



Publication Year	2022
Acceptance in OA	2022-06-16T13:45:05Z
Title	Atomic and molecular gas from the epoch of reionization down to redshift 2
Authors	MAIO, Umberto, Péroux, Céline, Ciardi, Benedetta
Publisher's version (DOI)	10.1051/0004-6361/202142264
Handle	http://hdl.handle.net/20.500.12386/32357
Journal	ASTRONOMY & ASTROPHYSICS
Volume	657

Atomic and molecular gas from the epoch of reionisation down to redshift 2

Umberto Maio^{1,2}, Céline Péroux^{3,4}, and Benedetta Ciardi²

¹ INAF-Italian National Institute of Astrophysics, Observatory of Trieste, via G. Tiepolo 11, 34143 Trieste, Italy
e-mail: umberto.maio@inaf.it

² Max Planck Institute for Astrophysics, Karl-Schwarzschild-Str. 1, 85748 Garching bei München, Germany

³ European Southern Observatory, Karl-Schwarzschild-Str. 2, 85748 Garching bei München, Germany

⁴ Aix Marseille Université, CNRS, LAM (Laboratoire d'Astrophysique de Marseille) UMR 7326, 13388 Marseille, France

Received 20 September 2021 / Accepted 16 November 2021

ABSTRACT

Context. Cosmic gas makes up about 90% of the baryonic matter in the Universe and H₂ molecule is the most tightly linked to star formation.

Aims. In this work we study cold neutral gas, its H₂ component at different epochs, and corresponding depletion times.

Methods. We perform state-of-the-art hydrodynamic simulations that include time-dependent atomic and molecular non-equilibrium chemistry coupled to star formation, feedback effects, different UV backgrounds presented in the recent literature and a number of additional processes occurring during structure formation (COLDSIM). We predict gas evolution and contrast the mass density parameters and gas depletion timescales. We also investigate their relation to cosmic expansion in light of the latest infrared and (sub)millimetre observations in the redshift range $2 \lesssim z \lesssim 7$.

Results. By performing updated non-equilibrium chemistry calculations we are able to broadly reproduce the latest HI and H₂ observations. We find neutral-gas mass density parameters $\Omega_{\text{neutral}} \approx 10^{-3}$ and increasing from lower to higher redshift, in agreement with available HI data. Because of the typically low metallicities during the epoch of reionisation, time-dependent H₂ formation is mainly led by the H⁺ channel in self-shielded gas, while H₂ grain catalysis becomes important in locally enriched sites at any redshift. Ultraviolet (UV) radiation provides free electrons and facilitates H₂ build-up while heating cold metal-poor environments. Resulting H₂ fractions can be as high as ~50% of the cold gas mass at $z \sim 4-8$, in line with the latest measurements from high-redshift galaxies. The H₂ mass density parameter increases with time until a plateau of $\Omega_{\text{H}_2} \approx 10^{-4}$ is reached. Quantitatively, we find agreement between the derived Ω_{H_2} values and the observations up to $z \sim 7$ and both HI and H₂ trends are better reproduced by our non-equilibrium H₂-based star formation modelling. The predicted gas depletion timescales decrease at lower z in the whole time interval considered, with H₂ depletion times remaining below the Hubble time and comparable to the dynamical time at all z . This implies that non-equilibrium molecular cooling is efficient at driving cold-gas collapse in a broad variety of environments and has done so since very early cosmic epochs. While the evolution of chemical species is clearly affected by the details of the UV background and gas self-shielding, the assumptions on the adopted initial mass function, different parameterizations of H₂ dust grain catalysis, photoelectric heating, and cosmic-ray heating can affect the results in a non-trivial way. In the Appendix, we show detailed analyses of individual processes, as well as simple numerical parameterizations and fits to account for them.

Conclusions. Our findings suggest that, in addition to HI, non-equilibrium H₂ observations are pivotal probes for assessing cold-gas cosmic abundances and the role of UV background radiation at different epochs.

Key words. astrochemistry – dark ages, reionization, first stars – ISM: general

1. Introduction

About 90% of the baryons in the Universe are in the form of gas and most of this resides either in the cosmic space, constituting the so-called inter-galactic medium (IGM), or around galaxies, where it shapes the circumgalactic medium (CGM). Only a tiny but extremely relevant fraction of gas populates neutral high-density regions, where the local medium cools and fragments. There, a large portion of the chemical composition is represented by neutral hydrogen, HI, and molecular hydrogen, H₂, the most abundant molecule in the Universe. Different gas phases are not necessarily separated, as structure formation brings diffuse material into dense molecular regions, and spreads initially dense parcels into the hotter CGM and IGM. How the involved processes work in detail is still a matter of debate and the interplay between different phases has drastic consequences for the ionisation state of H and the global amount of H₂.

In the whole $z < 6$ epoch, the measured neutral-gas mass density normalised to the present-day critical density (neutral-gas density parameter) is $\Omega_{\text{neutral}} \sim 10^{-3}$ and increases towards higher redshifts (Noterdaeme et al. 2009; Zafar et al. 2013; Rhee et al. 2013; Sánchez et al. 2016; Jones et al. 2018; Hu et al. 2019; Wolz et al. 2021; Chen et al. 2021). H₂ molecules show a more complex behaviour and are notoriously more difficult to probe. Until a couple of years ago there was little reliable information at intermediate redshifts and no data at all for cold-gas H₂ content in the distant Universe; it is only recently that initial data from a number of observational campaigns based on for example VLA¹, ALMA², NOEMA³ or UKIRT⁴ have started to be used to set constraints on its cosmological evolution.

¹ <http://www.vla.nrao.edu/>

² <https://www.almaobservatory.org>

³ <https://www.iram-institute.org/EN/noema-project.php>

⁴ <http://wsa.roe.ac.uk/UKIRT.html>

The exact processes driving molecular build-up in different cosmological environments are not yet fully understood. For this reason, H_2 mass in targeted objects is usually inferred through empirical fits, based for example on emission from CO (Scoville & Solomon 1975; Dickman et al. 1986; Maloney & Black 1988; Hughes et al. 2017) or [C II] (Madden et al. 1997; Pak et al. 1998; Hollenbach & Tielens 1999) calibrated in the local Universe. Heavy elements and C-rich molecules have been detected in metal-enriched collapsing sites, suggesting that CO cores exist surrounded by a [C II] envelope where H_2 is self-shielded from photodissociating radiation (Röllig et al. 2006; Wolfire et al. 2010; Genzel et al. 2012; Bolatto et al. 2013; Zanella et al. 2018; Madden et al. 2020; Gong et al. 2020). Notwithstanding the uncertainties related to calibration techniques, completeness and conversion factors, the currently estimated H_2 molecular-mass density in the local Universe is $\rho_{\text{H}_2} \approx 6.8 \times 10^6 M_\odot \text{Mpc}^{-3}$ and accounts for about 20% of the total abundance of cold gas (Fletcher et al. 2021). Despite the large scatter of one order of magnitude or more among different studies, the H_2 mass density parameter Ω_{H_2} is observed to increase at $z \approx 0\text{--}3$, assembling its mass with almost no observed environmental dependence (Darvish et al. 2018; Tadaki et al. 2019; Garratt et al. 2021), and has been found to mimic the cosmological star formation rate (SFR) density at higher z (Decarli et al. 2020; Riechers et al. 2020a). These observations highlight the longstanding need to explore the origin of the large supply of H_2 gas required to sustain star formation at different z (Rodighiero et al. 2019; Tacconi et al. 2020; Hunt et al. 2020) and question the ability to explain the large H_2 fractions (above 50%) detected in galaxies around $z \sim 4\text{--}6$ (Dessauges-Zavadsky et al. 2020; Boogaard et al. 2021) in a primordial, presumably metal-poor gas.

From a theoretical point of view, cold gas plays a key role in cooling and fragmentation. It hosts the conversion from atomic to molecular phase, through which it fuels collapse and star formation (Saslaw & Zipoy 1967; Peebles & Dicke 1968). Despite the well-determined HI observational trend, a thorough understanding of its physical behaviour over cosmological history has yet to be obtained. H-derived molecules are crucial for gas chemistry evolution (see e.g., Bromm & Yoshida 2011; Girichidis et al. 2020, for reviews), because they supply low-temperature coolants to cosmic gas and are the main drivers of gas depletion timescales. A full assessment of H_2 evolution in different epochs is elusive because of both a lack of observational data until recently and the large computing power needed to perform detailed chemistry calculations within three-dimensional simulations. A correct evaluation of cold-gas fractions is sensitive to a number of cooling and heating processes due to either small-scale physics or large-scale events (Maio 2021). Numerical analyses typically predict lower-than-observed HI mass densities and experience difficulty in reproducing their increasing trend in redshift at $z \approx 2\text{--}6$. Accurate chemistry calculations following H_2 formation and the consequent run-away cooling regime require a full time-dependent ‘non-equilibrium’ approach that is computationally expensive and hence not widespread within numerical implementations of cosmological simulations. Such an approach has so far been employed to study mainly primordial epochs (Abel et al. 1997; Yoshida et al. 2003; Maio et al. 2010; Wise et al. 2012b; Muratov et al. 2013; Skinner & Wise 2020), while non-equilibrium evaluations for Ω_{neutral} , Ω_{H_2} , and depletion times during and after the epoch of reionisation are still missing.

The main channels for H_2 production in pristine media, mainly composed of H, He, and electrons, are based on catalysis

of intermediate species interacting with H, with possible photon emission accompanying recombination (Lepp & Shull 1984; Galli & Palla 1998), i.e. H^- catalysis ($\text{H} + \text{e}^- \rightarrow \text{H}^- + \gamma$ and $\text{H}^- + \text{H} \rightarrow \text{H}_2 + \text{e}^-$) and H_2^+ catalysis ($\text{H} + \text{H}^+ \rightarrow \text{H}_2^+ + \gamma$ and $\text{H}_2^+ + \text{H} \rightarrow \text{H}_2 + \text{H}^+$). While these processes are dominant at intermediate densities below 10^4 K or in recombining gas where free charges are available, three-body interactions ($3\text{H} \rightarrow \text{H}_2 + \text{H}$) could further contribute in dense neutral media.

The picture is even more complex for metal-rich environments, because metallicity (Z) evolution and dust grain catalysis might influence H_2 abundances ($2\text{H} \rightarrow \text{H}_2$ on dust grains) – which also depend on the efficiency of photoelectric heating (e.g., Bakes & Tielens 1994) – whose effects on H_2 production at different cosmological epochs are currently uncertain. Cosmic-ray protons losing their energy in dense molecular gas (Goldsmith & Langer 1978) or in thinner photodissociating regions (Shaw et al. 2009) could heat the medium and affect early H_2 formation in a non-trivial way. Their possible influence on pristine primordial gas has been pointed out with basic semi-analytic calculations by Jasche et al. (2007). However, because of the poor information on the yield and rate of cosmic-ray heating at that time, its impact has not been simulated within three-dimensional numerical simulations of early structure formation and the implications on (non-equilibrium) HI and H_2 masses are still unknown.

Feedback mechanisms can remove local gas mass and inject entropy into the surrounding medium (e.g., Nagamine et al. 2004). As UV photons are capable of dissociating molecules and ionising neutral atoms in non-shielded regions, the build-up of a UV background determined by forming structures in the first gigayear (Gyr) at redshift $z \gtrsim 6$ affects the gas thermal state as well as HI and H_2 density parameters. Gas self shielding (e.g., Draine & Bertoldi 1996; Rahmati et al. 2013; Hartwig et al. 2015; Wolcott-Green et al. 2017; Ploekinger & Schaye 2020; Luo et al. 2020; Walter et al. 2020) limits the ability of UV radiation to penetrate dense material and preserves HI or H_2 fractions in star forming regions. However, the relevance and the relative effects of the two main (HI and H_2) shielding processes for chemical abundances in cosmic environments need to be further explored.

In addition, stellar evolution modulates the whole baryon cycle depending on stellar initial mass function (IMF), metal yields, and lifetimes. The shape of the IMF has implications for the resulting stellar population, its chemical patterns, and the galaxy luminosity function (Leitherer et al. 1999; Bruzual & Charlot 2003; Vazdekis et al. 2010; Tescari et al. 2014; Mancini et al. 2015, 2016; Ma et al. 2015, 2017a; Valentini et al. 2019b).

Modifications in the supernova (SN) efficiency and/or in the mechanical feedback can affect the whole energetics of the picture at all times and induce variations in the amount of gas mass expelled from the collapsing regions into the IGM (Maio et al. 2011a; Campisi et al. 2011), with possible consequences on atomic and molecular species (Ω_{neutral} and Ω_{H_2}).

More or less powerful sources alter the ionisation state of the IGM and suppress gas cooling depending on the strength of radiative feedback and HI or H_2 shielding parameterisations (Draine & Bertoldi 1996; O’Shea & Norman 2008; Petkova & Springel 2011; Petkova & Maio 2012; Wise et al. 2012a; Rahmati et al. 2013, 2015; Sternberg et al. 2014; Maio et al. 2016; Wolcott-Green et al. 2017; Jones & Bate 2018; Shull et al. 2021).

To what extent all of these processes affect the overall molecular chemistry in realistic environments and at different redshifts is a matter of debate (Genel et al. 2014;

Furlong et al. 2015; Pallottini et al. 2017; Davé et al. 2017, 2019; Donnari et al. 2019). In this respect, dedicated numerical analyses must be carried out to interpret available data in order to explore the role of the various physical phenomena that condition the manifold regimes of cosmic environments. With the present study, we shed light on the evolution of cosmic atomic and molecular gas by interpreting recent, new, state-of-the-art observations and by modelling HI and H₂ species in the frame of high-resolution N -body hydrodynamical simulations that include full time-dependent non-equilibrium chemistry, star formation feedback, and stellar evolution. A further goal of our study is to show how neutral and molecular gas densities and corresponding depletion times are modulated by different UV radiation fields, HI or H₂ gas self-shielding, stellar population parameters, and the local processes affecting cosmic chemistry in different epochs.

We adopt a flat Λ CDM cosmological model, consistently with cosmic microwave background data (Komatsu et al. 2011), and use a present-day expansion parameter normalised to $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$ of $h = 0.7$. Baryon, matter, and cosmological-constant density parameters are assumed to be $\Omega_{0,b} = 0.045$, $\Omega_{0,m} = 0.274$ and $\Omega_{0,\Lambda} = 0.726$, respectively. The spectral parameters are $\sigma_8 = 0.8$ for the $z = 0$ mass variance within $8 \text{ Mpc } h^{-1}$ radius and $n = 0.968$ for the slope of the primordial power spectrum, consistent with the latest *Planck* results (Planck Collaboration VI 2020). The present-day cosmological critical density is $\rho_{0,\text{crit}} \approx 277.4 h^2 M_{\odot} \text{ kpc}^{-3}$.

The paper is organised as follows. Details on observational data, numerical implementations, and data analysis are given in Sect. 2; results are presented in Sect. 3 and discussed in Sect. 4; and conclusions are summarised in Sect. 5.

2. Method

In the following we present the most recent observations of cold atomic and molecular gas, the theoretical models implemented (comprising several physical processes newly included in the simulations), and a comprehensive list of all our runs.

2.1. Observations

To quantify the masses of HI and H₂ at various epochs, different authors use either mass densities ρ_{HI} and ρ_{H_2} (in $M_{\odot} \text{ Mpc}^{-3}$) or the corresponding dimensionless Ω_{HI} and Ω_{H_2} mass density parameters. The evolution of the entire amount of cold (below 10^4 K) neutral gas density, ρ_{neutral} , can be obtained by correcting H-based measurements by helium content, that is, by scaling HI masses by a factor of 1.3 (e.g., Crighton et al. 2015). In the following, we discuss neutral and molecular gas in terms of $\Omega_{\text{neutral}} = \rho_{\text{neutral}}/\rho_{0,\text{crit}}$ and $\Omega_{\text{H}_2} = \rho_{\text{H}_2}/\rho_{0,\text{crit}}$. In practice, these parameters correspond to the mass fraction of the considered species multiplied by $\Omega_{0,b}$.

We consider HI data at $z \lesssim 5$, as collected by Péroux & Howk (2020) (hereafter PH20) and shown in their Table 1, which rely on low- z 21 cm emission ($z \lesssim 0.4$) and high- z quasar absorption data. At low redshift, 21 cm emission analysis and spectral stacking are performed on data from 2dFGRS (Delhaize et al. 2013), WSRT (Rhee et al. 2013; Hu et al. 2019), GMRT (Rhee et al. 2016, 2018; Bera et al. 2019), Arecibo/ALFA (Hoppmann et al. 2015), and ALFALFA (Jones et al. 2018) observational programs. The present-day estimated value of the HI mass density parameter is $\approx (4.02 \pm 0.26) \times 10^{-4}$ (Hu et al. 2019). High-redshift measurements are obtained using data from high-resolution spectroscopic surveys of tens

of objects performed at the VLT (Zafar et al. 2013), Calar Alto/CALIFA (Sánchez et al. 2016), HST (Rao et al. 2017), and lower-resolution spectra of hundreds or thousands of objects recorded by SDSS (Noterdaeme et al. 2009, 2012; Crighton et al. 2015). The HI density evolution is quite smooth, increasing by a factor of ~ 3 from the present up to $z \approx 5.3$ (see Fig. 3). Mass density parameters for cold neutral gas vary within ~ 0.5 and $\sim 1.4 \times 10^{-3}$ and can be fitted by Eq. (13) in Péroux & Howk (2020): $\Omega_{\text{neutral}} = (4.6 \pm 0.2) \times 10^{-4} (1+z)^{0.57 \pm 0.04}$.

