The profiles centred on neighbouring pixels along the filament crest, corresponding to six times the beam size ($6 \times 4'8$), are averaged to increase the S/N. The position of each of the profiles is shown on the intensity map of Fig. 1. The mean profiles are numbered from 1 to 7, running from the South to the North of the filament. Figure 2 shows the radial profiles of the Stokes parameters where hereafter r corresponds to the radial distance from the axis of the filament. The profiles in Fig. 2 illustrate the variability of the emission along the different cuts. The presence of neighbouring structures next (in projection) to the main Musca filament, can be seen in the profiles (e.g., the bumps at $r \simeq -2$ pc correspond to the elongated structure to the East of the axis of the Musca filament).

We observe a variation of the Stokes Q and U profiles of the filament associated with the change of its orientation on the POS. Thus the observed variations in the Stokes Q and U profiles are not necessarily due to variations of the $\mathbf{B}$ -field orientation with respect to the filament axis. In Fig. 3 the Q and U parameters, Q_{rot} and U_{rot} , are computed using the filament axis as the refer-

² <http://healpix.sourceforge.net>

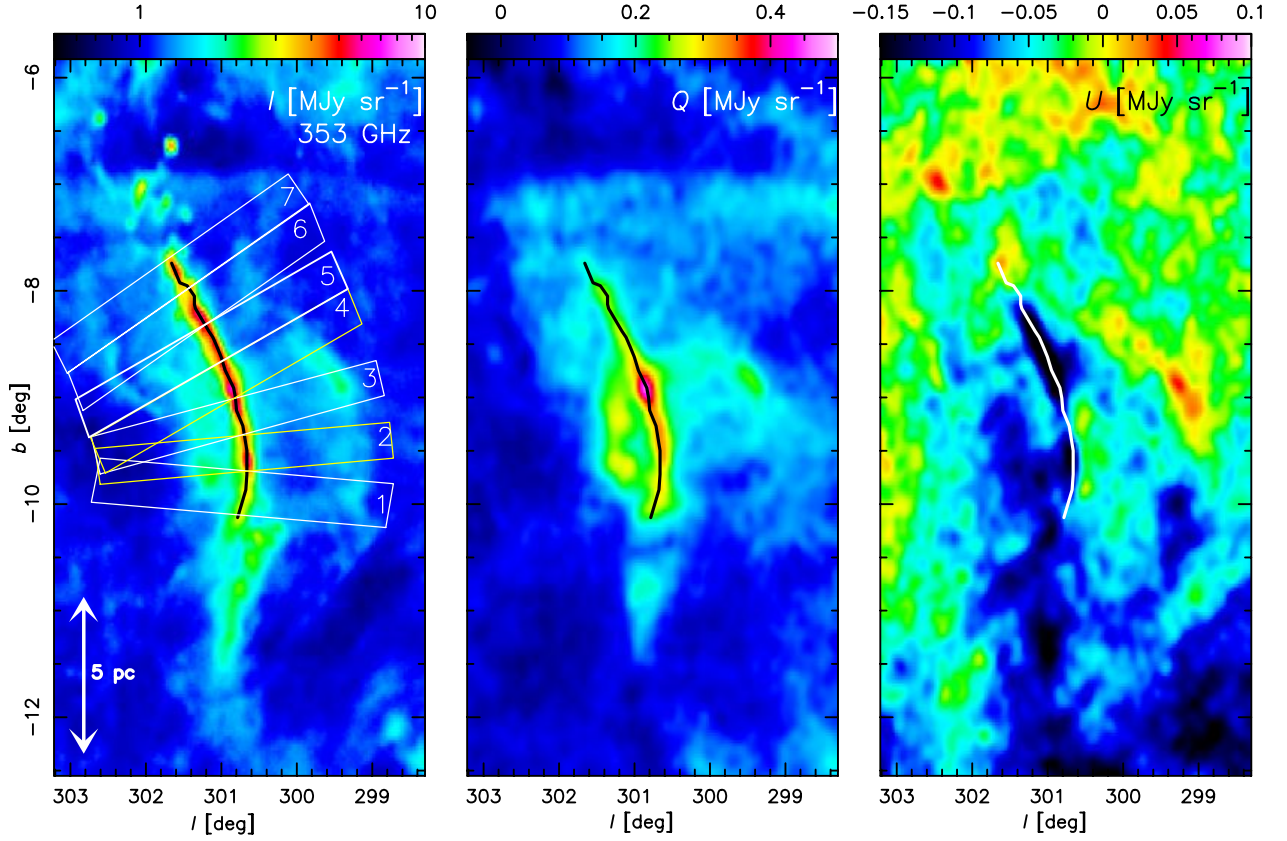


Fig. 1. *Planck* 353 GHz Stokes parameter maps of Musca (in MJy sr^{-1}). The total intensity map is at the resolution of $4''.8$, while the Q and U maps are smoothed to a resolution of $9''.6$ for better visualization. The crest of the filament traced on the I map is drawn in black (on the I and Q maps) and white (on the U map). The boxes drawn on the I map, numbered from 1 to 7, show the regions from which the mean profiles are derived (see Fig. 2).

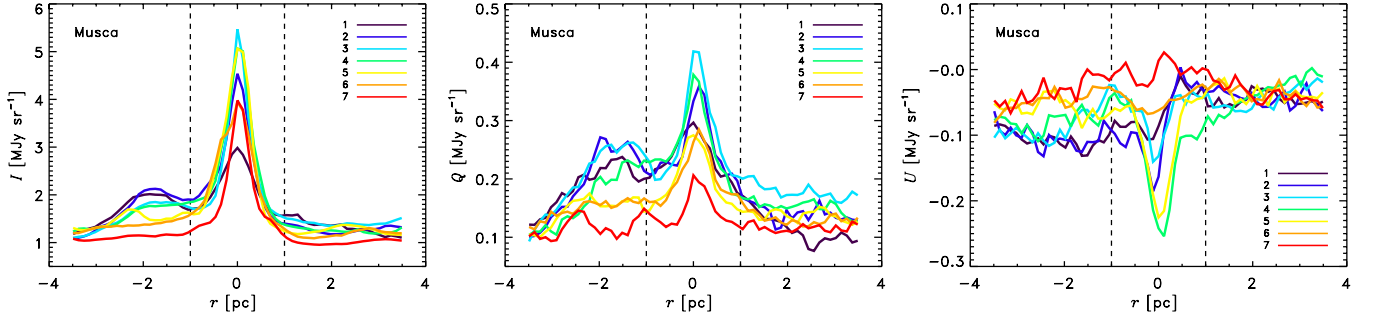


Fig. 2. Observed radial profiles perpendicular to the axis of the Musca filament. The I , Q , and U radial profiles are shown in the left, middle, and right panels, respectively. Values $r < 0$ correspond to the eastern side of the filament axis. The vertical dashed lines indicate the position of the outer radius R_{out} . The numbers of the profiles correspond to the map cuts shown on the left panel of Fig. 1.

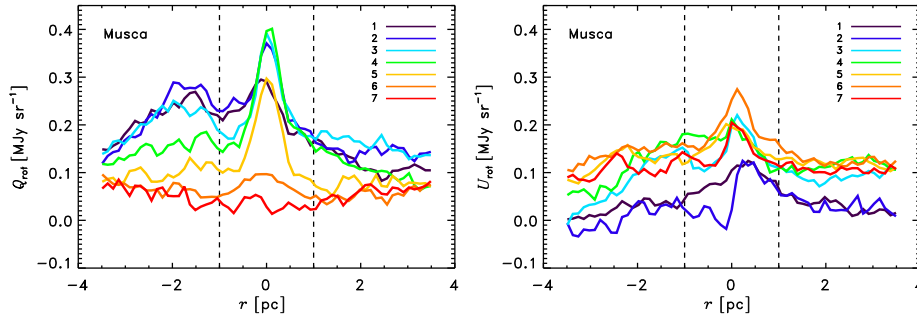


Fig. 3. Observed radial Q_{rot} (left) and U_{rot} (right) profiles of the Musca filament (same as Fig. 2) computed so that the reference direction is aligned with the filament axis.