Up-to-date H₂ mass densities at different z (for any given observational programme) are found in Riechers et al. (2020a,b) (VLASPEC, COLDz), Decarli et al. (2020) (ASPECS), Lenkić et al. (2020) (PHIBBS-2), Garratt et al. (2021) (UKIDSS-UDS), and Hamañowicz et al. (2021) (ALMACAL-CO). Some of these are also present in the compilation by Péroux & Howk (2020). Upper limits at $z \approx 0$ –2 are provided by Klitsch et al. (2019) (ALMACAL-absorption, ALMACAL-abs hereafter) and impose $\rho_{\text{H}_2} < 10^{8.39} M_{\odot} \text{ Mpc}^{-3}$, corresponding to $\Omega_{\text{H}_2} < 1.81 \times 10^{-3}$. This value is much higher than early Herschel PEP lower limits of molecular-mass density parameters $\gtrsim 10^{-5}$ inferred through indirect methods for gas at $z \lesssim 3$ (Berta et al. 2013). The currently established present-day value of $\rho_{\text{H}_2} \approx 6.8 \times 10^6 M_{\odot} \text{ Mpc}^{-3}$ is obtained by Fletcher et al. (2021) (xCOLDGASS) and corresponds to $\Omega_{\text{H}_2} \approx 5 \times 10^{-5}$ with a relative error of a factor of 2. ALMA and VLA observational programmes determined an increasing Ω_{H_2} trend from $\Omega_{\text{H}_2} \approx 5 \times 10^{-5}$ at $z \approx 0$ to values of $\sim 10^{-4}$ at $z \approx 2$ –3 (Decarli et al. 2020; Riechers et al. 2020a). Infrared UKIDSS-UDS constraints (Garratt et al. 2021) confirm existing data, finding molecular-mass densities of $\rho_{\text{H}_2} \approx 2 \times 10^7 M_{\odot} \text{ Mpc}^{-3}$ (i.e. $\Omega_{\text{H}_2} \approx 1.5 \times 10^{-4}$) at $z \approx 2$. H₂ fractions of up to 50%–60% in galaxies at redshift $z \sim 4$ –6 have recently been reported by for example Dessauges-Zavadsky et al. (2020), although H₂ densities within 1σ confidence levels decrease down to $\Omega_{\text{H}_2} \sim 10^{-5}$ towards $z \approx 7$ (Riechers et al. 2020b). The derived Ω_{H_2} values at low z span more than two orders of magnitude, from 10^{-6} to a few times 10^{-4} , but are more robust at $z \gtrsim 2$. In practice, the overall ensemble of recent Ω_{H_2} observational findings reveal a variety of values ranging between 10^{-3} and 10^{-6} in the $z \approx 0$ –7 range and the shape of the resulting Ω_{H_2} evolution is completely different from the smooth Ω_{neutral} one. A list with the detailed values derived by different observational programs is presented in Appendix A (Table A.1).

From ρ_{neutral} and ρ_{H_2} , it is possible to derive the corresponding depletion times, $t_{\text{depl,neutral}} = \rho_{\text{neutral}}/\dot{\rho}_{\star}$ and $t_{\text{depl,H}_2} = \rho_{\text{H}_2}/\dot{\rho}_{\star}$, where $\dot{\rho}_{\star}$ is the cosmic star formation rate density.

2.2. Theoretical models

In order to interpret observational data in a robust way, we ran and analysed a number of numerical simulations based on N -body and hydrodynamical calculations with an extended version of the parallel code P-GADGET3 (Springel 2005) modified to address cold-gas atomic and molecular content in detail over different cosmological epochs (COLDSIM). Besides gravity and smoothed-particle hydrodynamics, the code contains a self-consistent time-dependent treatment of atomic and molecular chemistry for e^{-} , H, H⁺, H⁻, He, He⁺, He⁺⁺, H₂, H₂⁺, D, D⁺, HD, HeH⁺, which follows—in non-equilibrium conditions—a network of reactions for species ionisation, recombination, and dissociation (Abel et al. 1997; Yoshida et al. 2003; Maio et al. 2007). Here the network has been extended to account for the main processes taking place from the epoch of reionisation down to lower

redshift and these are coupled to star formation, stellar evolution, and heavy-element enrichment of He, C, N, O, Ne, Mg, Si, S, Ca, Fe, and so on from SN II, AGB, and SN Ia phases (Tornatore et al. 2007, 2010; Maio et al. 2010, 2011a). In the following sections we describe in more detail the chemical processes included in the original version of the code, as well as the additional processes included for a better modelling of cold-gas evolution.

2.2.1. Basic chemistry evolution

Non-equilibrium chemistry is followed through a set of first-order differential equations accounting for creation and destruction processes, as well as corresponding heating or cooling, as described by Maio et al. (2010, 2016) for example. The number density evolution for each species and for each gas particle is computed by solving the differential equations through a backward difference scheme with an integration time of 0.1 times the actual time-step (to grant numerical convergence; Anninos et al. 1997).

Stellar evolution is followed for a range of stellar masses and initial metallicities. Stars with masses above $8 M_{\odot}$ explode as SNe II and inject a typical kinetic energy of 10^{51} erg into the surrounding medium, while lower mass stars evolve through an AGB or SNe Ia phase with consequent mass loss (Tornatore et al. 2007). Star formation is modelled stochastically (e.g., Katz 1992; Springel & Hernquist 2003) in particles with density above a threshold of 10 cm^{-3} and temperature below 10^4 K after the ‘loitering’ regime and the catastrophic runaway cooling phase (Maio et al. 2009). Wind feedback takes place with a reference wind velocity of 350 km s^{-1} , while wind particles are decoupled from hydrodynamics and treated in a collisionless fashion (i.e. they do not cool; Maio et al. 2011a) for a delay time after the initial kick of 0.025–0.1 times the Hubble time, t_H . Spreading of heavy elements during different stellar phases is traced for He, C, N, O, Ne, Mg, Si, S, Ca, Fe, and so on. Metal-dependent yields are taken from Woosley & Weaver (1995), van den Hoek & Groenewegen (1997), Woosley et al. (2002), and Thielemann et al. (2003), while stellar lifetimes follow Padovani & Matteucci (1993) (see also Sect. 2.1 in Maio et al. 2016, for more details). The reference initial mass function (IMF) has a Salpeter (1955) shape over the stellar-mass range $[0.1, 100] M_{\odot}$.

The chemical network is coupled to the insurgence of UV radiation according to available z -dependent tabulated photoheating and photoionisation rates. These are added to the local gas heating caused by ongoing exothermic chemical reactions and physical processes. Works in the recent literature suggest different epochs for the establishment of a UV background and different temporal evolution of the adopted UV rates, which we test by means of dedicated runs. The main physical differences among the UV models are related to the treatment of the possible sources of cosmic re-ionisation and the availability of observational data to constrain model parameters at various z . We adopt the standard literature prescriptions by Haardt & Madau (1996) (HM), as well as the most up-to-date modelling including latest high- z data by Puchwein et al. (2019) (P19) and Faucher-Giguère (2020) (FG20). While the HM case is a simple model based on early QSO data only, the FG20 model also includes the contributions from early galaxies with an onset of HI and HeII photoheating at $z \approx 8$ and 4, respectively (similarly to the Haardt & Madau 2012, where HI and HeII photoheating kicks in at $z \approx 9$ and 5) and seems to better reproduce the Ly α forest mean flux decrement in the low-redshift IGM (Christiansen et al. 2020). The rates provided by HM have a

fairly smooth evolution until $z \approx 6$, although updated analyses by P19, including contributions from both QSOs and galaxies, suggest rates that have a tail extending up to $z \approx 15$.

Although this setup is already enough to follow the time-dependent HI and H₂ evolution with a precision that is not commonly obtained in standard implementations of cosmic structure formation models, to evaluate the properties of cold gas in different environments even more accurately, additional processes that might influence chemical abundances in complex ways should be included, such as: HI and H₂ self-shielding from UV radiation, H₂ grain catalysis, photoelectric as well as cosmic-ray heating. In the following we discuss all these newly implemented processes separately.

2.2.2. Gas HI and H₂ self shielding

While UV radiation can easily penetrate thin media, gas self-shielding effects should be taken into account when estimating HI and H₂ fractions in dense gas.

For H₂ self shielding we adopt the formulae by Draine & Bertoldi (1996), who fit their results either by means of a single power law (their Eq. (36)) or by a slightly more accurate expression (their Eq. (37)). We also use the more recent results of the work by Wolcott-Green et al. (2017), which, similarly to Sternberg et al. (2014), is a reformulation of the study by Draine & Bertoldi (1996). Most runs discussed here include H₂ shielding according to Eq. (36) of Draine & Bertoldi (1996) unless otherwise stated. In the case of Wolcott-Green et al. (2017), the optimal scale at which to estimate the local H₂ column density, N_{H_2} , and related shielding have been investigated in depth by Luo et al. (2020). These latter authors showed that N_{H_2} can be quantified as $N_{\text{H}_2} = n_{\text{H}_2} \lambda_J / 4$, where n_{H_2} is the three-dimensional H₂ number density and λ_J the Jeans length. This was proven to be an excellent approximation. In Appendix B we show that different H₂ shielding implementations have a negligible effect on our results.

For HI self shielding, we rely on the redshift and density-dependent corrections proposed by Rahmati et al. (2013). We note that, while the authors provide corrections at $z \leq 5$, both observational data and theoretical investigations suggest the presence of cold shielded gas also at higher redshifts. Despite the numerical uncertainties discussed in the original paper, the redshift evolution of self-shielding corrections as a function of density presents only small (non-monotonic) variations, and deviations from the z -averaged mean/median values for any given density are modest. Therefore, to capture the overall behaviour of HI, we fit the median values of those shielding curves. As the redshift dependence is weak and in the absence of a better prescription, we extend such a relation to $z > 5$. The resulting density-dependent fitting expression is given in Appendix B (Eq. (B.1)). This nicely shows that gas with H number densities $n_{\text{H}} \lesssim 10^{-3} \text{ cm}^{-3}$ is almost unshielded (i.e. the correction factor is close to unity), while at larger number densities the effective photoionisation rate decreases by several orders of magnitude.

Thus, while we find that the implementation of gas self shielding in the simulations affects the resulting Ω_{neutral} and Ω_{H_2} (this is discussed in detail in Sect. 3), variations in its exact formulation have a minor impact.

2.2.3. H₂ dust grain catalysis

We coupled H₂ gas-grain catalysis to the non-equilibrium chemical network and followed it for different gas temperatures

and metallicities. Condensation of metals into dust grains can enhance H_2 formation via H abstraction, although the quantum modelling of H_2 formation on dust grains bears uncertainties of a factor of 2 (Bron et al. 2014). Chemical rates for H_2 gas-grain catalysis are expected to be of the order of $\sim 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ (Duley 1996) and generally scale with the sticking coefficient (i.e. the fraction of particles that adsorb to the grain surface), S_{H} , and the square root of gas temperature, $\sqrt{T}$. Cazaux & Tielens (2004) suggested a rate of $3 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ and a sticking coefficient following a second-order polynomial that depends on the adopted grain temperature, T_{gr} (Hollenbach & McKee 1979). Based on the work by Tielens & Hollenbach (1985), Omukai et al. (2005) propose an H_2 rate of $6 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ for gas at 300 K (corresponding to about $3.5 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ at 100 K) and the same sticking coefficient as Hollenbach & McKee (1979). Similar approaches were later used by Tomassetti et al. (2015) and more recently by Sillero et al. (2021) for example. Updated quantum-mechanical calculations by Thi et al. (2020) find a value of $3.74 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ for a gas at 80 K assuming a constant S_{H} of unity. Broadly speaking, all these results are in line with observational constraints of $3\text{--}4.5 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ (Jura 1975a,b; Gry et al. 2002), although the value by Thi et al. (2020) does not incorporate a temperature-dependent S_{H} . Gas-grain energy losses scale proportionally to $\sqrt{T}(T - T_{\text{gr}})$, and therefore contribute to gas heating or cooling depending on both T and T_{gr} . On the basis of Milky Way calibrations, the normalisation is expected to be $\sim 10^{-33} \text{ erg s}^{-1} \text{ K}^{-3/2} \text{ cm}^3$, with an error at low Z of roughly 1 dex. Such large deviations introduce a remarkable degree of freedom in the parameter study, suggesting for example that variations of the dust-to-gas ratio within a factor of 10 would still be consistent with the constraints. For this reason, the exact shape and Z scaling of dust-induced H_2 formation and cooling/heating rates have long been debated in the literature (Hollenbach & McKee 1989; Omukai et al. 2005; Draine & Li 2007; Goldsmith et al. 2011; Krumholz & Gnedin 2011; Glover & Clark 2012).

Here, we adopt an H_2 formation rate of $3.5 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$ at 100 K scaled by $\sqrt{T}$ and S_{H} (Hollenbach & McKee 1979; Cazaux & Tielens 2004) (see Appendix C) to update the H_2 abundances employed in the cooling/heating calculations (Omukai et al. 2005). As observational determinations are mainly based on data from the Milky Way, we scale the rates linearly with Z at metallicities different from solar. As a fiducial value, we assume $T_{\text{gr}} = 75 \text{ K}$ at all z . Nevertheless, we additionally check alternative hypotheses (see Appendix C), namely a lower and a higher value of 40 K and 120 K, respectively, both consistent with observational constraints and theoretical estimates of grain properties. Indeed, local determinations of T_{gr} are related to gas surrounding nearby early-type stars (60–120 K) and photodissociation regions (65 K for $\theta^1 \text{ Ori C}$). Instead, theoretical estimates refer to H abstraction modelling on a perfect surface (75 K) or completely imperfect surface (44 K). Updated observational best-fit values at different redshifts are $\sim 41 \text{ K}$ at $z \simeq 4.5$ and $38\text{--}43 \text{ K}$ at $z \simeq 5.5$ (Khusanova et al. 2021; Faisst et al. 2020). To study the effects of an evolving T_{gr} , we also consider either grain temperatures varying as the CMB temperature, i.e. $T_{\text{gr}}(z) = T_{0,\text{CMB}}(1 + z)$ with $T_{0,\text{CMB}} \simeq 2.7 \text{ K}$, or varying in accordance to the energy balance between CMB radiation and dust grain power-law emission (Draine & Lee 1984), i.e. $T_{\text{gr}}^{4+\beta}(z) = T_{0,\text{gr}}^{4+\beta} + T_{0,\text{CMB}}^{4+\beta}[(1 + z)^{4+\beta} - 1]$, with present grain temperature $T_{0,\text{gr}} = 18 \text{ K}$ (da Cunha et al. 2013) and $\beta \simeq 2$ emissivity index. We note that common β values are between

roughly 1 and slightly greater than 2, but the resulting $T_{\text{gr}}(z)$ is not very sensitive to particular choices. The adopted value is chosen in accordance with the latest ALMA determinations (da Cunha et al. 2021). We explore degeneracies and metallicity effects at different cosmological epochs, also implementing the possibility of adopting fixed values for Z (e.g., $0.01\text{--}1 Z_{\odot}$).

Different values for T_{gr} , either constant or z -dependent, cause local fluctuations in H_2 chemistry of comparable amplitude, but have little impact on the global Ω_{H_2} behaviour. Metallicity is relevant for values close to $Z_{\odot}$, which boost both local H_2 fractions (by one dex since $z \simeq 8$) and density parameters (by more than two dex at $z \gtrsim 10$ and by a factor of a few at $z \simeq 4$).

In practice, H_2 grain catalysis has a relevant local impact on metal-rich sites, while, generally speaking, its global role decreases at higher z as a result of the decreasing metallicity. Finally, it does not affect the global HI chemical history and Ω_{neutral} values do not vary significantly from the reference case.

2.2.4. Photoelectric heating

Gas-grain interactions are usually accompanied by photoelectric heating. This is one of the main heating processes of the diffuse interstellar medium (ISM) and is caused by the absorption of UV photons by dust grains which then re-emit electrons and heat up the surrounding gas. According to standard expressions commonly used in ISM investigations (Weingartner & Draine 2001), the photoelectric heating rate density can be written as a function of gas temperature, Habing parameter G_0 –quantifying the local UV field (Habing 1968)–, and electron fraction (Draine & Sutin 1987; Bakes & Tielens 1994). With the exception of Milky Way calibrations, the details of such process in different cosmological contexts are still unknown. We therefore either consider the fiducial constant case of $G_0 = 1.7$, or, because of the tight relationship between star formation and UV photon production, we scale it by the local SFR (Narayanan & Krumholz 2017), i.e. $G_0 \rightarrow G_0 \times \text{SFR}/\text{SFR}_{\odot}$, where $\text{SFR}_{\odot} \sim 2 M_{\odot} \text{ yr}^{-1}$ is the value of the Galactic SFR (Chomiuk & Povich 2011; Licquia & Newman 2015). A precise quantification of the local SFR depends on the IMF and different assumptions can lead to errors of up to 40%. This is smaller than the typical uncertainties on some chemistry rates (known within up to a factor of 2), and therefore the induced variations should not be dramatic. We verified that the HI and H_2 densities obtained with both prescriptions are very similar, with differences visible only on local scales (see details in Appendix D). We note that, while heating the surrounding gas, the photoelectric effect provides additional free electrons useful for the H^- channel. These charges react with H via radiative attachment and increase H_2 formation via associative detachment.

The H_2 abundances reached in the presence of photoelectric heating are higher by a factor of a few mostly at early times, while the overall effect on Ω_{neutral} is modest.

2.2.5. Cosmic-ray heating

Another source that likely plays a role in H_2 evolution is cosmic-ray heating. Cosmic rays are mostly constituted of high-energy protons usually formed in explosive SN events that can impact molecular-mass build-up during and after the epoch of reionisation. It is known that heating by cosmic rays is related to ionisation of atoms and the consequent production of free electrons. Each cosmic-ray proton ionises the medium generating slow electrons and these lead to second- or later-generation ionisation in two-thirds of the cases (causing an increase in the

yield of liberated energy by five-thirds) (Spitzer & Scott 1969; Opal et al. 1971). About 50% of the energy released goes into gas heating. Because of their relatively large abundances, the species mainly involved in the ionisation process and accounting for most of the gas heating are H, He, and H₂ (Glassgold et al. 2012), while others are almost irrelevant. Indeed, the probability that cosmic-ray protons interact with for example dust or heavy molecules is expected to be orders of magnitude smaller than that of interactions with H₂ molecules. As a reference, the dust cross-section per H nucleus in the diffuse ISM is $\sim 10^{-21} \text{ cm}^2$, while in the case of H₂ it is $\sim 10^{-17} \text{ cm}^2$. Even if interactions with dust were to occur, only 1% of them would produce photoelectrons (Dwek & Smith 1996). Gas heating due to cosmic rays is usually parameterized as a function of the heating yield and ionisation rate. A wide range of values exists in the literature for the cosmic-ray heating yield, which is estimated to be $\sim 7\text{--}20 \text{ eV}$ (Stahler & Palla 2004; Goldsmith & Langer 1978, respectively) when considering electron energies higher than 1 keV, but reach about 44 eV if including lower electron energies (Glassgold et al. 2012). As the normalisation of the transferred energy is weakly dependent on the local environment, we always assume 20 eV as the typical value. The ionisation rate is expected to be $\zeta \sim 10^{-17} \text{ s}^{-1}$ per H atom, although infrared (IR) measurements of $\zeta \gtrsim 10^{-16} \text{ s}^{-1}$ in dense molecular sites (Indriolo et al. 2007; Indriolo & McCall 2012; Hollenbach et al. 2012) demonstrated that it can vary with density and reach larger values. A new analysis by Thi et al. (2020) suggests a typical ionisation rate of $1.7 \times 10^{-17} \text{ s}^{-1}$ per H₂ molecule. Recent theoretical results by Padovani et al. (2018) show that ζ could be described by a decreasing function of the density, peaking at a value of $\sim 10^{-16} \text{ s}^{-1}$ at gas column densities of 10^{19} cm^{-2} (Neufeld & Wolfire 2017). This estimate is more than a factor of ten larger than that provided by Thi et al. (2020), but still consistent with SN energies of 10^{51} erg and with uncertainties related to the different derivation technique.