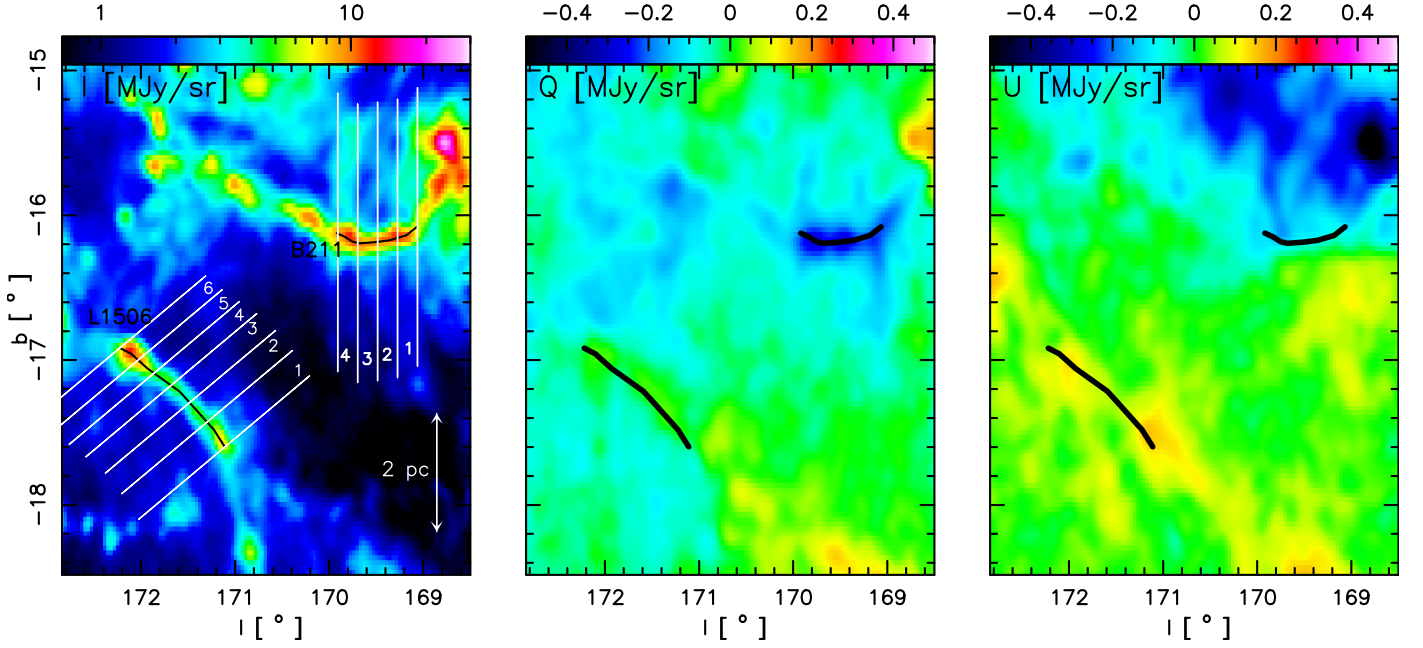


Fig. 4. Same as Fig. 1 for part of the Taurus molecular cloud around the B211 (Northwest) and the L1506 (Southeast) filaments. The numbers and white lines on the total intensity map correspond to the positions of the different cuts used to derive the radial profiles shown in Figs. 5 and 6.

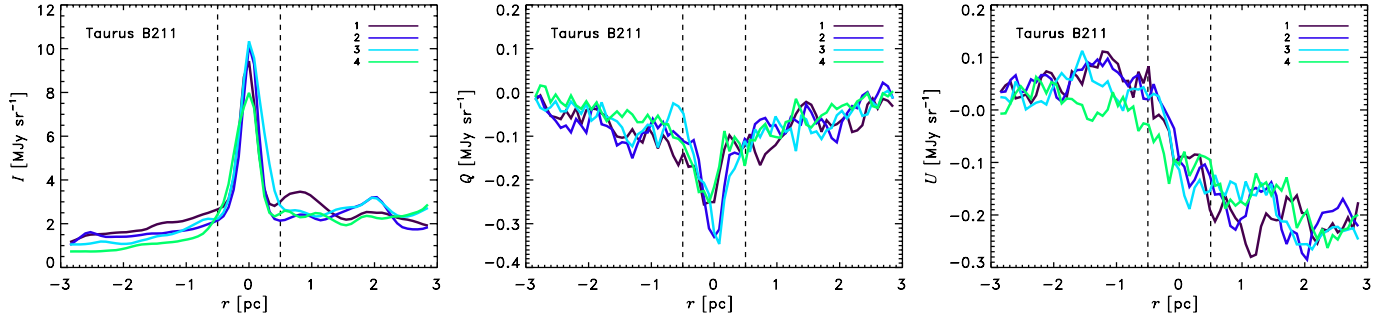


Fig. 5. Same as Fig. 2 for the Taurus B211 filament. Here $r < 0$ corresponds to the southern side of the filament axis. The filament is clearly seen in Q and is located in the area of a steep variation of the U emission. The dispersion of the emission is small along the length of the filament.

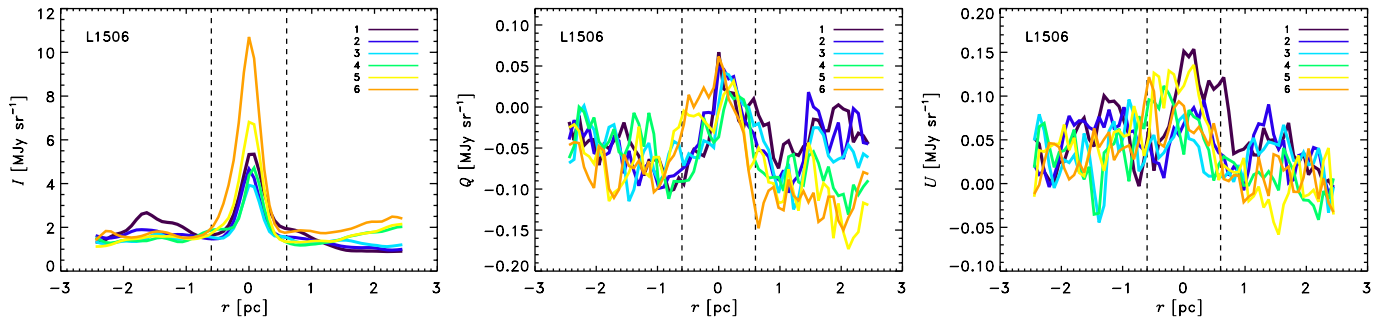


Fig. 6. Same as Fig. 2 for L1506. Here $r < 0$ corresponds to the southeastern side of the filament axis.

ence direction; the position angle (PA) of each segment (1 to 7) is estimated from the mean tangential direction to the filament crest. The parameter Q_{rot} is positive and $U_{\text{rot}} = 0$ if the magnetic field is perpendicular to the filament axis. The data (Fig. 3) show that most of the polarized emission of segments 1 to 5 is associated with $Q_{\text{rot}} > 0$ and $Q_{\text{rot}} > |U_{\text{rot}}|$. This is consistent with a magnetic field close to perpendicular to the filament axis. For

the segments 6 and 7, the relative orientation between the $\mathbf{B}_{\text{POS}}$ angle and the filament is different as indicated by the Q_{rot} and U_{rot} profiles.

3.2. The Taurus B211 filament

The B211 filament is located in the Taurus molecular cloud (TMC). It is one of the closest star forming regions in our Galaxy located at a distance of only 140 pc from the Sun (Elias 1978; Kenyon et al. 1994; Schlafly et al. 2014). This region has been the target of numerous observations, has long been considered as a prototypical molecular cloud of isolated low-mass star formation, and has inspired magnetically-regulated models of star formation (e.g., Shu et al. 1987; Nakamura & Li 2008). The B211 filament is one of the well-studied nearby star-forming filaments that shows a number of young stars and prestellar cores along its ridge (Schmalzl et al. 2010; Li & Goldsmith 2012; Palmeirim et al. 2013). Recently, Li & Goldsmith (2012) studied the Taurus B211 filament and found that the measured densities and column densities indicate a filament width along the LOS that is equal to the width observed on the POS (~ 0.1 pc). Studies previous to *Planck*, using polarization observations of background stars, found that the structure of the Taurus cloud and that of the magnetic field are related (e.g., Heyer et al. 2008; Chapman et al. 2011). Using the Chandrasekhar-Fermi method, Chapman et al. (2011) estimated a magnetic field strength of about $25 \mu\text{G}$ in the cloud surrounding the B211 filament, concluding that the former is magnetically supported.

Figure 4 shows the *Planck* 353 GHz Stokes parameter maps of the TMC around the B211 and L1506 filaments. The B211 filament is well detected in the I and Q maps, as a structure distinct from its surrounding. On the U map, on the other hand, the filament is not seen as an elongated structure, but it is perpendicular to a large U gradient that separates two regions of almost uniform U . The U emission is negative on the northern side of the filament while it is positive on the southern side. This indicates that the $\mathbf{B}$ -field orientation varies in the cloud surrounding the B211 filament. This variation can be seen very clearly in the radial profiles perpendicular to the filament axis, shown in Fig. 5. These profiles are derived as explained in the previous section (for the Musca filament). The four Q and U profiles (shown in the middle and right-hand panels of Fig. 5) are derived by averaging the cuts within a distance along the filament crest of 3 times the *Planck* beam (3×4.8). The cloud intensity (I) increases from the southern to the northern side of the filament, while the Q emission is similar on both sides of the filament axis. The (negative) Q emission of B211 is very clearly seen in the radial profiles. The different profiles show the approximate invariance of the emission along the filament crest. The total and polarized emission components are remarkably constant along the length of B211.