In our implementation, we couple cosmic-ray heating with non-equilibrium chemistry to handle both a constant $\zeta = 10^{-17} \text{ s}^{-1}$ and a density-dependent ζ , like the one expected by Padovani et al. (2018). In this latter case, we fit tabulated results of their model $\mathcal{L}$ in a friendly form (given in Appendix E). To constrain extreme behaviours, cosmic-ray heating is applied either to all gas particles in the simulated volume or to star forming particles only. Because of the lack of data for ionisation rates in regimes different from the local one, ζ is generally scaled by the local SFR, as it is linked to SN shocks in star forming regions.

While we refer the reader to Appendix E for more details on the impact of different prescriptions; here we simply mention that the inclusion of our reference cosmic-ray heating (i.e. a density-dependent ζ applied to star forming particles) only mildly affects the density parameters at all redshifts.

2.2.6. Star formation model

Finally, commonly used star formation implementations that convert gas into stars stochastically estimate the SFR relying on the ratio between the gas density above a given threshold, ρ_{th} , and a typical star formation time that scales with gas density. In particular, the star formation timescale can be written as $t_{\text{sf}} = t_{\text{sf},0}(\rho/\rho_{\text{th}})^{1/2}$, where the maximum star formation time $t_{\text{sf},0}$ is an empirical parameter that varies substantially between different observations. At each integration time, collisionless star particles are spawned stochastically with a probability given by $p = (m/m_{\text{star}})\{1 - \exp[-(1-\beta)x\Delta t/t_{\text{sf}}]\}$, where m is gas particles,

m_{star} is stellar particles, β is the fraction of short-lived stars that die as SNaE, x is the cold fraction, and Δt is the numerical time-step (Springel & Hernquist 2003). The resulting star formation rate associated to each gas parcel is then $\dot{M}_{\text{sf}} = (1-\beta)xm/t_{\text{sf}}$. Here we adopt a reference value of $t_{\text{sf},0} = 2 \text{ Gyr}$ (in line with Leroy et al. 2013; Tacconi et al. 2013, 2020). The value of m_{star} is estimated by assuming that each gas particle forms four stellar particles (four ‘generations’), β is computed according to the adopted IMF, and x follows Springel & Hernquist (2003), resulting in a value that is usually close to unity in high-density regions. In practice, all this means that at the threshold value the actual star formation time is $t_{\text{sf}} = t_{\text{sf},0}$ and the star formation probability p is small, typically being $\Delta t/t_{\text{sf}} \ll 1$. At larger densities, t_{sf} becomes shorter, while the star formation probability p increases. As we are able to follow detailed non-equilibrium H₂ evolution, we additionally implement an H₂-based approach in which the SFR is driven by the non-equilibrium H₂ density in each gas parcel above the star formation threshold of 10 cm^{-3} . In general, the H₂ star formation efficiency can be thought of as implicitly coded in the star formation timescale, and therefore efficiency values equal to (lower than) unity correspond to timescale values equal to (higher than) the reference timescale. We ran corresponding simulations and we discuss the results and their implications for HI and H₂ evolution in the following sections.

2.3. Numerical simulations

All the processes mentioned above and newly implemented in our theoretical framework have an impact on the number of free electrons or protons available for H₂ formation, in addition to increasing gas heating or cooling and associated species destruction or formation. Their net result in different environments and at different epochs needs to be investigated.

To this end, we ran a number of numerical simulations in a cubic volume of length $10 \text{ co-moving Mpc } h^{-1}$ (COLDSIM), as listed in Table 1. Gas and dark-matter fields are each sampled with 512^3 particles at an initial redshift of 100 (different initial redshifts have a modest effect on the results; e.g., Maio et al. 2011b). This setup corresponds to a resolution of $7.89 \times 10^4 M_{\odot}$ and $4.72 \times 10^5 M_{\odot}$, for gas and dark-matter particles, respectively. In our reference simulation (HM-HISSmed in Table 1), star formation happens in gas above 10 cm^{-3} with a Salpeter (1955) IMF; it has a SN efficiency of 0.1, wind velocity of 350 km s^{-1} , wind delay time of $0.025 t_{\text{H}}$, HM UV background, density-dependent HI self shielding according to Eq. (B.1), and H₂ self shielding by Draine & Bertoldi (1996) (their Eq. (36)). We ran additional simulations to explore and quantify the role of different assumptions (for UV background, star formation, and feedback effects related to IMF, SNe, or winds), as well as gas physics and chemistry processes (HI or H₂ shielding, H₂ formation channels, H₂ dust grain processes, cosmic-ray heating), as detailed in Table 1. The implications of the different HM, P19, and FG20 backgrounds (highlighted with different colours in the table and in the following figures) are addressed with dedicated HI-shielded or unshielded simulations. We note that most HI-shielded runs include HI self shielding according to Eq. (B.1) (and are denoted by the HISSmed suffix after the UV background name, i.e. HM-HISSmed, P19-HISSmed, and FG20-HISSmed), while HI self shielding according to the tables of Rahmati et al. (2013) is tested only in selected runs (denoted via the HISS suffix after the UV background name, i.e. HM-HISS, P19-HISS, and FG20-HISS). The gas physics and chemistry modelling described above was investigated while always using the HM

Table 1. Inputs to simulation models.

Properties (a)	Simulation run (b)	UV (c)	HI shielding (d)	H ₂ shielding (e)	IMF (f)	ε_{SN} (g)	Extra modules (h)
UV rate Modeling	HM	HM	–	DB96	S	0.1	–
	HM-HISS	HM	R13	DB96	S	0.1	–
	HM-HISSmed (ref)	HM	B.1	DB96	S	0.1	–
	P19	P19	–	DB96	S	0.1	–
	P19-HISS	P19	R13	DB96	S	0.1	–
	P19-HISSmed	P19	B.1	DB96	S	0.1	–
	FG20	FG20	–	DB96	S	0.1	–
	FG20-HISS	FG20	R13	DB96	S	0.1	–
	FG20-HISSmed	FG20	B.1	DB96	S	0.1	–
Star formation	HM-std	HM	–	DB96	S	0.1	Threshold 0.1 cm^{-3}
	HM-HISSmed-std	HM	B.1	DB96	S	0.1	Threshold 0.1 cm^{-3}
	HM-HISSmed-H2	HM	B.1	DB96	S	0.1	Non-equilibrium H ₂ -based
Gas physics & chemistry	HM-HISSmed-3b	HM	B.1	DB96	S	0.1	3-body processes
	HM-HISSmed-3b-DB2	HM	B.1	DB96 (Eq. (37))	S	0.1	3-body processes
	HM-HISSmed-3b-WG	HM	B.1	WG17	S	0.1	3-body processes
	HM-HISSmed-H ₂ ⁺	HM	B.1	DB96	S	0.1	H ₂ ⁺ channel only
	HM-HISSmed-none	HM	B.1	DB96	S	0.1	No H ₂ channels
	HM-HISSmed-cat-75-Zevol	HM	B.1	DB96	S	0.1	Catalysis at 75 K
	HM-HISSmed-cat-75-pe	HM	B.1	DB96	S	0.1	Catalysis at 75 K and photoelectric heating
	HM-HISS-cat-40-Zevol	HM	R13	DB96	S	0.1	Catalysis at 40 K
	HM-HISS-cat-75-Zevol	HM	R13	DB96	S	0.1	Catalysis at 75 K
	HM-HISS-cat-120-Zevol	HM	R13	DB96	S	0.1	Catalysis at 120 K
	HM-HISS-cat-Tcmb-Zevol	HM	R13	DB96	S	0.1	Catalysis at $T_{\text{CMB}}(z)$
	HM-HISS-cat-Tbeta-Zevol	HM	R13	DB96	S	0.1	Catalysis at $T_{\beta}(z)$
	HM-HISS-cat-75-Zsun	HM	R13	DB96	S	0.1	Catalysis at 75 K and $Z = Z_{\odot}$
	HM-HISS-cat-75-0.01Zsun	HM	R13	DB96	S	0.1	Catalysis at 75 K and $Z = 10^{-2} Z_{\odot}$
	HM-HISS-cat-75-Zt	HM	R13	DB96	S	0.1	Catalysis at 75 K and $Z = Z(t)$
	HM-cat-75-Zevol	HM	–	DB96	S	0.1	With $Z(t)$ -dependent cooling
	HM-HISSmed-cr	HM	B.1	DB96	S	0.1	Catalysis at 75 K
	HM-HISSmed-cr-P18	HM	B.1	DB96	S	0.1	Constant ζ , all gas
	HM-HISSmed-cr-P18sfr	HM	B.1	DB96	S	0.1	ζ by P18, ^(*) all gas
Feedback & IMF	HM-1	HM	–	DB96	S	1.0	–
	HM-0.5	HM	–	DB96	S	0.5	–
	HM-0.01	HM	–	DB96	S	0.01	–
	HM-w700	HM	–	DB96	S	0.1	Wind velocity of 700 km s^{-1}
	HM-wf	HM	–	DB96	S	0.1	Winds decoupled for $0.1 t_{\text{H}}$
	HM-Chabrier	HM	–	DB96	Ch	0.1	–
	HM-1-Chabrier	HM	–	DB96	Ch	1.0	–
	P19-1	P19	–	DB96	S	1.0	–
	P19-Chabrier	P19	–	DB96	Ch	0.1	–
	P19-1-Chabrier	P19	–	DB96	Ch	1.0	–

Notes. Blocks in the first column (a) collect, from top to bottom, runs with different implementation properties. Following columns refer to: simulation name (b), cosmological UV rates (c), HI shielding (d), H₂ shielding (e), IMF (f), SN energy fraction (g), and description of extra modules adopted besides basics ones (h). UV backgrounds are by [Haardt & Madau \(1996, HM\)](#), [Puchwein et al. \(2019, P19\)](#) or [Faucher-Giguère \(2020, FG20\)](#); HI shielding by [Rahmati et al. \(2013, R13\)](#) or Eq. (B.1); H₂ shielding by [Draine & Bertoldi \(1996, DB96\)](#), their Eq. (36) if not otherwise specified) or [Wolcott-Green et al. \(2017, WG17\)](#); IMF by [Salpeter \(1955, S\)](#) or [Chabrier \(2003, Ch\)](#). ^(*) Simple fit in Appendix E to the $\mathcal{L}$ model by [Padovani et al. \(2018\)](#).

background. For example, this choice was made when adopting (non-equilibrium) H₂-based star formation (HM-HISSmed-H2). Although our fiducial star formation threshold is 10 cm^{-3} , we made comparisons to investigate the impact on the H₂ mass density parameter of a standard low-density threshold of $\sim 0.1 \text{ cm}^{-3}$ with an HM background (HM-std and HM-HISSmed-std), finding that in this latter case H₂ fractions are not properly resolved. Similarly, we adopted the HM scenario to quantify the contribution of each H₂ formation channel by including in the reference run the three-body processes together with the H⁺ and H₂⁺ channels (HM-HISSmed-3b). H₂ self shieldings by [Draine & Bertoldi \(1996\)](#) (Eq. (37)) and [Wolcott-Green et al. \(2017\)](#) are tested in HM-HISSmed-3b-DB2 and HM-HISSmed-3b-WG runs, respectively. To isolate the implications of individual channels, two further tests were implemented, the first including the H₂⁺ channel only (HM-HISSmed-H₂⁺) and the second including none of the

H₂ channels (HM-HISSmed-none). A similar analysis was carried out for H₂ grain catalysis at different grain temperatures and metallicities (see Table 1), with or without HI shielding (HM-HISSmed-cat-75-Zevol, HM-cat-75-Zevol), or photoelectric heating (HM-HISSmed-cat-75-pe). Cosmic-ray heating with constant or density-dependent ([Padovani et al. 2018](#)) ionisation rate in shielded gas was explored by means of HM-HISSmed-cr and HM-HISSmed-crP18 simulations, respectively. For a more realistic analysis, we additionally considered the possibility that cosmic-ray heating is injected only in star forming parcels (HM-HISSmed-crP18sfr). We tested the effects linked to variations of the SN efficiency and IMF by simply employing unshielded UV backgrounds to maximise the impact of stellar feedback. Other features related to powerful winds (at 700 km s^{-1}) or winds recoupled after a longer time (wind delay time of $0.1 t_{\text{H}}$, 4 times the reference $0.025 t_{\text{H}}$) are explored as well. For each output

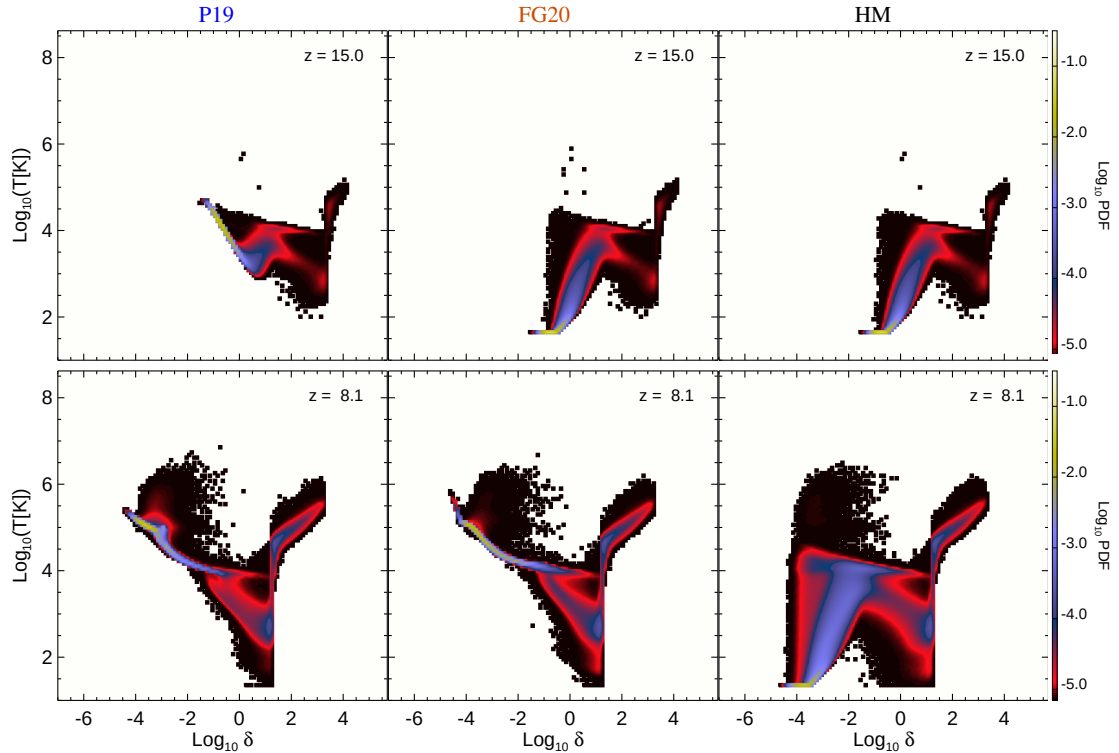


Fig. 1. Phase diagrams at redshift $z = 15.0$ (upper row) and $z = 8.1$ (lower row) for the simulations in Table 1 run with UV rates by Puchwein et al. (2019) (P19, left), Faucher-Giguère (2020) (FG20, centre), and Haardt & Madau (1996) (HM, right). The simulation data for temperature, T , and gas overdensity with respect to the gas mean, δ , have been gridded on a base-10 logarithmic scale. The colour coding refers to the total PDF.

time, cosmic structures are identified by means of a friends-of-friends algorithm with a linking length of 20% of the mean inter-particle separation. Substructures are identified by the Subfind algorithm (Dolag et al. 2009, and references therein) and are post-processed to trace: masses, positions, radii, velocities, star formation rates, temperatures, chemical abundances (of e^- , H, H^+ , H^- , He, He^+ , He^{++} , H_2 , H_2^+ , D, D^+ , HD, HeH^+ , C, N, O, Ne, Mg, Si, S, Ca, Fe, etc.), substructures, and all the relevant physical properties of each object. Our choices for initial conditions, box size, and resolution are determined by the necessary trade-off between the required accuracy of the physical descriptions implemented in the code and the numerical feasibility of the runs.

3. Results

In the following, we present the main results of our analysis of the simulations and their behaviour with respect to the observations described above.

3.1. Gas thermal state

We check the impact of the different UV backgrounds by looking at the effects on the thermal state of cosmic gas. Figure 1 shows the density–temperature diagram (phase space) for indicative runs in terms of gas overdensity, $\delta = \rho/\bar{\rho}$, where ρ is the mass density of each gas parcel and $\bar{\rho}$ the mean gas density. More specifically, phase space diagrams for three representative runs with P19, FG20, and HM UV rates are displayed and the colour code reflects the corresponding total probability density function (PDF). In these models, UV photoionisation is switched on at $z = 15.1$ (P19), 8.3 (FG20), and 6 (HM). At early times ($z = 15$), the trends in simulations run with FG20 and HM are similar, with

most of the gas being cold, below 10^4 K. This results from the natural evolution of gas chemistry in the absence of UV radiation. Low-density gas is shock-heated and the molecular fraction stays close to the initial-condition value (a few 10^{-6}). At higher densities, instead, non-equilibrium chemistry induces the rapid formation of H_2 molecules and consequent runaway cooling. In the P19 case, IGM or CGM-like material (around and below the mean density) has just been warmed up by the newly injected UV photoheating and experiences an inversion of its equation of state. However, high-density regions are little affected as a result of gas clumpiness in such regimes. How photoheating and photodissociation proceed depends on the chosen scenario, as highlighted by the lower panels at $z = 8.1$, when the gas thermal evolution has reached different stages: the traditional HM background has not heated cold, thin, cosmic gas, yet; in the FG20 and P19 panels, instead, photoheating is clearly effective since $z = 8.3$ for FG20 and $z = 15.1$ for P19. We note that the runaway molecular cooling branch is only mildly affected by UV radiation, as a consequence of the larger densities that shield H_2 molecules. At $z \lesssim 6$, all three models present phase diagrams similar to the latter case. We note that, irrespective of the chosen UV background rates, high-density regions behave in a similar way, dictated by local thermal processes rather than background radiation. Indeed, the star-forming branch exhibits the equation of state of SN-heated gas based on the multiphase ISM model of Springel & Hernquist (2003). This behaviour is caused by the SN energy released in the surrounding medium and is responsible for the increase in gas temperatures visible on the right of each the panel.

Collapsing star forming regions are more sensitive to feedback effects and the implications of different assumptions for feedback parameters might be relevant for the thermodynamical evolution of cosmic gas, independently of the adopted UV

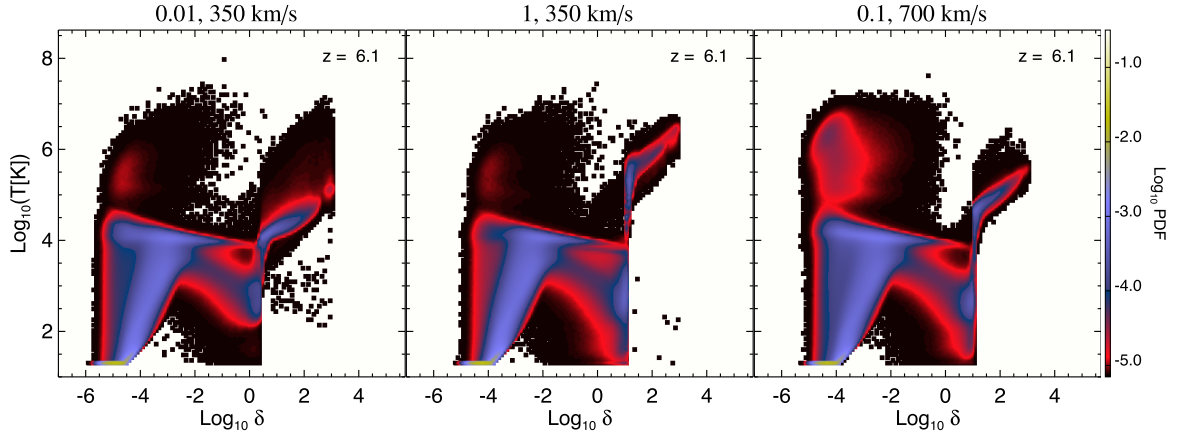


Fig. 2. Phase diagrams at redshift $z = 6.1$ in scenarios with HM background and, *from left to right*, a SN efficiency (wind velocity) of: 0.01 (350 km s^{-1}), 1 (350 km s^{-1}), and 0.1 (700 km s^{-1}). These are the runs HM-0.01, HM-1, and HM-w700, respectively.

prescriptions. As indicative examples, in Fig. 2 we show phase diagrams at redshift $z = 6.1$ for the runs with SN efficiencies of 0.01–1 and wind velocity of 350 or 700 km s^{-1} in the HM case. A low SN efficiency of 0.01 (left panel, HM-0.01) is incapable of removing dense material from the star forming regions (at $\text{Log}_{10}\delta \gtrsim 1$), where gas retains temperatures of 10^4 – 10^5 K without cooling further (red/blue branch). A higher efficiency of 1 (central panel, HM-1) removes more gas, as is clear from the probability distribution of the star forming branch (red region at $\text{Log}_{10}\delta \sim 1$ – 2.5). Such material circulates through the IGM and CGM again and becomes available for further cooling and fragmentation. The 0.1 case with the same winds (not plotted) features an intermediate behaviour. The results displayed in both the left and central panels have a wind velocity of 350 km s^{-1} . Stronger winds with velocities of for example 700 km s^{-1} (right panel with SN efficiency of 0.1, HM-w700) impact gas removal from star forming sites. In the case shown, dense material is ejected to outer regions more efficiently and abundantly populates the thin IGM at $\text{Log}_{10}\delta \lesssim -1$ and $T \gtrsim 10^5 \text{ K}$. Besides the role of wind velocity, other wind parameters, such as the wind delay time before re-coupling to hydrodynamics (e.g., $0.1 t_{\text{H}}$ adopted in HM-wf, instead of the reference $0.025 t_{\text{H}}$ adopted in Fig. 2), are expected to have less vital effects. The picture at different redshifts is qualitatively similar, as it is when assuming a Chabrier IMF (HM-Chabrier and HM-1-Chabrier), instead of a standard Salpeter IMF. Alternative UV rates for these models (e.g., P19, P19-1, P19-Chabrier, P19-1-Chabrier) show analogous behaviours, except for the mentioned (temporal) differences. These preliminary considerations highlight the main impact of different assumptions on the UV background and feedback effects, specifically on the thin cosmic medium. The implications for cold dense media (privileged sites hosting neutral and molecular gas) are analyzed in Sect. 3.2.

3.2. Density parameters

In this section, we focus on the evolution of mass density parameters for neutral gas, Ω_{neutral} , and molecular H_2 gas, Ω_{H_2} , as extracted from simulation outputs at different times, and compare them to state-of-the-art observational data (Sect. 2.1) in Fig. 3. Theoretical trends refer to runs with the reference implementation including time-dependent non-equilibrium abundance computations, a high-density threshold of 10 cm^{-3} for stochas-

tic star formation, stellar evolution, metal spreading, and H_2 self shielding. We distinguish between simulations accounting for HI self shielding, (HM-HISSmed, P19-HISSmed and FG20-HISSmed denoted by thick lines) and analogous unshielded results (HM, P19 and FG20 denoted by thin lines).

In the top panel, we focus on Ω_{neutral} . We can see that theoretical results increase smoothly with redshift at $z \approx 2$ – 5 , in broad agreement with observational data. UV radiation impacts our results after the onset of the UV background and leaves the signal from earlier epochs unaffected (as visible for all the UV models e.g., in Appendix G). In both HI shielded and unshielded HM scenarios, the cold mass surviving at $z \lesssim 6$ after photoionisation is turned on is only 5% of the original cold mass, corresponding to $\Omega_{\text{neutral}} \sim 10^{-3}$. As HI shielding preserves HI mass, the resulting Ω_{neutral} at $z \approx 2$ – 3 is larger by a factor of up to 2 with respect to the unshielded case. Although both curves are broadly consistent with the available data at $z \lesssim 5$, the unshielded run seems to predict a steeper evolution of cold gas. The shielded HM scenario is slightly above the 1σ error bars of observational data points. In the P19 and FG20 cases the UV model is turned on earlier, resulting in a larger effect of the associated feedback and flatter curves compared to those obtained with an HM background. In these cases, the predictions are slightly below 1σ observational determinations for the unshielded runs, while the corresponding shielded cases are roughly consistent with observational lower limits. The addition of further physical processes, as we see in the following, does not strongly affect Ω_{neutral} , whose values remain robustly close to the ones displayed in the figure and within the error bars of available data. We note that the displayed fitting expression by Péroux & Howk (2020), namely $\Omega_{\text{neutral}} \propto (1+z)^{0.57}$, is similar to other independent formulations finding $\Omega_{\text{neutral}} \propto (1+z)^{0.60}$ (Crighton et al. 2015) or $\Omega_{\text{neutral}} \propto (1+z)^{0.64}$ (Rao et al. 2017). Thus, uncertainties on the numerical fit do not affect our conclusions.

In the bottom panel of Fig. 3 we explore the outcome for Ω_{H_2} compared to the observational constraints (listed in Table A.1) by Hamanowicz et al. (2021) (ALMACAL-CO), Riechers et al. (2020a) (VLASPEC), Lenkić et al. (2020) (PHIBBS-2), Riechers et al. (2020b) (COLDz), Decarli et al. (2020) (ASPECS), and Garratt et al. (2021) (UKIDSS-UDS). For ALMACAL-CO, maximum and minimum values of preliminary estimates at $z < 2$ are shown. Darker to lighter shades correspond to 1, 2, and 3σ confidence levels by Péroux & Howk (2020). ALMACAL-abs upper limit in the $z \approx 0$ – 2 range is taken

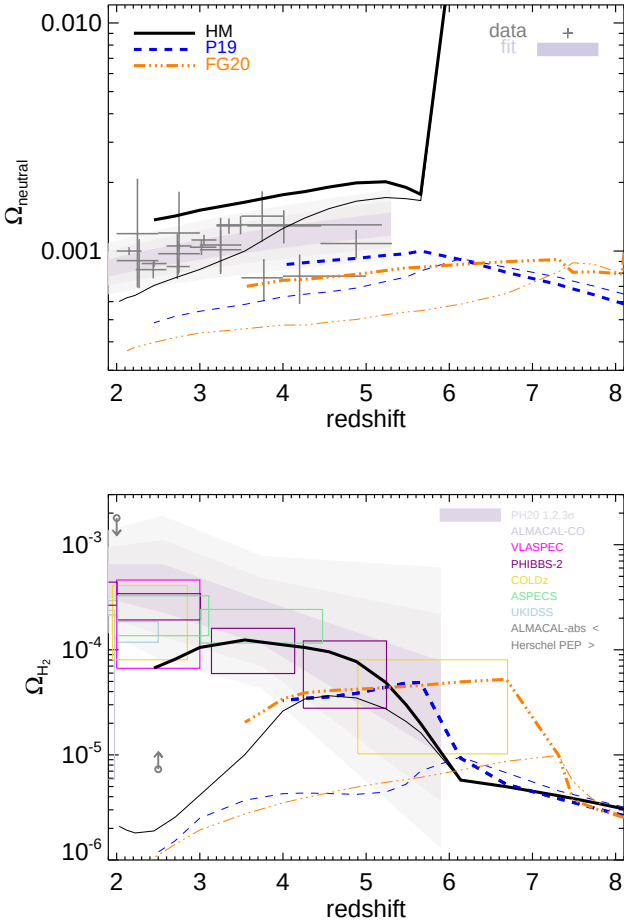


Fig. 3. *Upper panel:* redshift evolution of Ω_{neutral} compared to inferred values from HI observations with 1σ error bars (grey points) and corresponding fit (from darker to lighter shades) at 1 , 2 , and 3σ confidence levels (see Péroux & Howk 2020). The simulations considered are: HM-HISSmed (thick black solid lines), P19-HISSmed (thick blue dashed lines), and FG20-HISSmed (thick orange dot-dot-dot-dashed lines), and all include HI self shielding. As a comparison, corresponding unshielded runs with the same UV backgrounds (HM, P19 and FG20) are displayed by thin lines of the same colour and style. *Lower panel:* corresponding evolution of Ω_{H_2} , compared to the observational constraints listed in Table A.1 (PH20 1, 2, and 3σ confidence levels, shades; ALMACAL-CO, light grey; VLASPEC, magenta; PHIBBS-2, purple; COLDz, yellow; ASPECS, green; UKIDSS-UDS, cyan; ALMACAL-abs and Herschel PEP upper and lower limits, dark grey).

by Klitsch et al. (2019) while Herschel PEP most probable lower limit at $z \simeq 2-3$ is by Berta et al. (2013).

H_2 mass forms in cold high-density regions with rates depending on gas temperature and ionisation state. Therefore, as opposed to Ω_{neutral} , predicted values for Ω_{H_2} are very sensitive to the underlying chemical and physical modelling. We neatly see that HI shielding effects in the HM-HISSmed, P19-HISSmed, and FG20-HISSmed runs are responsible for largely increasing the amount of H_2 with respect to the corresponding unshielded HM, P19, and FG20 results. Indeed, the Ω_{H_2} parameter is enhanced by ~ 1 dex, while the HI mass increases by only a factor of up to 2. This reveals the highly non-linear nature of the involved chemical processes, as changes of a factor of a few in HI cause much larger variations in H_2 . Clearly, the unshielded HM, P19, and FG20 models produce excessive H_2 dissociation and are not consistent with the data (the related Ω_{H_2} values fall down to $\lesssim 2 \times 10^{-6}$ at $z \lesssim 3$, far from observational limits by

almost to two orders of magnitude). However, despite the inclusion of HI shielding, the P19 and FG20 scenarios feature an Ω_{H_2} evolution that flattens at $z \simeq 4-7$, hardly reaching $\Omega_{\text{H}_2} \sim 10^{-4}$. This is a result of the earlier onset of the UV background and more powerful rates associated to these two models at such epochs. Conversely, the HI-shielded HM model produces values closer to the observed ones by employing only the essential H_2 formation channels, which are able to enhance the H_2 mass density parameter at $z \simeq 4-6$ in the presence of a milder UV background. Indeed, the evolution of the H_2 density parameter is affected by the evolution of the photoionisation and photoheating rates adopted in the simulations. The P19 rates evolve smoothly from high redshift until $z \simeq 6$, where they get enhanced by more than three orders of magnitude, while the FG20 rates at $z \simeq 8$ go from zero to levels comparable to those of the P19 model. Although newly available free charges induce H_2 formation, on longer timescales the overall effect is H_2 disruption, in shielded as well as unshielded cases. The decline observed in Ω_{H_2} at lower redshift is linked to the stronger effect of both UV radiation and star formation, which destroy molecules through photoheating and stellar feedback. The latter is increasingly effective at later times (see e.g., lower- z trends for un-shielded models), while the former depends on the details of the UV background at different z . For an earlier and/or stronger UV background (e.g., P19 and FG20) H_2 suppression is more significant, albeit modulated by gas self shielding.

By looking at Ω_{H_2} data in light of our findings, one might think that the large dispersion in the observations at low redshifts (e.g., Klitsch et al. 2019; Decarli et al. 2019, 2020; Riechers et al. 2020b; Garratt et al. 2021) could be related to targeted objects found in conditions that are heterogeneous in terms of gas shielding, heating, ionisation, or photodissociating radiation (hence, the need for large statistical samples). In practice, the right combination of UV model and HI self shielding is needed to match both HI and H_2 data. A UV background turning on at $z \gtrsim 8$ seems to induce excessive feedback and predict too little cold gas. This suggests that either UV rates at those times should be lower than those adopted here or high- z gas self shielding should be stronger.

Typically, stochastic conversion of gas into stars is responsible for removing very dense gas parcels from collapsing material. Nevertheless, Ω_{neutral} and Ω_{H_2} parameters might be affected if gas-to-stars conversion involves particles that are still at relatively low density (below ~ 1 particle cm^{-3}). In this case, the abundance of HI and H_2 cannot grow significantly during their cooling process. To make sure that gas evolution through the cooling branch is followed properly and the amount of HI and H_2 formed is realistic, we have always used a density threshold of 10 cm^{-3} , as time-dependent non-equilibrium runaway cooling usually takes place in gas with densities $> 0.1 \text{ cm}^{-3}$ and temperatures $\sim 10^2-10^4 \text{ K}$. However, besides the density threshold, gas-to-star conversion is often assumed to depend on gas density, ρ , and a typical star formation timescale, t_{sf} (see Sect. 2.2.6). This means that the particle SFR is $\propto \rho/t_{\text{sf}}$. As H_2 molecules are the main drivers of star formation (and not simply the entire gas reservoir) and because we are able to follow their non-equilibrium chemical abundance precisely, in the following we employ the local H_2 density, ρ_{H_2} , as derived by our non-equilibrium calculations to estimate the particle SFR $\propto \rho_{\text{H}_2}/t_{\text{sf}}$ and related feedback effects (non-equilibrium H_2 -based star formation). In Fig. 4 we compare the resulting Ω_{neutral} and Ω_{H_2} parameters for such a scenario (HM-HISSmed- H_2 run) to the reference results (HM-HISSmed run). Although the evolution of Ω_{neutral} and Ω_{H_2} obtained with the H_2 -based approach is similar

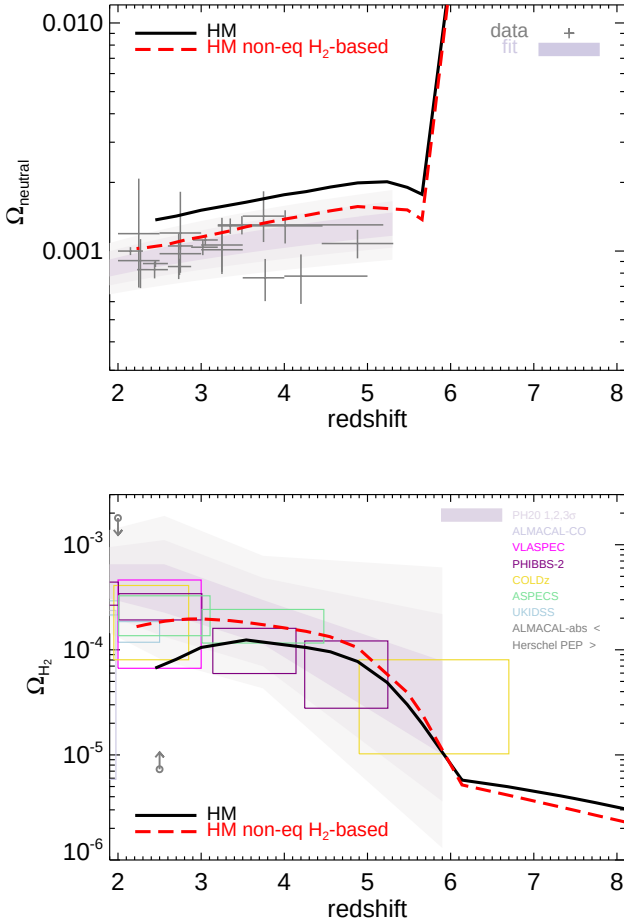


Fig. 4. *Upper panel:* Ω_{neutral} evolution for the non-equilibrium H_2 -based star formation model (red dashed line, HM-HISSmed-H2) with an HM background and compared to the reference run (solid black line, HM-HISSmed). *Lower panel:* corresponding Ω_{H_2} evolution. Observational determinations are listed in Table A.1 (see also text and Fig. 3).

to the reference one, it seems to be a better fit to observations of both gas components. With respect to the reference trends, Ω_{H_2} values are slightly higher as a consequence of the less effective star formation feedback. Consequently, HI is more easily converted into H_2 and the resulting Ω_{neutral} values are smaller.