3.3. The Taurus L1506 filament

The L1506 filament is located on the Southeast side of B211 (see Fig. 4). Stellar polarization data are presented by Goodman et al. (1990). The density structure and the dust emission properties have been studied by Stepnik et al. (2003), and more recently by Ysard et al. (2013) using *Herschel* data. This filament has mean column densities comparable to those of the Musca filament. Star formation at both ends of L1506 has been observed with the detection of a few candidate prestellar cores (Stepnik et al. 2003; Pagani et al. 2010). Figure 6 shows the radial profiles perpendicular to its axis. The colour profiles numbered from 1 to 5 (and derived as explained in Sect. 3.2), correspond to mean profiles at different positions along its crest. Profiles 1, 5, and 6 trace the emission corresponding to the star forming cores at the two ends of the filament. The other profiles (2 to 4) trace the

emission associated with the filament, not affected by emission of star-forming cores. The fluctuations seen in the Q and U profiles are of the same order as the fluctuations of the emission of B211 located a few parsecs Northwest of L1506, but the polarized emission associated with the filament is much smaller (the scale of the plots in Figs. 5 and 6 is not the same). The polarized intensity observed towards L1506 is smaller than that associated with the Musca and B211 filaments, while the total intensity is of the same order of magnitude.

3.4. Polarized intensity and polarization fraction

Figure 7 presents the polarized intensity (P) maps of the two studied molecular clouds, derived from the Q and U maps using Eq. (3) and debiased according to the method proposed by Plaszczyński et al. (2014), as mentioned in Sect. 2. The POS angle of the magnetic field (χ) is overplotted on the maps; the length of the pseudo-vectors is proportional to the observed (de-biased) polarization fraction. These maps show that the Musca and B211 filaments are detected in polarized emission, while the L1506 filament is not seen as an enhanced structure in polarized intensity unlike in total intensity.

The polarization fraction (p) is plotted as a function of the column density (N_{H}) for the filaments and their backgrounds in Fig. 8. This plot shows a large scatter of p for the lowest column density values corresponding to the background in L1506 and B211. Such a scatter is present in the statistical analysis of *Planck* polarization data towards Galactic molecular clouds (see in particular Fig. 2 in Planck Collaboration Int. XX 2014). For the filaments, p decreases as a function of column density with different slopes (see Fig. 8). We have drawn three lines, one for each filament. They represent the linear fit $\log p$ versus $\log N_{\text{H}}$ for N_{H} larger than 2.2×10^{21} , 6×10^{21} , and $3 \times 10^{21} \text{ cm}^{-2}$. The best fit slopes are -0.35 , -0.36 , and -1.15 , for Musca, B211 and L1506, respectively. A decrease of p with N_{H} has been reported in previous studies and ascribed to the loss of grain alignment efficiency (e.g. Lazarian et al. 1997; Whittet et al. 2008) and/or the random component of the magnetic field (e.g. Jones et al. 1992; Ostriker et al. 2001; Planck Collaboration Int. XIX 2015; Planck Collaboration Int. XX 2015). In the next sections, we take advantage of the imaging capability and sensitivity of *Planck* to further characterize the origins of the polarization properties of the filaments.

4. Polarization properties

In the following, we introduce a two-component model that uses the spatial information in *Planck* images to separate the emission of the filaments from the surrounding emission (Sect. 4.1). This allows us to characterize and compare the polarization properties of each emission component (Sects. 4.2 and 4.3).

4.1. A two-component model: filament and background

The observed polarized emission results from the integration along the LOS of the Stokes parameters. We take this into account by separating the filament and background emission using the spatial information of the *Planck* maps. We describe the dust emission observed towards the filaments as a simplified model with two components. One component corresponds to the filament, for $|r| < R_{\text{out}}$, where r is the radial position relative to the filament axis ($r = 0$) and R_{out} is the outer radius. The other component represents the background.

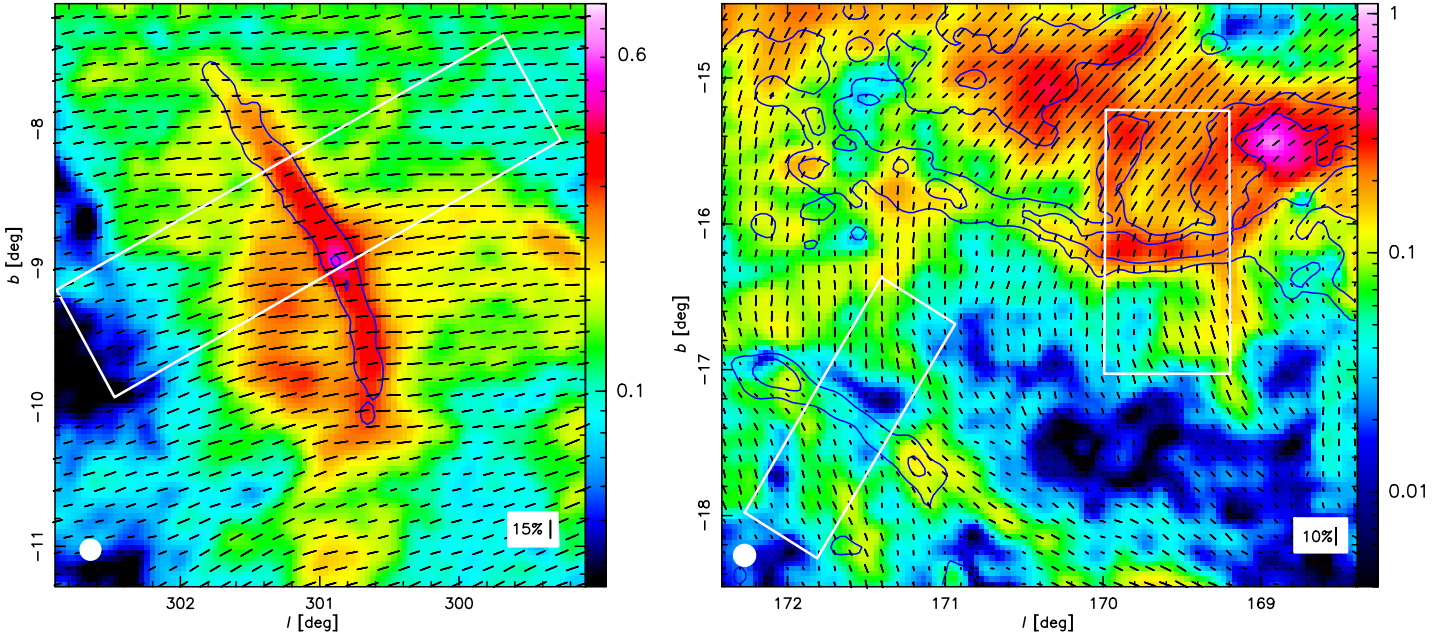


Fig. 7. Observed polarized emission at 353 GHz (in MJy sr^{-1}) of the Musca (left) and Taurus (right) clouds. The maps are at the resolution of $9''.6$ (indicated by the white filled circles) for increased S/N. The black segments show the $\mathbf{B}_{\text{POS}}$ -field orientation ($\psi+90^\circ$). The length of the pseudo-vectors is proportional to the polarization fraction. The blue contours show the total dust intensity at levels of 3 and 6 MJy sr^{-1} , at the resolution of $4''.8$. The white boxes correspond to the area of the filaments and their backgrounds that is analysed in the rest of the paper.

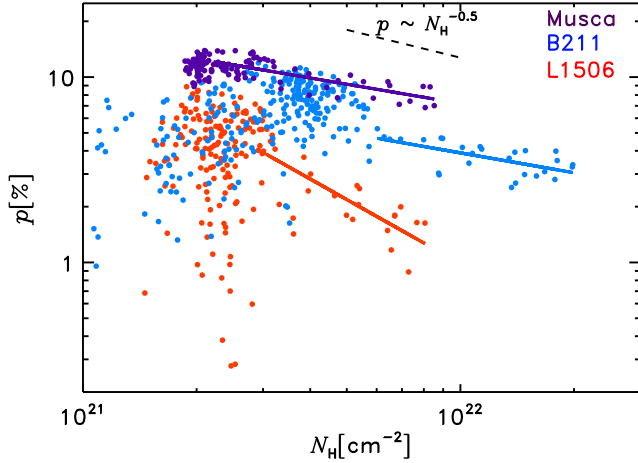


Fig. 8. Observed polarization fraction (p) as a function of column density (N_{H}), for the cuts across the axis of the filaments derived from the boxes shown in Fig. 7. The three lines show linear fits of $\log p$ versus $\log N_{\text{H}}$ described in Sect. 3.4. The data uncertainties depend on the intensity of the polarized emission. They are the largest for low p and N_{H} values. The mean error bar on p is 1.2 % for the data points used for the linear fits, and 2.5 % for the points where $p < 3\%$ and $N_{\text{H}} < 3 \times 10^{21} \text{ cm}^{-2}$.