We additionally investigated the role of individual H_2 formation channels, finding that H^- is a fundamental driver at all times, while three-body interactions are less important on large scales. Nevertheless, these latter are useful to reach large H_2 fractions of at least 50% (i.e. $\sim 67\%$ of the available H mass) even during the epoch of reionisation and explain the 50%–60% values at $z \sim 4$ –6 recently reported by for example Dessauges-Zavadsky et al. (2020) and Tacconi et al. (2018, 2020) (Appendix F). Including gas-grain processes coupled to the non-equilibrium molecular network and metal spreading leads to a more complete treatment of cold-gas chemistry, without substantially affecting our conclusions. Also, dust grains can enhance H_2 fractions by up to $\sim 50\%$ by $z \approx 7$, in line with observations (for a more detailed discussion see Appendices C and D), but are effective at relatively large metallicities. Heating due to cosmic rays formed in star forming regions is relatively localised and, regardless of the details of the ionisation rates, its impact remains at the 10% level (Appendix E). Feedback due to different SN efficiencies or wind parameterizations impact Ω_{neutral} and Ω_{H_2} , inhibiting –more or less efficiently– the amount of cold neutral and molecular gas

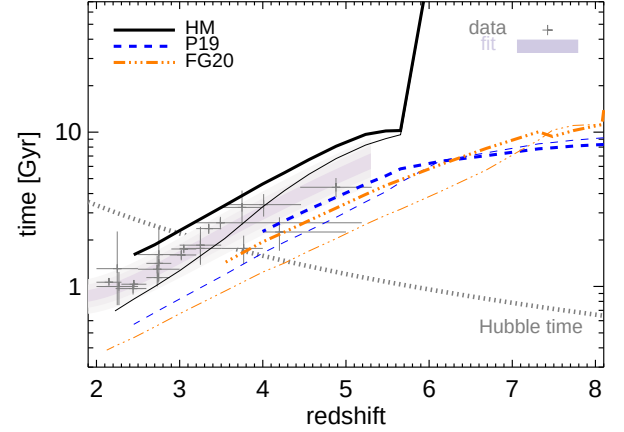


Fig. 5. Redshift evolution of the neutral-gas depletion times in simulations with HM, P19, and FG20 (solid, dashed and dot-dot-dot-dashed lines, respectively) UV backgrounds compared to depletion times with 1σ errors (grey points) derived from Ω_{neutral} observational data and 1, 2, and 3σ confidence levels (from darker to lighter shades) (see also Fig. 3). Results are for HI shielded (thick) and HI unshielded (thin) scenarios. The Hubble time (grey dotted line) is also shown.

available. Material in the distant IGM and CGM suffers only mild effects from these events (Appendices H and I).

In summary, we find that to accurately model cold gas and to reproduce the observed atomic and molecular abundances, it is crucial to follow the non-equilibrium chemistry of HI and H_2 self-shielded material down to densities of at least $\sim 10 \text{ cm}^{-3}$ and to resolve the gas runaway cooling. In this way, our results are in better agreement with observations than previous simulation predictions at high z .

3.3. Gas depletion times

Gas depletion times are useful tools with which to investigate the baryon cycle and its relation to cosmic expansion (often parameterized by the Hubble time, t_{H}). As hot gas is unlikely to collapse, it is natural to focus on cold neutral gas and on molecular H_2 -rich gas.

Figure 5 shows the cold-neutral-gas depletion time for different UV models compared to observational data and the Hubble time. For all the UV models, depletion times decrease with decreasing redshift, suggesting that typical cosmic structures can accumulate cold material that will eventually collapse and form stars. This qualitative behaviour is almost universal and little dependent on model details. Quantitatively, results from simulations including HI shielding are more consistent with the data, with values becoming lower than t_{H} at $z \lesssim 4$. Unshielded models with P19 and FG20 background radiation are only marginally different from observational constraints.

Figure 6 shows the corresponding H_2 depletion times compared to observational data. In this case, besides the Hubble time, we also plot the ‘dynamical’ time, t_{dyn} , defined as a fraction of 10% of the Hubble time, $t_{\text{dyn}} = 0.1 t_{\text{H}}$. This expression can be explained with simple dynamical arguments (see Appendix J) and is often quoted in observational studies (Lilly et al. 2013; Tacconi et al. 2020) as indicative of the evolution of a marginally stable rotating disk in which molecular cooling, gas fragmentation, and star formation should take place. In Fig. 6, H_2 global estimates agree well with observational results from alternative galaxy-based approaches that suggest a best-fitting trend of $t_{\text{depl},\text{H}_2}(z) = (1.6 \pm 0.5)(1+z)^{-(0.98 \pm 0.12)} \text{ Gyr}$ within 2σ error

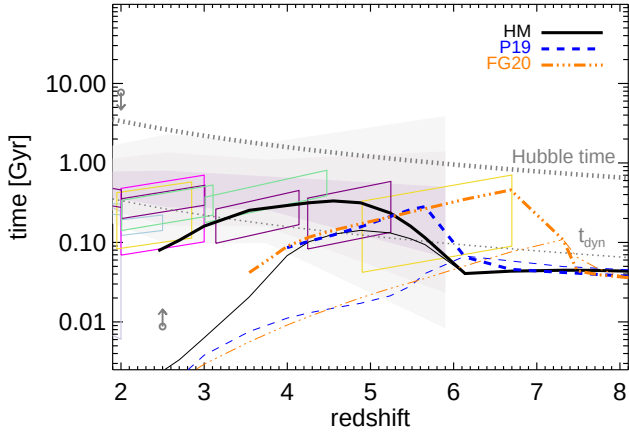


Fig. 6. Redshift evolution of the H_2 depletion time in simulations with HM, P19, and FG20 (solid, dashed and dot-dot-dashed lines, respectively) UV backgrounds. H_2 depletion times within 1σ range (slanted shapes), 1 , 2 , and 3σ confidence levels (from darker to lighter shades), and maximum and minimum values (grey arrows) are derived from Ω_{H_2} observational data and limits in Table A.1 and Fig. 3. The Hubble time (thick grey dotted line) and the dynamical time, t_{dyn} (thin grey dotted line) are also shown. Results refer to both HI shielded (thick) and HI unshielded (thin) scenarios.

bars (very close to t_{dyn}) and data dispersion of almost 1 dex (see Tacconi et al. 2020, who used existing literature data and ALMA archive molecular-mass detections up to $z \approx 5.3$). In line with studies of cosmic cold gas showing no explicit dependence on galaxy mass, size, or environment for galaxy-integrated depletion times (Darvish et al. 2018; Tadaki et al. 2019) and notwithstanding the operational costs to determine molecular masses, H_2 depletion times can track cosmic gas evolution if the star formation history is well known (Tacconi et al. 2020). Despite the relatively low scatter at $z \approx 2-4$ (between 0.1 and 1 Gyr), lower z determinations have a larger spread. Using available observational data, at $z \approx 0-2$ we find $t_{\text{depl}, \text{H}_2}$ comprised between 10 Gyr (ALMACAL-abs upper limits) and 0.01 Gyr (ASPECS and Herschel PEP lower limits). The latest UKIDSS data at $z \approx 2$ suggest values of around 0.1–0.3 Gyr. Interestingly, expected H_2 depletion times are always found below the Hubble time and often below the dynamical time. This is a more stringent constraint than the one derived from neutral-gas depletion times and supports the idea that cosmic structures form much beyond redshift $z \approx 6$. Thus, future observational efforts in the (sub)mm regimes, leading to observations of larger samples of high- z star forming galaxies, similar to those recently detected at $z \approx 6$ (Grupponi et al. 2020; Talia et al. 2021; Zavala et al. 2021), are required.

4. Discussion

In the previous sections, we investigate the role of different physical and chemical processes that could affect atomic and molecular cold-gas evolution. We tested three different UV backgrounds (HM, P19, FG20) coupled to non-equilibrium chemistry and find that UV radiation from forming structures has a clear impact on the thermodynamics, composition, and time evolution of cosmic gas. This is generally true for all the UV scenarios examined here, although the implications of each individual model vary remarkably and appear to be extreme for large UV onset redshifts ($z \gtrsim 8$).

Inclusion of HI and H_2 self shielding is relevant to address the role of UV photoionisation at high (above $1 \text{ particle cm}^{-3}$) and intermediate densities (in the range between $\sim 10^{-2}$ and $1 \text{ particle cm}^{-3}$). HI shielding has an important indirect impact during and after reionisation, because it significantly preserves the amount of HI, which is indispensable for H_2 formation, from UV photoionisation. Thus, self shielding ensures that large enough amounts of HI and H_2 are obtained to consistently match the observations. We remind that H_2 self shielding is effective mainly on dense gas and has little impact on IGM/CGM-like material (e.g., Petkova & Maio 2012), and therefore HI self shielding is found to play a major role in cosmic gas chemistry. The effect of varying H_2 shielding prescriptions, instead, is modest (Appendix B). As an example, the recently updated model by Wolcott-Green et al. (2017) results in excellent agreement with previous works by Draine & Bertoldi (1996) as long as the length scale used to derive the local H_2 column density is approximated by one-quarter of the Jeans length. The effects of alternative choices are small in thin media, but become important in dense sites (e.g., when estimating molecular cooling of collapsing gas or critical fluxes of impinging radiation during the formation of massive black-hole seeds; Luo et al. 2020; Maio et al. 2019). Neglecting HI shielding corrections at high redshift ($z > 5$) leads to a large degree of H ionisation and H_2 photodissociation, causing underestimation of HI and H_2 cosmological densities and leading to a trend of the atomic and molecular density parameters in tension with data even at $z < 5$. Furthermore, gas self shielding appears to be crucial for justifying the existence of molecular gas at high redshift, as observed ubiquitously in outflows of massive galaxies at $z \gtrsim 4$ with loading factors of the order of unity (Spilker et al. 2020).

Gas-grain processes have been implemented adopting different values for a constant ($T_{\text{gr}} = 40, 75$ and 120 K) and a z -dependent grain temperature, based either on the CMB scaling or on the dust emissivity index, β (da Cunha et al. 2021). As T_{gr} evolution is not very sensitive to β , we find that details of its implementation do not have a large impact on the bulk of structure formation and the overall H_2 mass formed; however, they can be relevant locally in metal-rich sites (in agreement with expectations from high- z starburst galaxies; Overzier et al. 2011) and boost molecular fractions above 50% (Appendix C).

Our results show that the origin of H_2 in different epochs is typically linked to free electrons made available during structure formation that boost the H^- channel in most cosmic environments. Such a relevant role of the H^- channel is in line with conclusions from analytic investigations that stressed the need to reduce the density of H^- to suppress star formation in early minihaloes (Cen 2017), and is also in line with recent semi-analytical ISM studies that highlighted the important role played by H^- (Thi et al. 2020). This species is effective in electron-rich, albeit not extremely dense ($\sim 0.1-1 \text{ cm}^{-3}$) gas, as is the case for most of the cosmic medium during or after reionisation. Free electrons are captured by H atoms via radiative attachment and increase the amount of H^- available for H_2 formation. The H_2^+ channel can provide an additional contribution (of up to about one-fifth), but it is typically smaller than that from the H^- channel because of the lower collisional rates (Appendix F). Reactions involving H^- and H_2^+ catalysts that form molecular hydrogen ($\text{H}^- + \text{H}_2^+ \rightarrow \text{H}_2 + \text{H}$) are less likely than H_2^+ or H^- impacts with H and the resulting H_2 enhancement is not substantial, given also their relatively low abundances. Three-body processes can provide some H_2 mass content. Their effects are subdominant for Ω_{neutral} and Ω_{H_2} estimates, but help reach high H_2 fractions of

roughly 50% at $z \sim 4-6$ in metal-poor sites (i.e. values similar to those reached by H_2 grain catalysis in metal-rich sites).

These processes nicely explain the origin of the large supply of molecular mass within galaxies at $z \gtrsim 2$ (Garratt et al. 2021). In fact, large observationally inferred H_2 fractions at early times (Dessauges-Zavadsky et al. 2020) can be explained either via standard H_2 formation channels in metal-poor or pristine gas or via H_2 grain catalysis in metal-rich sites. We warn the reader that, from a purely statistical point of view, large H_2 values, although detected, might not necessarily be typical for the whole galaxy population at those epochs. Indeed, there is a clear observational bias because of which galaxies with large H_2 fractions are easier to observe via their strong CO emission. Previous results from subgrid models for isolated galaxies at $z \simeq 2$ focusing on H_2 formation on dust grains only (Tomassetti et al. 2015) confirm the leading role of H_2 grain catalysis in enriched environments. The possibility to form H_2 molecules via the two mentioned chemistry paths is also consistent with the lack of observed environmental (metallicity) dependence up to $z \sim 3.5$ in the assembly of H_2 mass (e.g., Darvish et al. 2018; Tadaki et al. 2019). This hides the fundamental physical difference between the nearby Universe, where H_2 formation is led by grain catalysis in polluted media (in agreement with results of local molecular clouds; Wakelam et al. 2017), and the distant Universe, where H_2 production is mainly led by the H^- channel in shielded low- Z /pristine gas. We warn that, in principle, H_2 production could be enhanced by grain processes at any z , as long as the sites concerned have local metallicities of $Z \gtrsim 0.1 Z_\odot$. This conclusion is consistent with detailed ISM analyses by for example Gong et al. (2020) (who consider Z within $0.5-2 Z_\odot$) and Hu et al. (2021) (who explore Z within $0.1-3 Z_\odot$).

We improve upon previous semi-analytical studies by Jasche et al. (2007) who examined the possible heating due to cosmic rays at early epochs (Appendix E). Our constant cosmic-ray ionisation rate per H atom, $\zeta = 10^{-17} \text{ s}^{-1}$, is consistent with traditional values, with the latest determinations by Thi et al. (2020) and with the rate assumed in Narayanan & Krumholz (2017), who correct the suggested $\zeta \simeq 10^{-16} \text{ s}^{-1}$ by a factor of 0.1 (Indriolo & McCall 2012). We additionally consider the calculations by Padovani et al. (2018) for a density-dependent ζ and adopt it to assess the implications on star forming gas. We find that typical values for the cosmic-ray ionisation rate induce heating, in addition to the heating from structure formation shocks, and cause a deficit of Ω_{H_2} at early times. In the realistic scenario of cosmic-ray heating linked to star forming gas parcels, the effects observed at high z are not very prominent and the resulting Ω_{H_2} and Ω_{neutral} (or Ω_{HI}) are close to those without cosmic-ray heating. At lower z , the formation of molecular gas is slightly suppressed and Ω_{H_2} is slightly smaller than in the reference scenario without cosmic-ray heating. Overall, the effects are of the order of 10%. These results are consistent with the low level (up to a factor of 2) of star formation suppression found in the most recent studies of isolated disk galaxies (Semenov et al. 2021) and hint at the limited role of cosmic-ray heating in high- z structures.

The additional processes mentioned above (metallicity evolution, metal-dependent H_2 grain catalysis, photoelectric effect, cosmic-ray heating, etc.) may have an impact on the local environment, depending on the chemical and thermal state of the hosting gas. H_2 grain catalysis and photoelectric heating can boost Ω_{H_2} by up to a factor of 3 at $z \simeq 6$, still within observational constraints (Riechers et al. 2020b), while large metallicities enhance H_2 grain catalysis up to $\Omega_{\text{H}_2} \simeq 2-3 \times 10^{-4}$ for

$Z \sim Z_\odot$. We note that we have scaled the H_2 grain reaction and cooling/heating rates linearly with Z , but dust-to-gas ratios could be steeper in low- Z environments (as in blue compact dwarfs, which can be thought as nearby probes of the physics of distant primeval sources). In such cases, the suggested scaling could be $\propto Z^{1.5}$ (Galametz et al. 2011) or even $\propto Z^2$ (Herrera-Camus et al. 2012). This would lower the contribution of gas-grain cooling/heating at low Z , imply metallicities closer to solar which would render the H_2 grain catalysis more effective, and indicate a much smaller role of heavy elements at early times. Non-equilibrium results about the cosmic-ray heating rely on the ionisation rate and yield derived from realistic H, He, and H_2 gas mixtures. Although improved with respect to previous works, those quantities are still obtained by neglecting heavy elements, and therefore analyses of the energy transfer in more general conditions are still required. In our study, we varied the ionisation rate by up to one order of magnitude and found small effects for HI and H_2 mass densities in star forming regions at $z < 6$. Furthermore, we tested the implications of different IMFs and wind assumptions on mass density parameters, but found no significant changes (Appendix I).

The actual role of some physical processes, such as the photoelectric effect, cosmic rays, or dust cycling in galaxies during the epoch of reionisation, is still unclear and more data are needed (Burgarella et al. 2020). Despite these uncertainties, gas self shielding, which preserves HI and H_2 abundances, is likely the principal reason for cool molecular gas to extend further out than dust in observations of star forming galaxies. Indeed, we find that, without self shielding, lower H_2 values are obtained even with the inclusion of H_2 grain catalysis. This is in line with recent interpretations of ALMA observations (Calistro Rivera et al. 2018) and should hold a fortiori at high redshift, when metals and dust grains are expected to be under-abundant. In this respect, observational analyses by Calistro Rivera et al. (2018) support our conclusions.