We define as *background* the emission that is observed in the vicinity of a filament. It comprises the emission from the molecular cloud where the filament is located and from the diffuse ISM on larger scales. We argue that the former is the dominant contribution. Indeed, the Taurus B211 and L1506 filaments and the lower column density gas surrounding them are detected at similar velocities in ^{13}CO and ^{12}CO (between 2 and 9 km s^{-1} , Goldsmith et al. 2008), indicating that most of the background

emission is associated with the filaments. CO emission is also detected around the Musca filament (Mizuno et al. 2001). Planck Collaboration Int. XXVIII (2014) presents a map of the dark neutral medium in the Chameleon region derived from the comparison of γ -ray emission measured by *Fermi* with H I and CO data. This map shows emission around the Musca filament indicating that the background is not associated with the diffuse ISM traced by H I emission.

We separate the filament and background contributions to the I , Q , and U maps within the three fields defined by the white boxes in the Taurus and Musca images displayed in Fig. 7. The filaments have all a constant orientation on the POS within the selected fields. For L1506 the field also excludes the star-forming parts of that filament (see Sect. 3.3). Within each field, we separate pixels between filament and background areas using the I map to delineate the position and width of the filament. We fit the pixels over the background area with a polynomial function in the direction perpendicular to the filament axis. The fits account for the variations of the background emission, most noticeable for U in B211 (see Fig. 4). The spatial separation is illustrated on the I , Q , and U radial profiles shown in Fig. 9. These mean profiles are obtained by averaging data within the selected fields in the direction parallel to the filament axes. They are related to the profiles presented in Sect. 3 as follows. The mean profile of Musca corresponds to the averaging of profiles 4 and 5 in Fig. 2, that of the B211 filament to profiles 1 to 4 in Fig. 5, and for L1506 to the profiles 2 to 4 in Fig. 6. Figure 9 displays the fits of the I , Q and U profiles for $|r| > R_{\text{out}}$ with polynomial functions of degree three and interpolated for $|r| < R_{\text{out}}$. The fits reproduce well the variations of the background emission outside of the filaments (Fig. 9).

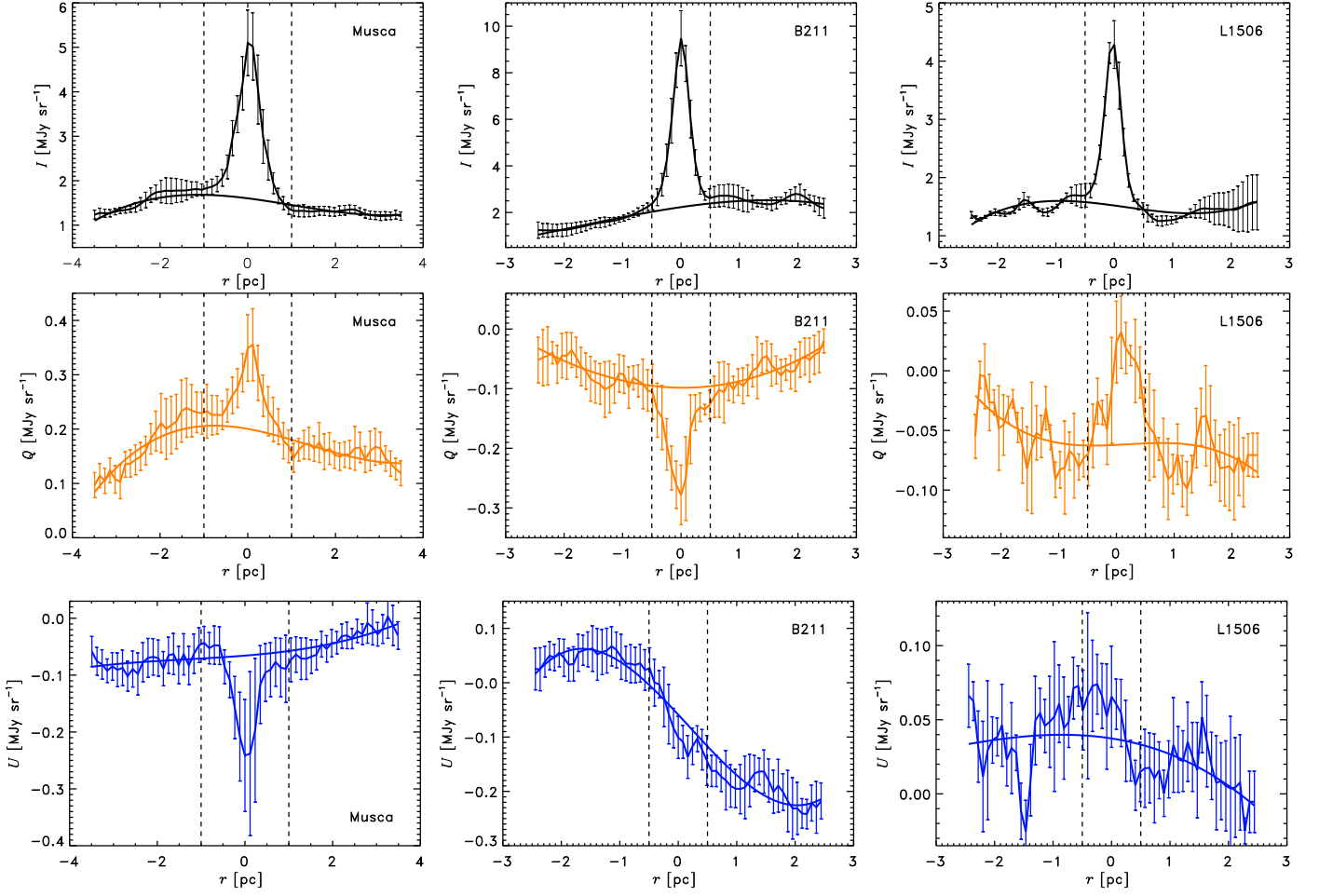


Fig. 9. Stokes parameters observed towards Musca (left), B211 (middle), and L1506 (right). The profiles correspond to the observed I (top), Q (middle) and U (bottom) emission averaged along the filament crest as explained in Sect. 4.1. The error-bars represent the dispersion of the pixel values that have been averaged at a given r . The polynomial fits to the background are also shown. The vertical dashed lines indicate the position of the outer radius R_{out} for each filament.

4.2. Derivation of the polarization properties

We use the spatial separation of the filament and background contributions to the Stokes maps to derive the polarization properties of the filaments and their backgrounds listed in Table 2. We detail how the various entries in the Table have been computed.

The fits provide estimates of the background values interpolated at $r = 0$. The entries I_{bg} , Q_{bg} , and U_{bg} in Table 2 are mean values averaged along the filament crests. The polarization angles (ψ_{bg}) and fractions (p_{bg}) for the background are computed from I_{bg} , Q_{bg} , and U_{bg} . The error-bars are statistical uncertainties. There is also an uncertainty associated with our specific choice for the degree of the polynomial function, which we quantify giving values derived from a third degree polynomial (pol3) and a linear (pol1) fit of the background. To compute the dispersion of the polarization angle ($\sigma_{\psi_{\text{bg}}}$), we smooth the Q and U background subtracted maps with a 3×3 pixels boxcar average. The values of $\sigma_{\psi_{\text{bg}}}$ in Table 2 are noise corrected. They correspond to the square root of the difference between the variance of the polarization angles on the background and that of the noise. The noise variance is computed from the dispersion of Q and U in reference, low brightness, areas within the Taurus and Musca maps, outside the molecular clouds. It comprises both the data noise and the fluctuations of the Galactic emission. The uncertainty on the noise correction is not a significant source of

error on $\sigma_{\psi_{\text{bg}}}$ after smoothing the data with a 3×3 pixels boxcar. We have also checked that we obtain values for $\sigma_{\psi_{\text{bg}}}$ within the quoted error-bars using a 5×5 pixels boxcar average.

We compute the filament I , Q , and U emission averaging pixels of the background-subtracted maps along cuts perpendicular to the filament. The data averaging, done to reduce the noise, yields about 20 values of each Stokes parameters along the crest of each filament, spaced by $2''$ for an angular resolution of $4''.8$. The mean Stokes parameters (I_{fil} , Q_{fil} , and U_{fil}), the mean polarization angle (ψ_{fil}) and fraction (p_{fil}), the dispersion $\sigma_{\psi_{\text{fil}}}$, and their error bars are computed from the average and the dispersion of these values. In Table 2, we also list the polarization properties computed for the total filament emission without background subtraction (i.e. the observed emission towards the filament). The values of $\sigma_{\psi_{\text{fil}}}$ are systematically greater with than without background subtraction, because the dispersion of polarization angles depend on the intensity of the polarized emission, which is reduced by the subtraction of the background.