Earlier cosmological simulations have highlighted the difficulty in reproducing the behaviour of chemical density parameters. In particular, the observed increasing trend of Ω_{HI} and Ω_{neutral} has been challenging to model. Numerical efforts by Nagamine et al. (2004) using similar star formation and feedback models to Springel & Hernquist (2003) in a dozen Gadget simulations highlighted the relevant role of wind feedback and obtained Ω_{HI} results consistent with observations at $z = 2-5$ with a ‘weak’ wind speed of 242 km s^{-1} . This value is in line with our reference wind speed of 350 km s^{-1} . The consistency in the general trend is encouraging and corroborates the results presented in this manuscript. Nagamine et al. (2004) could not study Ω_{H_2} evolution because of a lack of observational data at the time. Davé et al. (2013) proposed a treatment for HI and H_2 gas content based on H ionisation balance to account for HI and on ISM pressure equilibrium to account for H_2 . They computed H_2 fractions in star forming particles only. Gas that is not star forming was assumed to have zero molecular content. These approximations were required because the star formation threshold used by the authors was 0.1 cm^{-3} (too low to resolve runaway molecular cooling in dense cold gas) and HI/ H_2 self-shielding effects were not included. Gas properties were corrected for HI shielding in post-processing, but they found an HI mass density parameter decreasing with increasing redshift, with $\Omega_{\text{HI}} < 10^{-3}$ at $z < 5$ and $\Omega_{\text{HI}} \simeq$ a few 10^{-4} at $z \simeq 5$. These predictions led Davé et al. (2013) to question the ability of equilibrium-based models to capture the fundamental processes shaping the HI and H_2 behaviour, as also noted in Davé et al. (2020). Similarly, low HI mass densities

and decreasing Ω_{HI} redshift evolution have been obtained by other independent groups based on semi-analytical models run on top of N -body simulations (e.g., [Spinelli et al. 2020](#)). The deviations of H_2 abundances from equilibrium in cosmic environments highlight the need to follow a time-dependent non-equilibrium approach to obtain reliable molecular fractions (as stressed lately by [Hu et al. 2017, 2021](#), and as done throughout this work). Other popular hydrodynamic simulations (such as Owls or Eagle; [Schaye et al. 2015](#), and references therein) adopt UV rates similar to the ones used here (HM), but employ low-density thresholds for star formation and do not partition hydrogen into its ionised, neutral, and molecular components (as also done in the NIHAO project; [Obreja et al. 2019](#)). Post-processing assumptions on how to distribute these species are therefore needed ([Blitz & Rosolowsky 2006](#) or [Gnedin & Kravtsov 2011](#)). Post-processing modelling of hydrogen phases for the Eagle simulations ([Rahmati et al. 2015](#)) leads to a roughly flat HI curve at $z \sim 2\text{--}6$, while Illustris-TNG results in a 100 Mpc h^{-1} side box feature a non-monotonic behaviour attributed to a lack of resolution ([Villaescusa-Navarro et al. 2018](#)). As it is usually based on local calibrations, this approach is effective for studying the nearby Universe or enriched systems, but might present issues at higher redshift or in low-metallicity environments, such as the whole epoch of reionisation and the first few cosmological gigayears. In practice, as they are not included in hydrodynamical and chemistry run-time calculations, H_2 molecules cannot play any role in gas cooling. It is probably for this reason that semi-analytical computations by [Lagos et al. \(2018\)](#), and references therein) performed on the outputs of numerical simulations to estimate HI and H_2 fractions with post-processing scaling relations find HI densities which are not fully consistent with observations. Their HI (neutral) mass density parameter decreases from a few 10^{-4} (at $z \approx 1$) down to 10^{-5} (at $z \approx 3.5$) and also their values never reach $\Omega_{\text{HI}} \sim 10^{-3}$ ([Rhee et al. 2018](#)). Despite that, [Lagos et al. \(2018\)](#) can roughly reproduce Ω_{H_2} values at $z \lesssim 3$. The various Illustris simulations (e.g., [Springel et al. 2018](#), and references therein) address HI and H_2 properties via the empirical model of [Gnedin & Draine \(2014, 2016\)](#), but do not implement non-equilibrium atomic and molecular chemistry. When post-processed with semi-analytical models ([Somerville et al. 2015](#)), results predict H_2 masses that are too low at $z > 1$ and cosmic densities (Ω_{H_2}) in tension with ASPECS data, independently of the adopted H_2 partition recipe, as their simulated gas (for which the star formation density threshold is $\sim 0.1 \text{ cm}^{-3}$) is not dense enough to become molecular ([Popping et al. 2019](#)). The smaller Ω_{H_2} values found by [Popping et al. \(2019\)](#) might also be linked to the chosen UV background by [Faucher-Giguère et al. \(2009\)](#), which (similarly to [Faucher-Giguère 2020](#), FG20) assumes an earlier onset and hence causes a longer photoheating injection with respect to the HM model. Although this latter is adopted in [Lagos et al. \(2018\)](#), their latest semi-analytical estimates ([Lagos et al. 2020](#)) still find ρ_{H_2} values systematically below the observational constraints. Other recent studies (such as [Gjergo et al. 2018, 2020](#), [Vogelsberger et al. 2019](#), [Graziani et al. 2020](#), [Granato et al. 2021](#)) have incorporated dust mass modelling from gas mass metallicities within three-dimensional numerical simulations, however their implementations are not coupled to non-equilibrium H_2 chemistry. Finally, recent H_2 modelling by [Schäbe et al. \(2020\)](#) that includes H_2 formation via dust grain catalysis only in a 12 Mpc/ h side box suggests the existence of undetected molecular amounts at high redshift, as their predicted H_2 mass densities at $z \approx 4\text{--}6$ were higher than current observational determinations (as in Fig. C.2).

We note that, as in any such work, numerical accuracy is important, but the different star formation schemes and feedback implementations adopted often have a larger impact. Feedback efficiency and star formation timescales modulate the whole evolution of H_2 mass. Changing the shape of the IMF from Salpeter to Chabrier slightly alters star-formation-related quantities (in agreement with e.g., [Cassarà et al. 2013](#)), while varying wind velocities ([Hassan & Gronke 2021](#)) or SN efficiency has an impact of up to 1 dex when these parameters are varied by a factor of 5–10, independently of other model assumptions ([Steinwandel et al. 2020](#)). For HI, the impact is less dramatic and results vary by less than 0.5 dex. Chemistry rates and yields are still affected by factor-of-two uncertainties (for examples, compare H_2 grain catalysis rates in [Hollenbach & McKee 1979](#); [Tielens & Hollenbach 1985](#); [Cazaux & Tielens 2004](#); [Tomassetti et al. 2015](#)) and this influences resulting abundance ratios ([Maio & Tescari 2015](#); [Ma et al. 2015, 2017b](#); [Valentini et al. 2019a](#)).

From an observational point of view, HI mass densities are relatively well established up to $z \lesssim 6$ with errors below a factor of 2. Moreover, exploiting [C II] emission in high- z enriched environments (as lately done by [Heintz et al. 2021](#)) would possibly open the door to observing Ω_{neutral} at $z > 6$, where our results predict different scenarios depending on the chosen UV background. On the other hand, estimates of the reservoir of H_2 masses in star forming environments from [C II] or CO observational data are challenging and the conversion factors usually adopted bear uncertainties and biases ([Madden et al. 2020](#); [Gong et al. 2020](#); [Breyse et al. 2021](#)). The [C II] 158 micron line is a workhorse for (sub-)mm observations and is resolved on a kiloparsec scale by ALMA ([Rybak et al. 2019](#)). As extended [C II] halos are found more and more commonly in high- z galaxies (early star forming sources of $10^{11}\text{--}10^{12} M_{\odot}$ fit with classical ‘normal’ star forming galaxies; [Ginolfi et al. 2019](#); [Hodge & da Cunha 2020](#)) and because [C II] emissions tracing a combination of molecular, ionised, and atomic gas are still very little explored, future assessments of H_2 via [C II] could significantly improve the current picture for Ω_{H_2} .

Throughout this work we assumed a Λ CDM cosmology. We briefly point out that in some particular cases (such as for warm dark matter, [Maio & Viel 2015](#)) the background cosmological model mostly influences the baryonic-structure evolution at higher redshift. This plays a role during the beginning of the onset of star formation, but in the epochs of interest here, baryon evolution tends to dominate and alleviate any discrepancy due either to alternative cosmologies ([Maio et al. 2006](#)) and matter non-Gaussianities ([Maio & Iannuzzi 2011](#); [Maio 2011](#); [Maio et al. 2012](#); [Maio & Khochfar 2012](#)) or to a different dark-matter nature ([Maio & Viel 2015](#)). Finally, the baryon census ($\Omega_{0,b}$) is crucial for assessing atomic and molecular gas evolution. Alternative estimates of $\Omega_{0,b}$ have been proposed (using e.g., FRBs, [Macquart et al. 2020](#)) and, although uncertainties still persist, they are consistent with the cosmic microwave background and Big Bang nucleosynthesis.

5. Conclusions

We quantified the evolution of cold atomic and molecular cosmic gas, from the epoch of reionisation down to $z \sim 2$. We performed cosmological N -body hydrodynamic chemistry simulations to model the origin and evolution of cold-gas density parameters and timescales. Our implementation follows time-dependent non-equilibrium atomic and molecular abundance calculations and considers the impact of different UV backgrounds, as well

as a number of physical processes that could affect the build-up of H_2 and neutral-gas mass. Star formation in dense HI and H_2 self-shielded regions, stellar feedback, and production of heavy elements from stars with different masses and metallicities are also accounted for. We constrain the effects of the major processes involved in cold-gas evolution and interpret state-of-the-art observations in the (sub-)mm and IR ranges. The present study is among the first of its kind to address cosmic HI and H_2 evolution at these epochs using three-dimensional hydrodynamic simulations and including detailed non-equilibrium chemistry networks. Our findings can be summarised as follows.

- The evolution of cold atomic and molecular gas obtained with basic time-dependent non-equilibrium chemical reactions in dense gas is broadly consistent with the latest HI and H_2 observational data once HI and H_2 self shielding from UV radiation is taken into account within the chemical network.
- The resulting mass of neutral gas slowly increases with redshift up to $\Omega_{\text{neutral}} \sim 2 \times 10^{-3}$ at $z \simeq 6$, while H_2 features a plateau at $\Omega_{\text{H}_2} \sim 10^{-4}$ at $z \gtrsim 2$.
- Details of the UV background model adopted (HM, P19 and FG20) have a modest impact on Ω_{neutral} at $z \lesssim 6$, while they are relevant for Ω_{H_2} : the onset epoch of the UV background in particular seems to be crucial, suggesting that early ($z \gtrsim 8$) onsets could be in tension with H_2 data and could require either lower UV rates or larger self shielding at those times.
- Resolving dense shielded gas and adopting a high star formation density threshold is necessary to properly estimate the amount of cold gas and to obtain results in line with HI and H_2 observational data.
- Our non-equilibrium H_2 -based star formation model leads to results that are in slightly better agreement with available HI and H_2 determinations.
- H_2 evolution is globally driven by the H^- channel, with a relevant contribution from H_2 grain catalysis at high metallicities and on local scales, while other formation channels are negligible. This explains the observationally inferred lack of environmental dependence in H_2 mass build-up at $z \lesssim 3.5$.
- Cosmic-ray heating in star forming regions, quantified in accordance with different models for the cosmic-ray ionisation rate, affects the H_2 abundance at the 10% level globally.
- Wind feedback impacts results mostly at lower redshift, while SN explosions affect early star forming regimes, with effects from IMF variations usually remaining small at all times.
- Recently detected molecular fractions of $\sim 50\%$ at $z \simeq 4-6$ can be explained by essential non-equilibrium H_2 formation channels in metal-poor media or H_2 grain catalysis in metal-rich gas: in this latter case, precise determination of grain temperature has little relevance and is generally subdominant to metallicity effects.
- Despite the resurgence of UV radiation, H_2 depletion times reach values that are lower than the Hubble time, and even comparable to the dynamical time, within the first half-gigayear, meaning that cosmic gas is able to collapse already at such early epochs.

The ability to form significant amounts of H_2 and to reach short depletion times during the epoch of reionisation means that further discoveries of molecular-rich star forming galaxies at early times will be possible in the coming years. New data from upcoming international facilities, such as JWST (Gardner & JWST Science Working Group 2009), ELT (Puech et al. 2010), SKA (Koopmans et al. 2015), Roman/WFIRST (Whalen et al. 2013) or ATHENA (Nandra et al. 2013), will be decisive in shedding light on the

still unanswered questions about the origin of chemical species in the cosmic gas and the whole baryon cycle.

Acknowledgements. We are grateful to the anonymous referee for his/her careful reading and suggestions that improved the original manuscript. We are thankful to F. Haardt, S. Borgani, L. Tornatore, G. Popping and R. Szakacs for their constructive comments. U.M. is indebted to L. Böss and U. Steinwandel for insightful conversations and to M. Padovani for kindly sharing the full table of his ionisation rate calculations used throughout this work. We thank A. Hamanowicz for sharing with us preliminary ALMACAL-CO results. We also thank the Max Planck Computation and Data Facility (MPCDF) of the Max Planck Society, where simulation runs and analyses have been performed. We acknowledge the NASA Astrophysics Data System and the JSTOR archive for their bibliographic research tools.

References

- Abel, T., Anninos, P., Zhang, Y., & Norman, M. L. 1997, *New Astron.*, **2**, 181
- Abel, T., Bryan, G. L., & Norman, M. L. 2002, *Science*, **295**, 93
- Anninos, P., Zhang, Y., Abel, T., & Norman, M. L. 1997, *New Astron.*, **2**, 209
- Bakes, E. L. O., & Tielens, A. G. G. M. 1994, *ApJ*, **427**, 822
- Bera, A., Kanekar, N., Chengalur, J. N., & Bagla, J. S. 2019, *ApJ*, **882**, L7
- Berta, S., Lutz, D., Nordon, R., et al. 2013, *A&A*, **555**, L8
- Binney, J., & Tremaine, S. 2008, *Galactic Dynamics: Second Edition* (Princeton University Press)
- Blitz, L., & Rosolowsky, E. 2006, *ApJ*, **650**, 933
- Bolatto, A. D., Wolfire, M., & Leroy, A. K. 2013, *ARA&A*, **51**, 207
- Boogaard, L. A., Bouwens, R. J., Riechers, D., et al. 2021, *ApJ*, **916**, 12
- Breyse, P. C., Yang, S., Somerville, R. S., et al. 2021, *ApJ*, submitted, [arXiv:2106.14904]
- Bromm, V., & Yoshida, N. 2011, *ARA&A*, **49**, 373
- Bron, E., Le Bourlot, J., & Le Petit, F. 2014, *A&A*, **569**, A100
- Bruzual, G., & Charlot, S. 2003, *MNRAS*, **344**, 1000
- Burgarella, D., Nanni, A., Hirashita, H., et al. 2020, *A&A*, **637**, A32
- Calistro Rivera, G., Hodge, J. A., Smail, I., et al. 2018, *ApJ*, **863**, 56
- Campisi, M. A., Maio, U., Salvaterra, R., & Ciardi, B. 2011, *MNRAS*, **416**, 2760
- Cassarà, L. P., Piovani, L., Weiss, A., Salaris, M., & Chiosi, C. 2013, *MNRAS*, **436**, 2824
- Cazaux, S., & Tielens, A. G. G. M. 2004, *ApJ*, **604**, 222
- Cen, R. 2017, *MNRAS*, **465**, L69
- Chabrier, G. 2003, *PASP*, **115**, 763
- Chen, Q., Meyer, M., Popping, A., et al. 2021, *MNRAS*, **508**, 2758
- Chomiuk, L., & Povich, M. S. 2011, *AJ*, **142**, 197
- Christiansen, J. F., Davé, R., Sorini, D., & Anglés-Alcázar, D. 2020, *MNRAS*, **499**, 2617
- Crighton, N. H. M., Murphy, M. T., Prochaska, J. X., et al. 2015, *MNRAS*, **452**, 217
- da Cunha, E., Groves, B., Walter, F., et al. 2013, *ApJ*, **766**, 13
- da Cunha, E., Hodge, J. A., Casey, C. M., et al. 2021, *ApJ*, **919**, 30
- Darvish, B., Scoville, N. Z., Martin, C., et al. 2018, *ApJ*, **860**, 111
- Davé, R., Katz, N., Oppenheimer, B. D., Kollmeier, J. A., & Weinberg, D. H. 2013, *MNRAS*, **434**, 2645
- Davé, R., Rafieferantsoa, M. H., & Thompson, R. J. 2017, *MNRAS*, **471**, 1671
- Davé, R., Anglés-Alcázar, D., Narayanan, D., et al. 2019, *MNRAS*, **486**, 2827
- Davé, R., Crain, R. A., Stevens, A. R. H., et al. 2020, *MNRAS*, **498**, 146
- Decarli, R., Walter, F., González-López, J., et al. 2019, *ApJ*, **882**, 138
- Decarli, R., Aravena, M., Boogaard, L., et al. 2020, *ApJ*, **902**, 110
- Delhaize, J., Meyer, M. J., Staveley-Smith, L., & Boyle, B. J. 2013, *MNRAS*, **433**, 1398
- Dessauges-Zavadsky, M., Ginolfi, M., Pozzi, F., et al. 2020, *A&A*, **643**, A5
- Dickman, R. L., Snell, R. L., & Schloerb, F. P. 1986, *ApJ*, **309**, 326
- Dolag, K., Borgani, S., Murante, G., & Springel, V. 2009, *MNRAS*, **399**, 497
- Donnari, M., Pillepich, A., Nelson, D., et al. 2019, *MNRAS*, **485**, 4817
- Draine, B. T., & Bertoldi, F. 1996, *ApJ*, **468**, 269
- Draine, B. T., & Lee, H. M. 1984, *ApJ*, **285**, 89
- Draine, B. T., & Li, A. 2007, *ApJ*, **657**, 810
- Draine, B. T., & Sutin, B. 1987, *ApJ*, **320**, 803
- Duley, W. W. 1996, *MNRAS*, **279**, 591
- Dwek, E., & Smith, R. K. 1996, *ApJ*, **459**, 686
- Faisst, A. L., Fudamoto, Y., Oesch, P. A., et al. 2020, *MNRAS*, **498**, 4192
- Faucher-Giguère, C.-A. 2020, *MNRAS*, **493**, 1614
- Faucher-Giguère, C.-A., Lidz, A., Zaldarriaga, M., & Hernquist, L. 2009, *ApJ*, **703**, 1416
- Fletcher, T. J., Saintonge, A., Soares, P. S., & Pontzen, A. 2021, *MNRAS*, **501**, 411
- Flower, D. R., & Harris, G. J. 2007, *MNRAS*, **377**, 705

- Forrey, R. C. 2013, *ApJ*, **773**, L25
- Furlong, M., Bower, R. G., Theuns, T., et al. 2015, *MNRAS*, **450**, 4486
- Galametz, M., Madden, S. C., Galliano, F., et al. 2011, *A&A*, **532**, A56
- Galli, D., & Palla, F. 1998, *A&A*, **335**, 403
- Gardner, J. P., & JWST Science Working Group 2009, in *American Astronomical Society Meeting Abstracts #213*, *Bull. Am. Astron. Soc.*, **41**, 254
- Garratt, T. K., Coppin, K. E. K., Geach, J. E., et al. 2021, *ApJ*, **912**, 62
- Genel, S., Vogelsberger, M., Springel, V., et al. 2014, *MNRAS*, **445**, 175
- Genzel, R., Tacconi, L. J., Combes, F., et al. 2012, *ApJ*, **746**, 69
- Ginolfi, M., Schneider, R., Valiante, R., et al. 2019, *MNRAS*, **483**, 1256
- Girichidis, P., Offner, S. S. R., Kritsuk, A. G., et al. 2020, *Space Sci. Rev.*, **216**, 68
- Gjergo, E., Granato, G. L., Murante, G., et al. 2018, *MNRAS*, **479**, 2588
- Gjergo, E., Palla, M., Matteucci, F., et al. 2020, *MNRAS*, **493**, 2782
- Glassgold, A. E., Galli, D., & Padovani, M. 2012, *ApJ*, **756**, 157
- Glover, S. C. O., & Clark, P. C. 2012, *MNRAS*, **421**, 9
- Glover, S. C. O., & Savin, D. W. 2009, *MNRAS*, **393**, 911
- Gnedin, N. Y., & Draine, B. T. 2014, *ApJ*, **795**, 37
- Gnedin, N. Y., & Draine, B. T. 2016, *ApJ*, **830**, 54
- Gnedin, N. Y., & Kravtsov, A. V. 2011, *ApJ*, **728**, 88
- Goldsmith, P. F., & Langer, W. D. 1978, *ApJ*, **222**, 881
- Goldsmith, P. F., Liseau, R., Bell, T. A., et al. 2011, *ApJ*, **737**, 96
- Gong, M., Ostriker, E. C., Kim, C.-G., & Kim, J.-G. 2020, *ApJ*, **903**, 142
- Granato, G. L., Ragone-Figueroa, C., Taverna, A., et al. 2021, *MNRAS*, **503**, 511
- Graziani, L., Schneider, R., Ginolfi, M., et al. 2020, *MNRAS*, **494**, 1071
- Gruppioni, C., Béthermin, M., Loiacono, F., et al. 2020, *A&A*, **643**, A8
- Gry, C., Boulanger, F., Nehmé, C., et al. 2002, *A&A*, **391**, 675
- Haardt, F., & Madau, P. 1996, *ApJ*, **461**, 20
- Haardt, F., & Madau, P. 2012, *ApJ*, **746**, 125
- Habing, H. J. 1968, *Bull. Astron. Inst. Netherlands*, **19**, 421
- Hamanowicz, A., Péroux, C., Zwaan, M., et al. 2021, *MNRAS*, submitted
- Hartwig, T., Glover, S. C. O., Klessen, R. S., Latif, M. A., & Volonteri, M. 2015, *MNRAS*, **452**, 1233
- Hassan, S., & Gronke, M. 2021, *ApJ*, **908**, 219
- Heintz, K. E., Watson, D., Oesch, P. A., Narayanan, D., & Madden, S. C. 2021, *ApJ*, **922**, 147
- Herrera-Camus, R., Fisher, D. B., Bolatto, A. D., et al. 2012, *ApJ*, **752**, 112
- Hodge, J. A., & da Cunha, E. 2020, *R. Soc. Open Sci.*, **7**, 200556
- Hollenbach, D., & McKee, C. F. 1979, *ApJS*, **41**, 555
- Hollenbach, D., & McKee, C. F. 1989, *ApJ*, **342**, 306
- Hollenbach, D. J., & Tielens, A. G. G. M. 1999, *Rev. Mod. Phys.*, **71**, 173
- Hollenbach, D., Kaufman, M. J., Neufeld, D., Wolfire, M., & Goicoechea, J. R. 2012, *ApJ*, **754**, 105
- Hopmann, L., Staveley-Smith, L., Freudling, W., et al. 2015, *MNRAS*, **452**, 3726
- Hu, C.-Y., Naab, T., Glover, S. C. O., Walch, S., & Clark, P. C. 2017, *MNRAS*, **471**, 2151
- Hu, W., Hopmann, L., Staveley-Smith, L., et al. 2019, *MNRAS*, **489**, 1619
- Hu, C. Y., Sternberg, A., & van Dishoeck, E. F. 2021, *ApJ*, **920**, 44
- Hughes, T. M., Ibar, E., Villanueva, V., et al. 2017, *MNRAS*, **468**, L103
- Hunt, L. K., Tortora, C., Ginolfi, M., & Schneider, R. 2020, *A&A*, **643**, A180
- Indriolo, N., & McCall, B. J. 2012, *ApJ*, **745**, 91
- Indriolo, N., Geballe, T. R., Oka, T., & McCall, B. J. 2007, *ApJ*, **671**, 1736
- Jasche, J., Ciardi, B., & Enßlin, T. A. 2007, *MNRAS*, **380**, 417
- Jones, M. O., & Bate, M. R. 2018, *MNRAS*, **480**, 2562
- Jones, M. G., Haynes, M. P., Giovanelli, R., & Moorman, C. 2018, *MNRAS*, **477**, 2
- Jura, M. 1975a, *ApJ*, **197**, 581
- Jura, M. 1975b, *ApJ*, **197**, 575
- Katz, N. 1992, *ApJ*, **391**, 502
- Khusanova, Y., Béthermin, M., Le Fèvre, O., et al. 2021, *A&A*, **649**, A152
- Klitsch, A., Zwaan, M. A., Péroux, C., et al. 2019, *MNRAS*, **482**, L65
- Komatsu, E., Smith, K. M., Dunkley, J., et al. 2011, *ApJS*, **192**, 18
- Koopmans, L., Pritchard, J., Mellema, G., et al. 2015, *Advancing Astrophysics with the Square Kilometre Array (AASKA14)*, **1**
- Krumholz, M. R., & Gnedin, N. Y. 2011, *ApJ*, **729**, 36
- Lagos, C. d. P., Tobar, R. J., & Robotham, A. S. G. 2018, *MNRAS*, **481**, 3573
- Lagos, C. d. P., da Cunha, E., Robotham, A. S. G., et al. 2020, *MNRAS*, **499**, 1948
- Leitherer, C., Schaerer, D., Goldader, J. D., et al. 1999, *ApJS*, **123**, 3
- Lenkić, L., Bolatto, A. D., Förster Schreiber, N. M., et al. 2020, *AJ*, **159**, 190
- Lepp, S., & Shull, J. M. 1984, *ApJ*, **280**, 465
- Leroy, A. K., Walter, F., Sandstrom, K., et al. 2013, *AJ*, **146**, 19
- Licquia, T. C., & Newman, J. A. 2015, *ApJ*, **806**, 96
- Lilly, S. J., Carollo, C. M., Pipino, A., Renzini, A., & Peng, Y. 2013, *ApJ*, **772**, 119
- Luo, Y., Shlosman, I., Nagamine, K., & Fang, T. 2020, *MNRAS*, **492**, 4917
- Ma, Q., Maio, U., Ciardi, B., & Salvaterra, R. 2015, *MNRAS*, **449**, 3006
- Ma, Q., Maio, U., Ciardi, B., & Salvaterra, R. 2017a, *MNRAS*, **466**, 1140
- Ma, Q., Maio, U., Ciardi, B., & Salvaterra, R. 2017b, *MNRAS*, **472**, 3532
- Macquart, J. P., Prochaska, J. X., McQuinn, M., et al. 2020, *Nature*, **581**, 391
- Madden, S. C., Poglitsch, A., Geis, N., Stacey, G. J., & Townes, C. H. 1997, *ApJ*, **483**, 200
- Madden, S. C., Cormier, D., Hony, S., et al. 2020, *A&A*, **643**, A141
- Maio, U. 2011, *CQG*, **28**, 225015
- Maio, U. 2021, ArXiv e-prints [arXiv:2111.01804]
- Maio, U., & Iannuzzi, F. 2011, *MNRAS*, **415**, 3021
- Maio, U., & Khochfar, S. 2012, *MNRAS*, **421**, 1113
- Maio, U., & Tescari, E. 2015, *MNRAS*, **453**, 3798
- Maio, U., & Viel, M. 2015, *MNRAS*, **446**, 2760
- Maio, U., Dolag, K., Meneghetti, M., et al. 2006, *MNRAS*, **373**, 869
- Maio, U., Dolag, K., Ciardi, B., & Tornatore, L. 2007, *MNRAS*, **379**, 963
- Maio, U., Ciardi, B., Yoshida, N., Dolag, K., & Tornatore, L. 2009, *A&A*, **503**, 25
- Maio, U., Ciardi, B., Dolag, K., Tornatore, L., & Khochfar, S. 2010, *MNRAS*, **407**, 1003
- Maio, U., Khochfar, S., Johnson, J. L., & Ciardi, B. 2011a, *MNRAS*, **414**, 1145
- Maio, U., Koopmans, L. V. E., & Ciardi, B. 2011b, *MNRAS*, **412**, L40
- Maio, U., Salvaterra, R., Moscardini, L., & Ciardi, B. 2012, *MNRAS*, **426**, 2078
- Maio, U., Petkova, M., De Lucia, G., & Borgani, S. 2016, *MNRAS*, **460**, 3733
- Maio, U., Borgani, S., Ciardi, B., & Petkova, M. 2019, *PASA*, **36**, e020
- Maloney, P., & Black, J. H. 1988, *ApJ*, **325**, 389
- Mancini, M., Schneider, R., Graziani, L., et al. 2015, *MNRAS*, **451**, L70
- Mancini, M., Schneider, R., Graziani, L., et al. 2016, *MNRAS*, **462**, 3130
- Muratov, A. L., Gnedin, O. Y., Gnedin, N. Y., & Zemp, M. 2013, *ApJ*, **772**, 106
- Nagamine, K., Springel, V., & Hernquist, L. 2004, *MNRAS*, **348**, 421
- Nandra, K., Barret, D., Barcons, X., et al. 2013, ArXiv e-prints [arXiv:1306.2307]
- Narayanan, D., & Krumholz, M. R. 2017, *MNRAS*, **467**, 50
- Neufeld, D. A., & Wolfire, M. G. 2017, *ApJ*, **845**, 163
- Noterdaeme, P., Petitjean, P., Ledoux, C., & Srianand, R. 2009, *A&A*, **505**, 1087
- Noterdaeme, P., Petitjean, P., Carithers, W. C., et al. 2012, *A&A*, **547**, L1
- Obreja, A., Macciò, A. V., Moster, B., et al. 2019, *MNRAS*, **490**, 1518
- Omukai, K., Tsuribe, T., Schneider, R., & Ferrara, A. 2005, *ApJ*, **626**, 627
- Opal, C. B., Peterson, W. K., & Beatty, E. C. 1971, *J. Chem. Phys.*, **55**, 4100
- Orel, A. E. 1987, *J. Chem. Phys.*, **87**, 314
- O'Shea, B. W., & Norman, M. L. 2008, *ApJ*, **673**, 14
- Overzier, R. A., Heckman, T. M., Wang, J., et al. 2011, *ApJ*, **726**, L7
- Padovani, P., & Matteucci, F. 1993, *ApJ*, **416**, 26
- Padovani, M., Galli, D., Ivlev, A. V., Caselli, P., & Ferrara, A. 2018, *A&A*, **619**, A144
- Pak, S., Jaffe, D. T., van Dishoeck, E. F., Johansson, L. E. B., & Booth, R. S. 1998, *ApJ*, **498**, 735
- Palla, F., Salpeter, E. E., & Stahler, S. W. 1983, *ApJ*, **271**, 632
- Pallottini, A., Ferrara, A., Bovino, S., et al. 2017, *MNRAS*, **471**, 4128
- Peebles, P. J. E., & Dicke, R. H. 1968, *ApJ*, **154**, 891
- Péroux, C., & Howk, J. C. 2020, *ARA&A*, **58**, 363
- Petkova, M., & Maio, U. 2012, *MNRAS*, **422**, 3067
- Petkova, M., & Springel, V. 2011, *MNRAS*, **415**, 3731
- Planck Collaboration VI. 2020, *A&A*, **641**, A6
- Ploekinger, S., & Schaye, J. 2020, *MNRAS*, **497**, 4857
- Popping, G., Pillepich, A., Somerville, R. S., et al. 2019, *ApJ*, **882**, 137
- Puchwein, E., Haardt, F., Haehnelt, M. G., & Madau, P. 2019, *MNRAS*, **485**, 47
- Puech, M., Rosati, P., Toft, S., et al. 2010, *MNRAS*, **402**, 903
- Rahmati, A., Pawlik, A. H., Raičević, M., & Schaye, J. 2013, *MNRAS*, **430**, 2427
- Rahmati, A., Schaye, J., Bower, R. G., et al. 2015, *MNRAS*, **452**, 2034
- Rao, S. M., Turnshek, D. A., Sardane, G. M., & Monier, E. M. 2017, *MNRAS*, **471**, 3428
- Rhee, J., Zwaan, M. A., Briggs, F. H., et al. 2013, *MNRAS*, **435**, 2693
- Rhee, J., Lah, P., Chengalur, J. N., Briggs, F. H., & Colless, M. 2016, *MNRAS*, **460**, 2675
- Rhee, J., Lah, P., Briggs, F. H., et al. 2018, *MNRAS*, **473**, 1879
- Riechers, D. A., Boogaard, L. A., Decarli, R., et al. 2020a, *ApJ*, **896**, L21
- Riechers, D. A., Hodge, J. A., Pavesi, R., et al. 2020b, *ApJ*, **895**, 81
- Rodighiero, G., Enia, A., Delvecchio, I., et al. 2019, *ApJ*, **877**, L38
- Röllig, M., Ossenkopf, V., Jeyakumar, S., Stutzki, J., & Sternberg, A. 2006, *A&A*, **451**, 917
- Rybak, M., Calistro Rivera, G., Hodge, J. A., et al. 2019, *ApJ*, **876**, 112
- Salpeter, E. E. 1955, *ApJ*, **121**, 161
- Sánchez, S. F., García-Benito, R., Zibetti, S., et al. 2016, *A&A*, **594**, A36
- Saslaw, W. C., & Zipoy, D. 1967, *Nature*, **216**, 976
- Schäbe, A., Romano-Díaz, E., Porciani, C., Ludlow, A. D., & Tomassetti, M. 2020, *MNRAS*, **497**, 5008
- Schaye, J., Crain, R. A., Bower, R. G., et al. 2015, *MNRAS*, **446**, 521

- Scoville, N. Z., & Solomon, P. M. 1975, [ApJ](#), **199**, L105
- Semenov, V. A., Kravtsov, A. V., & Caprioli, D. 2021, [ApJ](#), **910**, 126
- Shaw, G., Ferland, G. J., Henney, W. J., et al. 2009, [ApJ](#), **701**, 677
- Shull, J. M., Danforth, C. W., & Anderson, K. L. 2021, [ApJ](#), **911**, 55
- Sillero, E., Tissera, P. B., Lambas, D. G., et al. 2021, [MNRAS](#), **504**, 2325
- Skinner, D., & Wise, J. H. 2020, [MNRAS](#), **492**, 4386
- Somerville, R. S., Popping, G., & Trager, S. C. 2015, [MNRAS](#), **453**, 4337
- Spilker, J. S., Phadke, K. A., Aravena, M., et al. 2020, [ApJ](#), **905**, 85
- Spinelli, M., Zoldan, A., De Lucia, G., Xie, L., & Viel, M. 2020, [MNRAS](#), **493**, 5434
- Spitzer, L. J., & Scott, E. H. 1969, [ApJ](#), **158**, 161
- Springel, V. 2005, [MNRAS](#), **364**, 1105
- Springel, V., & Hernquist, L. 2003, [MNRAS](#), **339**, 289
- Springel, V., Pakmor, R., Pillepich, A., et al. 2018, [MNRAS](#), **475**, 676
- Stahler, S. W., & Palla, F. 2004, [The Formation of Stars](#) (Weinheim: Wiley-VCH)
- Steinwandel, U. P., Moster, B. P., Naab, T., Hu, C.-Y., & Walch, S. 2020, [MNRAS](#), **495**, 1035
- Sternberg, A., Le Petit, F., Roueff, E., & Le Bourlot, J. 2014, [ApJ](#), **790**, 10
- Tacconi, L. J., Neri, R., Genzel, R., et al. 2013, [ApJ](#), **768**, 74
- Tacconi, L. J., Genzel, R., Saintonge, A., et al. 2018, [ApJ](#), **853**, 179
- Tacconi, L. J., Genzel, R., & Sternberg, A. 2020, [ARA&A](#), **58**, 157
- Tadaki, K.-I., Kodama, T., Hayashi, M., et al. 2019, [PASJ](#), **71**, 40
- Talia, M., Cimatti, A., Giuliotti, M., et al. 2021, [ApJ](#), **909**, 23
- Tescari, E., Katsianis, A., Wyithe, J. S. B., et al. 2014, [MNRAS](#), **438**, 3490
- Thi, W. F., Hocuk, S., Kamp, I., et al. 2020, [A&A](#), **634**, A42
- Thielemann, F.-K., Argast, D., Brachwitz, F., et al. 2003, [Nucl. Phys. A](#), **718**, 139
- Tielens, A. G. G. M., & Hollenbach, D. 1985, [ApJ](#), **291**, 722
- Tomassetti, M., Porciani, C., Romano-Díaz, E., & Ludlow, A. D. 2015, [MNRAS](#), **446**, 3330
- Tornatore, L., Borgani, S., Dolag, K., & Matteucci, F. 2007, [MNRAS](#), **382**, 1050
- Tornatore, L., Borgani, S., Viel, M., & Springel, V. 2010, [MNRAS](#), **402**, 1911
- Valentini, M., Chiappini, C., Bossini, D., et al. 2019a, [A&A](#), **627**, A173
- Valentini, M., Borgani, S., Bressan, A., et al. 2019b, [MNRAS](#), **485**, 1384
- van den Hoek, L. B., & Groenewegen, M. A. T. 1997, [A&AS](#), **123**, 305
- Vazdekis, A., Sánchez-Blázquez, P., Falcón-Barroso, J., et al. 2010, [MNRAS](#), **404**, 1639
- Villaescusa-Navarro, F., Genel, S., Castorina, E., et al. 2018, [ApJ](#), **866**, 135
- Vogelsberger, M., McKinnon, R., O’Neil, S., et al. 2019, [MNRAS](#), **487**, 4870
- Wakelam, V., Bron, E., Cazaux, S., et al. 2017, [Mol. Astrophys.](#), **9**, 1
- Walter, F., Carilli, C., Neeleman, M., et al. 2020, [ApJ](#), **902**, 111
- Weingartner, J. C., & Draine, B. T. 2001, [ApJS](#), **134**, 263
- Whalen, D. J., Fryer, C. L., Holz, D. E., et al. 2013, [ApJ](#), **762**, L6
- Wise, J. H., Turk, M. J., Norman, M. L., & Abel, T. 2012a, [ApJ](#), **745**, 50
- Wise, J. H., Abel, T., Turk, M. J., Norman, M. L., & Smith, B. D. 2012b, [MNRAS](#), **427**, 311
- Wolcott-Green, J., Haiman, Z., & Bryan, G. L. 2017, [MNRAS](#), **469**, 3329
- Wolfire, M. G., Hollenbach, D., & McKee, C. F. 2010, [ApJ](#), **716**, 1191
- Wolz, L., Pourtsidou, A., Masui, K. W., et al. 2021, [MNRAS](#), in press, [arXiv:2102.04946]
- Woosley, S. E., & Weaver, T. A. 1995, [ApJS](#), **101**, 181
- Woosley, S. E., Heger, A., & Weaver, T. A. 2002, [Rev. Mod. Phys.](#), **74**, 1015
- Yoshida, N., Abel, T., Hernquist, L., & Sugiyama, N. 2003, [ApJ](#), **592**, 645
- Zafar, T., Popping, A., & Péroux, C. 2013, [A&A](#), **556**, A140
- Zanella, A., Daddi, E., Magdis, G., et al. 2018, [MNRAS](#), **481**, 1976
- Zavala, J. A., Casey, C. M., Manning, S. M., et al. 2021, [ApJ](#), **909**, 165

Appendix A: Data samples

Data samples for H_2 mass density values, ρ_{H_2} (and corresponding Ω_{H_2}), are summarised in Table A.1, where redshift range, H_2

measurements, and publication references are quoted. Many of them are present in [Péroux & Howk \(2020\)](#).