The data analysis is illustrated in two figures. The profiles of the polarization angle, the total polarized intensity, and the polarization fraction derived from the data and the fits to the background are shown in Fig. 10. This figure also displays the intrinsic polarized intensity of the filament after subtraction of the background emission. Fig. 11-left shows the profile of ψ_{fil}

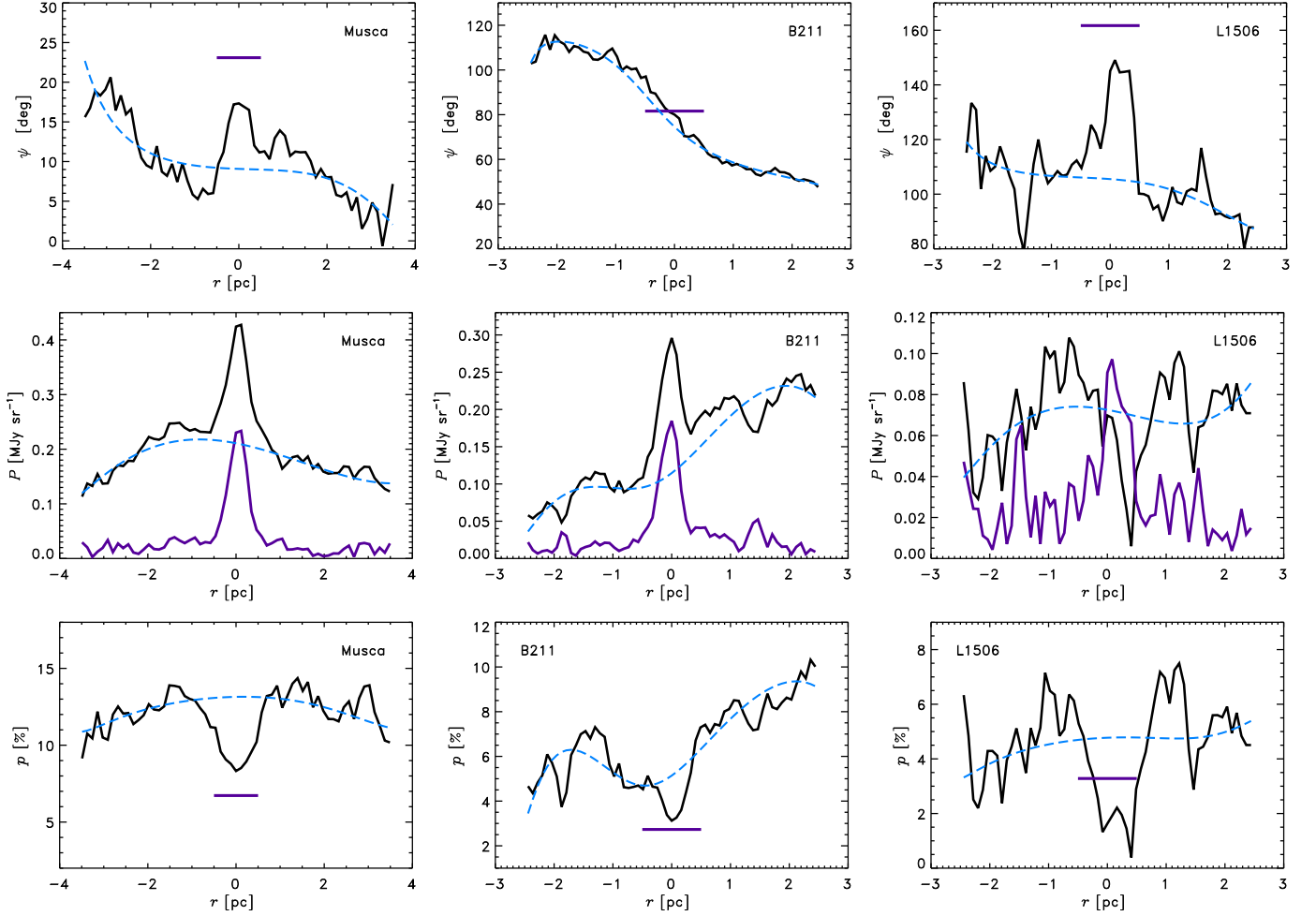


Fig. 10. Observed profiles (in black) of the polarization angle, the polarized intensity, and the polarization fraction, from top to bottom. The dashed blue curves show the variation of the background values of ψ_{bg} , P_{bg} , and p_{bg} derived from I_{bg} , Q_{bg} , and U_{bg} . The P_{fil} profiles in purple are derived from the polynomial fits I_{fil} , Q_{fil} , and U_{fil} . The horizontal purple lines indicate the mean polarization angle and fraction of the filaments for $|r| \leq R_{\text{out}}$.

along the crest for each of the three filaments. We have also averaged the background-subtracted I , Q , and U maps in the direction parallel to the filament axis to plot the profiles of the polarization angle across the filaments (Fig. 11-right).

4.3. Comparing the filament properties with that of their backgrounds

We use the results of our data analysis to compare the polarization properties of the filaments to those of their backgrounds.

Figs. 10 and 11 show that for the three filaments, ψ_{fil} differs from ψ_{bg} by 12° , 6° and 54° for the Musca, B211 and L1506 filaments, respectively (see Table 2). In Appendix A, we compute analytically the polarized emission resulting from the superposition along the line of sight of two emission components with different polarization angles. This analytical model is used to compute the observed polarization angle and fraction of the total emission as a function of the polarized intensity contrast and the difference in polarization angles. In the observations, the two components represent the filament and its background. Like in the model, the observed polarization angle derived from the total emission at the position of the filament (without background subtraction) differs from ψ_{fil} . The difference of 29° for L1506

is in good agreement with the value for the analytical model in Fig. A.1 for $\Delta\psi = 54^\circ$ and equal contributions of the filament and background to the polarized emission.

The LOS integration of both components, for $\psi_{\text{fil}} \neq \psi_{\text{bg}}$, always depolarizes the total emission. This effect has been ignored in earlier studies because it cannot be easily taken into account with stellar and sub-mm ground-based polarization observations. The L1506 filament illustrates the depolarization that results from the integration of the emission along the LOS: the polarized emission peaks at the position of the filament only after subtraction of the background (Fig. 10). For each of the filaments the effect of the LOS integration on p is different. The polarization fractions of the filaments are smaller than the values derived from the total emission for Musca and B211, while for L1506 it is greater. For the three filaments, the polarization fraction is smaller than that of the background interpolated at $r = 0$, as can be read in the right column of Table 2 and seen in the last row of Fig. 10, but this decrease is small for L1506 ($p_{\text{fil}} = 3.3 \pm 0.3$ vs $p_{\text{bg}} = 3.9 \pm 0.3$). In Appendix A.2, we compute the depolarization factor F as a function of the polarization angle difference and of the polarized intensity contrast. Figure A.2 shows that for $\Delta\psi = 54^\circ$, $F \simeq 0.6$ for comparable contributions of the filament and background to the polarized emission as in L1506 (see P profile in Fig. 10). This factor is in good agreement with the

Table 2. Polarization properties of the Musca, B211, and L1506 filaments (Fil) and their backgrounds (Bg). The total and filament values are computed on maps without and with background subtraction, respectively. They are average values across the filament area as explained in Sect. 4.2. The background values are at $r = 0$. We give two sets of values derived from the polynomial fits of degree three (pol3) and one (pol1) for comparison.

	I [MJy sr ⁻¹]	Q [MJy sr ⁻¹]	U [MJy sr ⁻¹]	$\psi^{(1)}$ [deg]	$\sigma_\psi^{(2)}$ [deg]	p [%]
Musca						
Total	3.67 ± 0.04	0.29 ± 0.01	-0.17 ± 0.01	15.4 ± 0.5	2.1 ± 0.3	9.1 ± 0.5
Fil(pol3)	2.12 ± 0.04	0.11 ± 0.01	-0.11 ± 0.01	22.2 ± 1.3	5.1 ± 0.6	7.3 ± 0.4
Fil(pol1)	2.39 ± 0.05	0.15 ± 0.01	-0.12 ± 0.01	19.3 ± 1.0	3.8 ± 0.4	8.2 ± 0.4
Bg(pol3)	1.55 ± 0.01	0.18 ± 0.01	-0.06 ± 0.01	9.8 ± 0.3	2.7 ± 0.2	12.1 ± 0.1
Bg(pol1)	1.28 ± 0.01	0.13 ± 0.01	-0.05 ± 0.01	10.0 ± 0.4	3.8 ± 0.2	11.2 ± 0.1
B211						
Total	7.31 ± 0.19	-0.24 ± 0.01	-0.11 ± 0.01	77.9 ± 0.8	3.5 ± 0.4	3.5 ± 0.2
Fil(pol3)	4.50 ± 0.19	-0.12 ± 0.01	-0.04 ± 0.01	81.0 ± 1.8	7.8 ± 0.9	2.7 ± 0.2
Fil(pol1)	4.86 ± 0.19	-0.14 ± 0.01	-0.03 ± 0.01	84.7 ± 1.6	6.7 ± 0.8	2.9 ± 0.2
Bg(pol3)	2.81 ± 0.03	-0.12 ± 0.01	-0.07 ± 0.01	75.3 ± 0.8	5.7 ± 0.6	4.9 ± 0.2
Bg(pol1)	2.45 ± 0.02	-0.10 ± 0.01	-0.07 ± 0.01	70.1 ± 1.0	7.9 ± 0.6	5.1 ± 0.1
L1506						
Total	3.28 ± 0.09	-0.01 ± 0.01	0.07 ± 0.01	132.3 ± 2.5	6.5 ± 2.0	2.1 ± 0.2
Fil(pol3)	1.69 ± 0.08	0.04 ± 0.01	0.03 ± 0.01	161.7 ± 3.4	9.9 ± 2.4	3.3 ± 0.3
Fil(pol1)	1.77 ± 0.09	0.05 ± 0.01	0.03 ± 0.01	164.0 ± 2.8	7.8 ± 2.1	3.6 ± 0.4
Bg(pol3)	1.59 ± 0.03	-0.05 ± 0.01	0.04 ± 0.01	107.8 ± 2.3	15.1 ± 1.5	3.9 ± 0.3
Bg(pol1)	1.50 ± 0.02	-0.06 ± 0.01	0.04 ± 0.01	105.2 ± 2.0	13.5 ± 1.3	4.7 ± 0.2

Notes. ⁽¹⁾ The errors on the polarization angles, ψ , correspond to statistical errors on the mean value of ψ . ⁽²⁾ The dispersion of the polarization angles, σ_ψ , are derived as explained in Sect. 4.2.

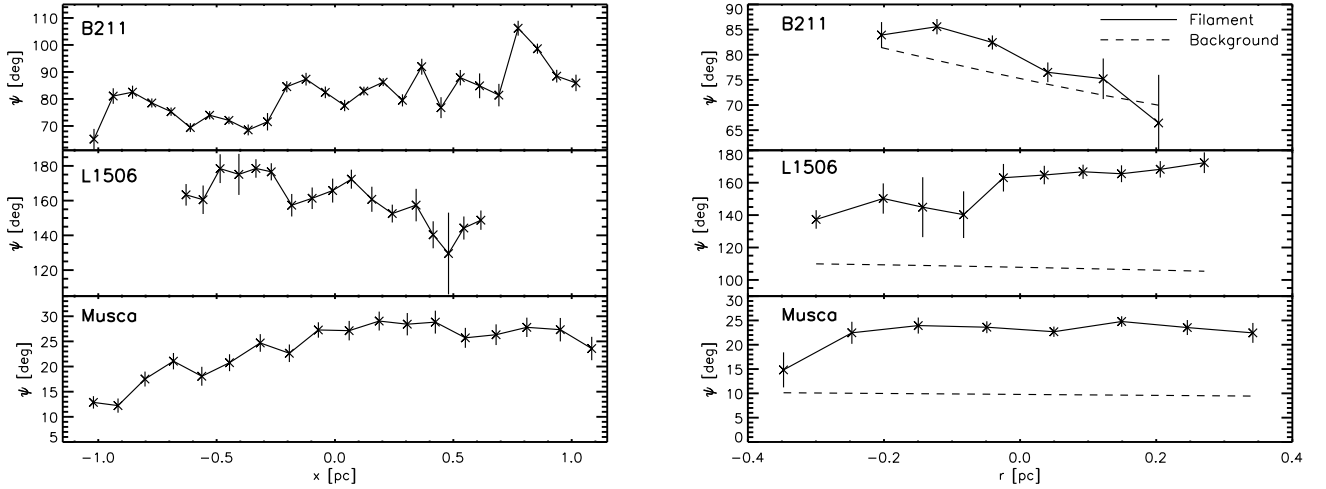


Fig. 11. Polarization angle along (left panel), and perpendicular (right panel) to, the crests of the filaments. The crosses are data points computed from Q and U values, after averaging the background subtracted maps in the direction perpendicular (left panel) and parallel (right) to the filament axes. In the left panel, x is a coordinate along the filament crest, while in the right panel, r is the radial distance to the filament axes. The beam is 0.3 pc for Musca, and 0.2 pc for B211 and L1506.

ratio between the two p values, without and with background subtraction, for L1506 in Table 2.

The differences between the filament position angles (PA) and χ ($\psi + 90^\circ$) are listed in Table 3. We find that B_{POS} in the backgrounds of Musca and B211 are close, within 20° , to being orthogonal to the filament axis, while for L1506, the background B_{POS} is at 37° . In the filaments, B_{POS} is perpendicular within 10° to the axis of Musca and B211, while it is close to parallel in L1506. We point out, though, that two orientations that are nearly perpendicular in 3D may be close to parallel on the POS

(Planck Collaboration Int. XXXII 2014; Planck Collaboration Int. XXXV 2015).

5. Interpretation of the polarization fraction

We discuss possible interpretations of the polarization fraction and its variation from the backgrounds to the filaments. The polarization fraction depends on dust grain properties and on the magnetic field structure expressed as the sum of mean and turbulent components. The observed polarization fraction is empir-

ically parametrized as

$$p = p_{\text{dust}} R F \cos^2 \gamma, \quad (6)$$

to distinguish four different effects due to both the local properties of dust and magnetic fields, and the LOS integration. The polarization properties of dust are taken into account with p_{dust} that depends on the composition, size, and shape of dust grains (Lee & Draine 1985; Hildebrand 1988). The Rayleigh reduction factor, $R \leq 1$, characterizes the efficiency of grain alignment with the local magnetic field orientation. The factor F expresses the impact on the polarization fraction of the variation of the magnetic field orientation along the LOS and within the beam. The role of the orientation of the mean magnetic field with respect to the POS is expressed by the $\cos^2 \gamma$ factor. The polarization fraction is maximal when the magnetic field is uniform and in the POS ($\gamma = 0$), while there is no linear polarization if the magnetic field is along the LOS ($\gamma = 90^\circ$). A main difficulty in the interpretation of polarization observations is that these four quantities cannot be determined independently. In particular, the product $p_{\text{dust}} R F$ is degenerated with the orientation of the mean magnetic field.

The interpretation of the polarization fraction presented in Sect. 5.1 focuses on the structure of the magnetic field. The factors p_{dust} and R are discussed in Sect. 5.2.

5.1. The structure of the magnetic field

5.1.1. Mean magnetic field orientation

For each of the three filaments, we find that the polarization angles vary from the background to the filament. These variations reflect changes in the 3D structure of the magnetic field, which impact p in two ways. First, changes of ψ along the LOS depolarize the emission lowering the observed p (see Appendix A). Second, p depends on the angle of $\mathbf{B}$ with respect to the POS (γ), which statistically must vary as much as ψ . We quantify these two aspects.

(1) L1506 illustrates the depolarization due to the superposition of emitting layers with different polarization angles (Sect. 4.3). For this filament, the decrease of p versus N_{H} in Fig. 8 can be almost entirely explained by the change of the $\mathbf{B}_{\text{POS}}$ orientation between the filament and its background. For Musca and B211, the ψ differences are too small to account for the observed decrease of p in the filaments (see Fig. A.2).

(2) The smooth variations of ψ_{bg} in the background of B211 and Musca, by about 60° and 20° respectively, are associated with variations of p by 3-5 % (Fig. 10). The variations of ψ are likely to be associated with variations of γ of comparable amplitude that could contribute to the variations of p . We build on this idea to quantify the variations of γ that would be needed to account for the difference between p values for the filament and the background (at $r = 0$), p_{fil} and p_{bg} , listed in Table 2. The angles γ_{fil} and γ_{bg} of $\mathbf{B}$ with respect to the POS for the filament and the background are calculated, within the range 0° to 90° , from Eq. (6) written as

$$p = p_0 \cos^2 \gamma, \quad (7)$$

where $p_0 = p_{\text{dust}} R F$ may differ between the filament (p_0^{fil}) and the background (p_0^{bg}). The difference $\Delta\gamma = \gamma_{\text{fil}} - \gamma_{\text{bg}}$ depends on both p_0^{bg} and $f_0 = p_0^{\text{fil}}/p_0^{\text{bg}}$. For illustration we discuss two cases. First, in Table 3 for $f_0 = 1$, we give two values of $\Delta\gamma$ computed for extreme values of p_0^{bg} : the minimum value set by the observed polarization fraction at $r = 0$ and a maximum value

Table 3. Columns 2 and 3 give the values of p_0^{bg} and the corresponding $\Delta\gamma = \gamma_{\text{fil}} - \gamma_{\text{bg}}$ computed for $p_0^{\text{bg}} = p_0^{\text{fil}}$ (see Sect. 5.1.1). Column 4 gives the values of $\Delta\chi = |\chi_{\text{fil}} - \chi_{\text{bg}}|$ corresponding to the ψ_{fil} and ψ_{bg} values of Table 2 for the polynomial fits (pol3). Columns 5 and 6 give the relative angle between the PA of the filament and the $\mathbf{B}_{\text{POS}}$ angle in the filament and in the background, respectively. The PA of the filaments are given in Table 1.

		$p_0^{\text{bg}} \text{ }^{(1)}$	$\Delta\gamma$ [deg]	$\Delta\chi$ [deg]	$ \chi_{\text{fil}} - \text{PA} $ [deg]	$ \chi_{\text{bg}} - \text{PA} $ [deg]
Musca	..	0.12–0.2	39–14	12	82	70
B211	...	0.049–0.2	42–8	6	81	75
L1506	..	0.039–0.2	25–3	54	17	37

Notes. ⁽¹⁾ The smallest value of p_0^{bg} is the observed p_{bg} . The maximum value of 0.2 is close to the maximum dust polarization fraction observed by Planck at 353 GHz (Planck Collaboration Int. XIX 2015).

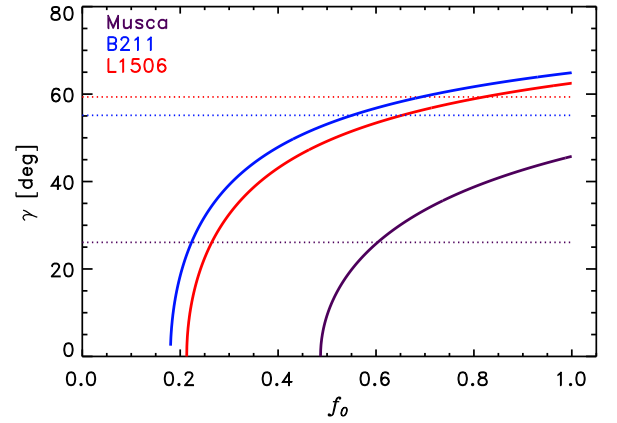


Fig. 12. Plot of the angles of $\mathbf{B}$ with respect to the POS γ_{bg} (dotted line) and γ_{fil} (solid line) computed with Eq. 7, as a function of $f_0 = p_0^{\text{fil}}/p_0^{\text{bg}}$ for $p_0^{\text{bg}} = 0.15$.

of 0.2. Second, in Fig. 12, we plot γ_{bg} and γ_{fil} versus f_0 for $p_0^{\text{bg}} = 0.15$. In this figure, the sign of $\Delta\gamma$ changes from negative to positive at different values of f_0 for each of the filaments. The orientation of $\mathbf{B}$ contributes to the decrease of the polarization fraction in the filament when $\Delta\gamma > 0$, i.e., $\mathbf{B}$ is closer to the LOS in the filament than in the background. By no way, this could be the rule to explain the low values of the polarization fraction that have been observed in all other filaments in dark clouds (e.g. Goodman et al. 1995; Sugitani et al. 2011; Cashman & Clemens 2014). We conclude that other factors than the mean magnetic field orientation contribute to the decrease of p in the filaments.

5.1.2. Fluctuation of the magnetic field orientation

Depolarization in filaments could result from the integration along the LOS of a large number of emission layers with different orientations of the magnetic field. Assuming the number of layers is proportional to the total column density N_{H} (Myers & Goodman 1991), we expect p to decrease for increasing N_{H} due to the averaging of the random component of the magnetic field (Jones et al. 2015). These models depend on the ratio be-

tween the strength of the random and of the mean components of the magnetic field (Jones et al. 1992). The steepest dependence, p scaling as $N_H^{-0.5}$, is obtained when the random component is dominant, in which case the dispersion of the polarization angle reaches its maximum value $\sigma_\psi^{\max}$ of 52° (Planck Collaboration Int. XIX 2015). In such a model, we expect the dispersion of ψ to be close to $\sigma_\psi^{\max}$ in the background and much smaller in the filament (see Fig. 9 in Jones et al. 1992). This prediction is inconsistent with our data because (1) $\sigma_{\psi_{bg}}$ is much smaller than $\sigma_\psi^{\max}$, and (2) it is comparable to and even smaller than $\sigma_{\psi_{fil}}$ (Table 2).

Moreover Fig. 11 shows that the variations of the magnetic field orientation are not random. Systematic variations of the polarization angle along and across the filaments must also exist on scales unresolved by *Planck* observations. Hence, we expect some depolarization from coherent changes of the field orientation in the beam and along the LOS. Spectroscopic observations of B211 show density and velocity structures on scales five times smaller than the *Planck* beam, and coherent over lengths of ~ 0.4 pc, i.e., two *Planck* beams (Hacar et al. 2013). Similar structures are anticipated to exist for the magnetic field.

Theoretical modelling is warranted to quantify the depolarization within the beam and along the LOS, and to test whether the structure of the magnetic field may account for the observed decrease of p in the filaments. The decrease of p due to the structure of the magnetic field has already been quantified for helical fields (e.g., Carlqvist & Kristen 1997; Fiege & Pudritz 2000). Other models could be investigated such as the magneto-hydrostatic configuration presented by Tomisaka (2014). Tomisaka (2015) describes the change in the polarization angle and the decrease of the polarization fraction produced by the pinching of the $\mathbf{B}$ -field lines by gravity within this model. Since the angular resolution of *Planck* does not resolve the inner structure of the filaments, observations with a higher angular resolution would be needed to fully test such models. This is the research path to understanding the role played by the magnetic field in the formation of star forming filaments.

5.2. Grain alignment efficiency and dust growth

Different mechanisms have been proposed to explain how the spin axes of grains can become aligned with the magnetic field. Alignment could result from magnetic relaxation (Davis & Greenstein 1951; Jones & Spitzer 1967; Purcell 1979; Spitzer & McGlynn 1979). However, the most recent theory stresses the role of radiative torques (RAT, Dolginov & Mitrofanov 1976; Draine & Weingartner 1996, 1997; Lazarian et al. 1997; Lazarian 2007; Lazarian & Hoang 2007; Hoang & Lazarian 2014). A number of studies interpret polarization observations in the framework of this theory (Gerakines et al. 1995; Whittet et al. 2001, 2008; Andersson & Potter 2010; Andersson et al. 2011, 2013; Cashman & Clemens 2014). The observed drop of p with column density has been interpreted as evidence of the progressive loss of grain alignment with increasing column density (Andersson 2015). However, this interpretation cannot be validated without also considering the impact of gas density on the grain size and shape.

Dust observations, both in extinction and in emission, provide a wealth of evidence for grain growth in dense gas within molecular clouds (e.g., Ysard et al. 2013; Roy et al. 2013; Lefèvre et al. 2014, as recent references). This increase of the typical size of large grains may contribute to the observed dependence of $\lambda_{\max}$, the peak of the polarization curve in extinction, on the visual extinction A_V (Wurm & Schnaiter 2002;

Voshchinnikov et al. 2013; Voshchinnikov & Hirashita 2014). Dust growth through coagulation and accretion also modifies the shape of grains, therefore their polarization cross-sections, and p_{dust} . So the study of the variation of polarization with A_V in dense shielded regions requires the modelling of both grain growth and alignment efficiency. Grain growth may allow for a sustained alignment up to high column densities (Andersson 2015). Thus, the product $p_{\text{dust}}R$ may not be changing much from the backgrounds to the filaments.

6. Conclusions

We have presented and analysed the *Planck* dust polarization maps towards three nearby star forming filaments: the Musca, B211, and L1506 filaments. These filaments can be recognized in the maps of intensity and Stokes Q and U parameters. We use these maps to separate the filament emission from its background, and infer the structure of the magnetic field from the polarization properties. This focussed study complements statistical analysis of *Planck* polarization observations of molecular clouds (Planck Collaboration Int. XX 2015; Planck Collaboration Int. XXXII 2014; Planck Collaboration Int. XXXV 2015).

Planck images allow us to describe the observed Stokes parameters with a two-component model, the filaments and their backgrounds. We show that it is important to remove the background emission in all three Stokes parameters, I , Q , and U to properly measure the polarization properties (p and ψ) intrinsic to the filaments. Both the polarization angle and fraction measured at the intensity peak of the filaments differ from their intrinsic values.

In all three cases, we measure variations in the polarization angle of the filaments (ψ_{fil}) with respect to that of their backgrounds (ψ_{bg}) and these variations are found to be coherent along the pc-scale length of the filaments. The differences between ψ_{fil} and ψ_{bg} for two of the three filaments are larger than the dispersion of the polarization angles. Hence, these differences are not random fluctuations and they indicate a change in the orientation of the POS component of the magnetic field between the filaments and their backgrounds. We also observe coherent variations of ψ across the background and within the filaments. These observational results are all evidence for changes of the 3D magnetic field structure.

Like in earlier studies, we find a systematic decrease of the polarization fraction for increasing gas column density. For L1506 the change of ψ in the filament with respect to that of the background accounts for most of the observed drop of p in the filament. We argue that the magnetic field structure contributes to the observed decrease of the polarization fraction in the filaments. We show that the depolarization in the filaments cannot be due to random fluctuations of ψ because (1) the dispersion of ψ is small (10°) and much smaller than the value of 52° for a random distribution, and (2) it is comparable in the filaments and their corresponding backgrounds.

Variations of the angle of $\mathbf{B}$ with respect to the POS cannot explain the systematic decrease of p with N_H either, but unresolved structure of the magnetic field within the filaments may contribute to that decrease. Indeed, we find that the dispersion of ψ in the filaments is comparable to, and even larger than, that in the background. These fluctuations of ψ are not random but due to coherent variations along and across the filaments that trace the structure of the magnetic field within the filaments. The drop in p expected from the magnetic field structure does not preclude some contribution from variations of grain alignment with

column density. Theoretical modelling is needed to test whether the inner structure of the magnetic field may account for the observed decrease of p in the filaments. Modelling is also crucial to quantify the role that the magnetic field plays in the formation and evolution of star forming filaments.

The ordered magnetic fields implied by the small dispersion of the polarization angle measured inside and around the three filaments suggest that the magnetic field is dynamically significant at the scale of the clouds. This is consistent with recent studies showing that the relative orientation between $\mathbf{B}_{\text{POS}}$ and the column density structures changes systematically with column density (Planck Collaboration Int. XXXII 2014; Planck Collaboration Int. XXXV 2015). These results are also in agreement with the ordered morphology of magnetic fields observed from 100 pc to sub-pc scales (see e.g., Li et al. 2014).

Further analyses of a larger sample of filaments observed by Planck, but also higher angular resolution observations, are required to investigate the magnetic field structure in filaments. More extensive molecular line mapping of a larger sample of filaments is very desirable, in order to set stronger observational constraints on the dynamics of these structures, as well as to investigate the link between the velocity and the magnetic fields in molecular clouds. Comparison with dedicated numerical simulations will also be valuable in our understanding and interpretation of the observational results.

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Appendix A: A two-component model along the LOS

The observed polarized emission results from the integration along the LOS of Stokes Q and U parameters of linearly polarized emission. Thus the observed polarization angle and fraction correspond to mean values of the emission along the LOS, which can be represented by the superposition of various layers/components with independent properties. A simplified two-component model applies as a first approximation to interstellar filaments and their backgrounds.

A.1. Mean polarization angle along the LOS

Here, we estimate the difference between the polarization angle ψ observed towards the filament, resulting from the integration of the emission along the LOS, and the intrinsic polarization angle of the filament ψ_{fil} . This difference depends on the polarized intensity contrast of the filament with respect to that of the background.

The observed Q and U emission integrated over the filament and the background are

$$Q = P_{\text{bg}} (f_d \cos 2\psi_{\text{fil}} + \cos 2\psi_{\text{bg}}), \quad (\text{A.1})$$

$$U = P_{\text{bg}} (f_d \sin 2\psi_{\text{fil}} + \sin 2\psi_{\text{bg}}), \quad (\text{A.2})$$

where P_{bg} is the polarized emission of the background, and $f_d = P_{\text{fil}}/P_{\text{bg}}$ the polarized intensity contrast between the two components. If the two components have the same polarized intensities ($f_d = 1$) the observed polarization angle ψ is equal to the average value, as can be seen in Fig. A.1. When the filament polarized intensity contrast is larger than one ($f_d > 1$) and $|\psi_{\text{fil}} - \psi_{\text{bg}}| > 0$, the difference between ψ_{fil} and ψ decreases when f_d increases. For $f_d > 1$, this difference first increases with $|\psi_{\text{fil}} - \psi_{\text{bg}}|$ and then decreases when $|\psi_{\text{fil}} - \psi_{\text{bg}}|$ approaches 90° , while for $f_d < 1$, it increases with $|\psi_{\text{fil}} - \psi_{\text{bg}}|$. It is thus important to separate the components along the LOS, to access the underlying magnetic field orientation of the filament.

A.2. Depolarization from rotation of the POS component of the magnetic field

Here, we estimate the decrease of the polarized emission with respect to the total emission when two components with different field orientations overlap along the LOS.

For the simplified two-component model, the depolarization factor, F , can be expressed as

$$F = \frac{P}{P_{\text{fil}} + P_{\text{bg}}}, \quad (\text{A.3})$$

where P is the observed polarized emission summed over the filament and the background. Equation (A.3) is equivalent to

$$F^2 = \frac{P^2}{P_{\text{fil}}^2 + P_{\text{bg}}^2 + 2P_{\text{fil}}P_{\text{bg}}}, \quad (\text{A.4})$$

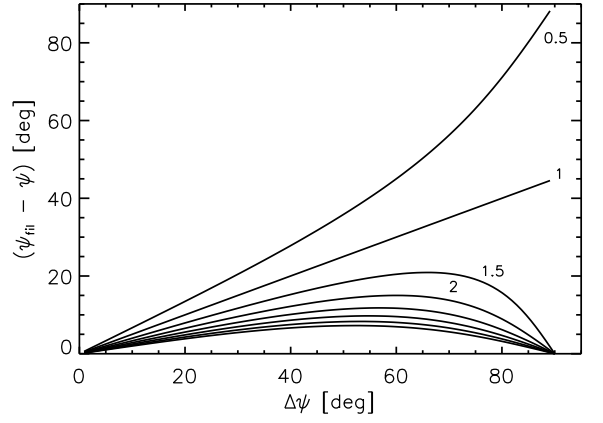


Fig. A.1. Difference between the intrinsic polarization angle of the filament, ψ_{fil} , and the observed polarization angle, ψ , as a function of $\Delta\psi = |\psi_{\text{fil}} - \psi_{\text{bg}}|$. The polarized intensity contrast of the filament is indicated close to the corresponding curves. Note that for $\Delta\psi = 90^\circ$ and $f_d = 1$, ψ is not defined and the resulting observed polarization fraction is null.

where $P^2 = U^2 + Q^2$ with $U = U_{\text{fil}} + U_{\text{bg}}$ and $Q = Q_{\text{fil}} + Q_{\text{bg}}$. Here Q and U are given by Eqs. (1) and (2) with the corresponding subscripts for the filament and the background. Thus

$$P^2 = P_{\text{fil}}^2 + P_{\text{bg}}^2 + 2P_{\text{fil}}P_{\text{bg}} \cos 2\Delta\psi, \quad (\text{A.5})$$

where $\Delta\psi = |\psi_{\text{fil}} - \psi_{\text{bg}}|$. These relations lead to

$$F^2 = 1 - \frac{2P_{\text{fil}}P_{\text{bg}}(1 - \cos 2\Delta\psi)}{P_{\text{fil}}^2 + P_{\text{bg}}^2 + 2P_{\text{fil}}P_{\text{bg}}}, \quad (\text{A.6})$$

which is equivalent to

$$F^2 = 1 - 2 \frac{1 - \cos 2\Delta\psi}{(1 + \beta)^2} \beta, \quad (\text{A.7})$$

for $\beta = P_{\text{bg}}/P_{\text{fil}}$. The maximal depolarization, i.e., the smallest F value $|\cos \Delta\psi|$, is obtained for $P_{\text{bg}} = P_{\text{fil}}$.

The observed polarized emission of two components, due to the combination of the Stokes Q and U parameters along the LOS, results in depolarization if the POS magnetic field rotates in one component with respect to the other. P is zero if $\Delta\psi = 90^\circ$ and the two components have the same polarized emission ($P_{\text{fil}} = P_{\text{bg}}$, see Fig. A.2). The depolarization factor towards the L1506 filament is $F \approx 0.6$ for $\Delta\psi = 54^\circ$ and a contrast of polarized emission of about one. For the Musca and B211 filament, F is close to unity since the POS angles in the filaments are close ($\Delta\psi \sim 10^\circ$) to that of their backgrounds (cf. Table 2).

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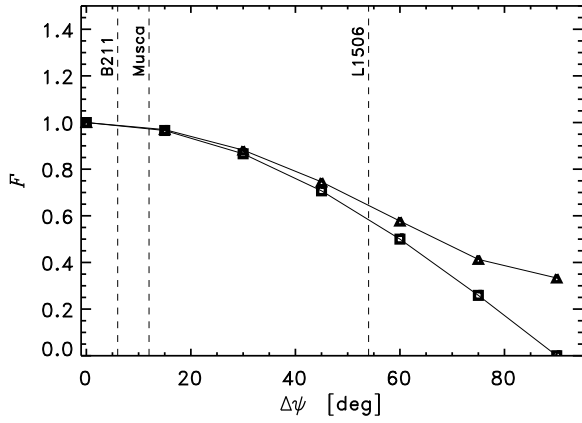


Fig. A.2. Depolarization factor due to the rotation of the field on the POS for two components with the same polarized intensity (squares) and with a contrast of two (triangles).

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