Table A.1. Observational determinations of molecular (H_2) gas considered in this work.

z_-	z_+	$\text{Log } \rho_{H_2,-}$	$\text{Log } \rho_{H_2,+}$	$\text{Log } \Omega_{H_2,-}$	$\text{Log } \Omega_{H_2,+}$	Reference	Survey
0.0	0.5	5.903	6.940	-5.230	-4.194	Hamanowicz et al. (2021)*	ALMACAL-CO
0.5	1.0	6.991	7.510	-4.142	-3.623	"	"
1.0	1.5	6.832	7.420	-4.301	-3.714	"	"
0.0	0.5	6.362	7.228	-4.772	-3.906	"	"
0.0	0.5	5.08	6.57	-6.05	-4.56	Garratt et al. (2021)	UKIDSS-UDS
0.5	1.0	7.10	7.33	-4.03	-3.80	"	"
1.0	1.5	7.28	7.44	-3.85	-3.69	"	"
1.5	2.0	7.47	7.60	-3.66	-3.53	"	"
2.0	2.5	7.21	7.40	-3.92	-3.73	"	"
-	0	6.581	6.992	-4.553	-4.142	Fletcher et al. (2021)	xCOLDGASS
0.003	0.369	5.17	6.36	-5.96	-4.77	Decarli et al. (2020)	ASPECS
0.271	0.631	6.78	7.33	-4.35	-3.80	"	"
0.695	1.174	7.44	7.87	-3.69	-3.26	"	"
1.006	1.738	7.61	7.87	-3.52	-3.26	"	"
2.008	3.107	7.27	7.65	-3.86	-3.48	"	"
3.011	4.475	7.20	7.52	-3.93	-3.61	"	"
2.0	3.0	6.96	7.80	-4.17	-3.33	Riechers et al. (2020a)	VLASPEC
1.95	2.85	7.041	7.748	-4.093	-3.386	Riechers et al. (2020b)	COLDz
4.90	6.70	6.146	7.041	-4.988	-4.093	"	"
0.4799	1.4799	7.47	7.72	-3.66	-3.41	Lenkić et al. (2020)	PHIBBS-2
1.0056	2.0056	7.56	7.78	-3.57	-3.35	"	"
2.0084	3.0084	7.42	7.67	-3.71	-3.46	"	"
3.1404	4.1404	6.91	7.34	-4.22	-3.79	"	"
4.2451	5.2451	6.58	7.22	-4.55	-3.91	"	"
0.003	0.369	-	<8.26	-	<-2.87	Klitsch et al. (2019)	ALMACAL-abs
0.2713	0.6306	-	<8.32	-	<-2.81	"	"
0.6950	1.1744	-	<8.39	-	<-2.74	"	"
1.006	1.738	-	<8.21	-	<-2.92	"	"
2.0	3.0	6.00	-	-5.14	-	Berta et al. (2013)	Herschel PEP

From left to right, columns refer to lower and upper redshift range limits, H_2 mass density $\rho_{H_2} [M_\odot/\text{Mpc}^3]$ with corresponding Ω_{H_2} range limits (1σ), publication reference from which H_2 data are taken or converted and observational survey. * Submitted. Private communication.

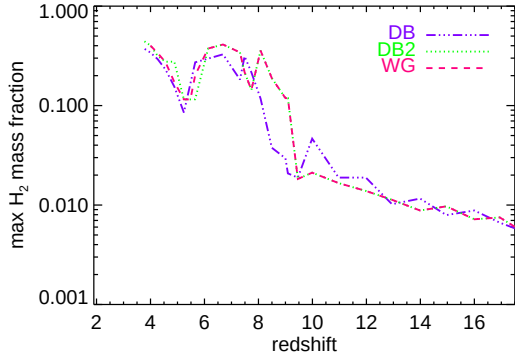


Fig. B.1. Redshift evolution of the maximum H_2 abundance reached in simulations with different H_2 self-shielding formulations: eq. 36 (violet dot-dot-dot-dashed line; HM-HISSmed-3b in Table 1) and eq. 37 (green dotted line; HM-HISSmed-3b-DB2) in [Draine & Bertoldi \(1996\)](#) and the formulation by [Wolcott-Green et al. \(2017\)](#) (magenta dashed line; HM-HISSmed-3b-WG).

Appendix B: HI and H_2 self shielding

We write the HI self shielding, $f_{\text{shield,HI}}$, as a function of H number density, n_{H} , as:

$$f_{\text{shield,HI}} = 0.985 \left[1 + \left(\frac{n_{\text{H}}}{n_0} \right)^{1.9} \right]^{-2} + 0.015 \left(1 + \frac{n_{\text{H}}}{n_0} \right)^{-0.72}, \quad (\text{B.1})$$

where $n_0 = 0.006 \text{ cm}^{-3}$ is a parameter. Asymptotically $f_{\text{shield,HI}}$ converges to 1 for $n_{\text{H}} \ll n_0$ and to 0 for $n_{\text{H}} \gg n_0$. Besides eq. B.1, we checked that the alternative use of the tables by [Rahmati et al. \(2013\)](#) does not change our findings substantially, although truncation at $z = 5$ causes an unstable behaviour in abundance calculations around that particular redshift.

For H_2 shielding, we refer to [Draine & Bertoldi \(1996\)](#) (their eq. 36 in most cases and their eq. 37 in selected runs). Alternative formulations for H_2 shielding, such as the revisitations by [Sternberg et al. \(2014\)](#) or [Wolcott-Green et al. \(2017\)](#) of the expressions of [Draine & Bertoldi \(1996\)](#), have a similar impact on the Ω_{H_2} mass density parameter. A detailed comparison of different H_2 shielding models is also done in [Luo et al. \(2020\)](#). Maximum deviations from the reference run, reached locally at different epochs, can be estimated by looking at the maximum H_2 mass fractions recorded at different z . These are more sensitive than Ω_{H_2} and are plotted in Fig. B.1 for simulations including H^- , H_2^+ and three-body formation channels, with H_2 self-shielding parameterizations by [Draine & Bertoldi \(1996\)](#) and the more recent [Wolcott-Green et al. \(2017\)](#) one. Although we observe differences of up to an order of magnitude at selected redshifts, overall the maximum H_2 mass fraction reached is not substantially affected by the prescription used to model the H_2 self shielding.

Appendix C: H_2 grain catalysis

The rate of H_2 formation due to dust grain catalysis at gas temperature T and grain temperature T_{gr} is:

$$k_{\text{H}_2,\text{gr}} = 3.5 \times 10^{-17} S_{\text{H}} \sqrt{\frac{T}{100 \text{ K}}} \text{ cm}^3/\text{s}, \quad (\text{C.1})$$

where the sticking coefficient S_{H} is given by ([Hollenbach & McKee 1979](#); [Cazaux & Tielens 2004](#)):

$$\frac{1}{S_{\text{H}}} = 1 + 0.4 \sqrt{\frac{T + T_{\text{gr}}}{100 \text{ K}}} + 0.2 \left(\frac{T}{100 \text{ K}} \right) + 0.08 \left(\frac{T}{100 \text{ K}} \right)^2. \quad (\text{C.2})$$

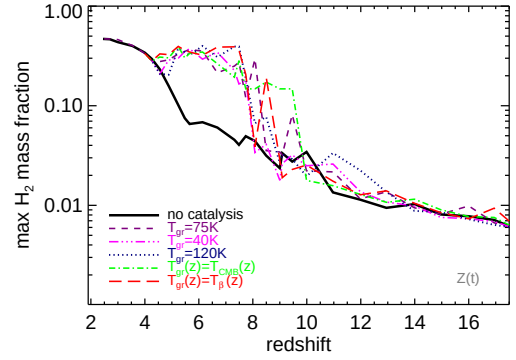


Fig. C.1. Redshift evolution of the maximum H_2 fractions reached in simulations without (solid black line; HM-HISSmed reference run) and with H_2 dust grain catalysis for $T_{\text{gr}} = 75 \text{ K}$ (purple short-dashed line; HM-HISS-cat-75-Zevol), 40 K (magenta dot-dot-dot-dashed line; HM-HISS-cat-40-Zevol), 120 K (blue dotted line; HM-HISS-cat-120-Zevol), $T_{\text{gr}}(z) = T_{\text{CMB}}(z)$ (green dot-dashed line; HM-HISS-cat-Tcmb-Zevol) and $T_{\text{gr}}(z) = T_{\beta}(z)$ with dust emissivity index $\beta = 2$ (red long dashed line; HM-HISS-cat-Tbeta-Zevol) are also considered. All the runs include metal spreading from stellar evolution, as indicated in the bottom right corner by $Z(t)$.

In the absence of precise determinations at different epochs and Z , $k_{\text{H}_2,\text{gr}}$ is linearly scaled by Z , via $k_{\text{H}_2,\text{gr}} \rightarrow k_{\text{H}_2,\text{gr}} \times Z/Z_{\odot}$.

The normalisation of eq. C.1 is similar to the one in [Thi et al. \(2020\)](#) and [Sternberg et al. \(2014\)](#), while [Omukai et al. \(2005\)](#) divide eq. C.1 by $1 + \exp[750(1/75 - 1/T_{\text{gr}})]$, which suppresses catalysis by a factor ≥ 2 at grain temperatures $T_{\text{gr}} \geq 75 \text{ K}$. The energy density transfer rate, Λ_{gr} , is computed accordingly. In the canonical form, calibrated in the near Universe,

$$\Lambda_{\text{gr}} \simeq 3 \times 10^{-33} \sqrt{T} (T - T_{\text{gr}}) n_{\text{H}}^2 \text{ erg/s/cm}^3. \quad (\text{C.3})$$

Also in this case there are alternative formulations, as e.g. in [Omukai et al. 2005](#), where the expression is multiplied by the dimensionless factor $1 - 0.8 \exp(-75 \text{ K}/T)$. Similarly to the H_2 formation rate, the energy density transfer rate is scaled by Z , $\Lambda_{\text{gr}} \rightarrow \Lambda_{\text{gr}} \times Z/Z_{\odot}$. We ran simulations by employing both eqs. C.1-C.3 and corrections by [Omukai et al. \(2005\)](#), finding differences of at most a few per cent for the H_2 fractions and median relative variations of the order of 10^{-4} for Ω_{H_2} values. For HI and neutral gas differences are even smaller.

In Fig. C.1 we explore the effect of T_{gr} by showing the evolution of the H_2 abundance obtained in simulations with the reference no-catalysis implementation, together with runs including dust grain catalysis with $T_{\text{gr}} = 40, 75$, and 120 K , as well as a z -dependent $T_{\text{gr}}(z)$ following either the CMB, $T_{\text{gr}}(z) = T_{0,\text{CMB}}(1+z)$ with $T_{0,\text{CMB}} \simeq 2.7 \text{ K}$, or the dust emissivity model with $\beta = 2$ ([da Cunha et al. 2021](#)). We note that here three-body interactions for H_2 production (considered e.g. in Fig. B.1 and F.1) are switched off. We see that grain catalysis is responsible for increasing maximum H_2 fractions at $z \simeq 4-8$ up to $\sim 50\%$ (corresponding to roughly 67% of H mass). This holds independently from the exact value of T_{gr} , or whether it evolves with redshift. Ω_{neutral} and Ω_{H_2} are unaffected by the exact choices of constant T_{gr} and are weakly affected from different scaling relations — e.g. T_{CMB} vs. T_{β} — for $T_{\text{gr}}(z)$ evolution.

In Fig. C.2 we explore the effects of metallicity on H_2 grain catalysis at $T_{\text{gr}} = 75 \text{ K}$. Indeed, such H_2 formation process is efficient mostly in cold collapsing gas after metal pollution has started. In addition to the reference simulation, we show results obtained from test runs in which we assume H_2 grain catalysis at fixed $Z = Z_{\odot}$ and $Z = 0.01 Z_{\odot}$. The largest effects are

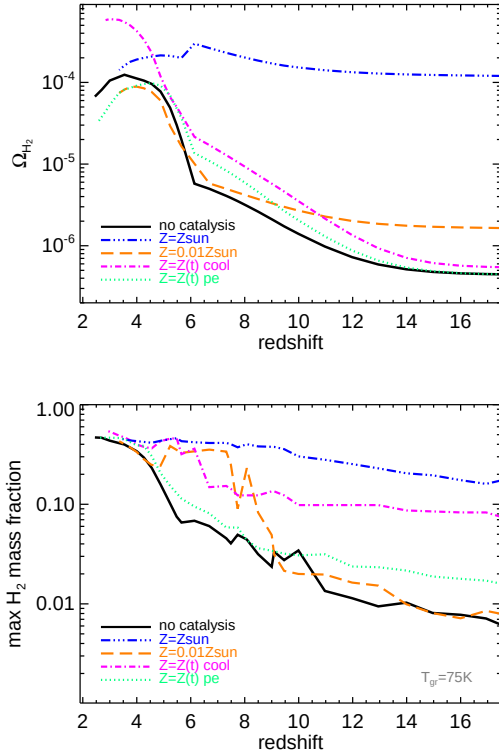


Fig. C.2. Ω_{H_2} evolution (upper panel) and maximum H_2 mass fractions (lower panel) reached in the no-catalysis simulation (black solid lines; HM-HISSmed) are compared to runs including H_2 grain catalysis at $T_{\text{gr}} = 75$ K. Gas Z is either forced to constant values of $Z = Z_{\odot}$ (blue dot-dot-dot-dashed lines; HM-HISS-cat-75- Z_{sun}) and $0.01 Z_{\odot}$ (orange dashed lines; HM-HISS-cat-75- $0.01Z_{\text{sun}}$), or consistently computed from temporal evolution of SN II, AGB, and SN Ia metal spreading and cooling from both resonant and fine-structure lines (magenta dot-dashed lines; HM-HISS-cat-75- $Z(t)$). Photoelectric heating on dust grains is tested, as well (green dotted lines; HM-HISSmed-cat-75-pe).

expected at $z \gtrsim 5$, where metallicities have a remarkable impact on Ω_{H_2} . Typical metallicities in the no-catalysis case are close to zero at $z \sim 20$ and reach values around $0.01 Z_{\odot}$ at $z \sim 10$, but they have no direct effects on H_2 , because grain catalysis is not active. In the low- Z case ($Z = 0.01 Z_{\odot}$), we see the formation of an $\Omega_{\text{H}_2} \sim 2 \times 10^{-6}$ floor at high redshift that converges at $z < 6$ to the reference trend. The formation of such a floor is due to additional H_2 formed via grain catalysis in early enriched gas. The increasingly dominant role of UV radiation at $z \lesssim 6$ provides free electrons that enhance H_2 formation in shielded and/or in recombining gas. This is consistent with a leading role played by the H^- channel, which becomes more important than low- Z gas-grain processes at the end of reionisation. The extreme $Z = Z_{\odot}$ case predicts $\Omega_{\text{H}_2} \sim 1\text{--}3 \times 10^{-4}$ during most of the cosmological evolution. These values are higher than those expected in the reference run, but one should keep in mind that they are probably unrealistic, as it is unlikely that most of the cosmic gas is polluted at solar metallicity by the first gigayear. In any case, it is a nice confirmation that, at high Z , grain catalysis seems to be the mostly relevant process for Ω_{H_2} . The effects of UV background onset around $z \simeq 6$ (with the additional contributions from the H^- channel) causes modest adjustments to the otherwise smooth Ω_{H_2} evolution. The results obtained with a constant Z highlight how assuming a fixed metallicity floor at early times could drive to misleading conclusions for H_2 estimates (off by orders of magnitude) in the first few billion years.

Maximum H_2 abundances are clearly boosted at any redshift in the (extreme) case with constant $Z = Z_{\odot}$. In the case with a $Z = 0.01 Z_{\odot}$ floor, instead, H_2 fractions are quite close to the results expected for the reference (no-catalysis) run at $z \gtrsim 10$, but, consistently with Fig. C.1, they show an enhancement at $z \simeq 4\text{--}8$ when H_2 mass fractions reach $\sim 50\%$ (i.e. 67% with respect to H mass). At $z \gtrsim 8$, H_2 fractions are similar in both cases, but corresponding Ω_{H_2} values (upper panel) differ as a consequence of the adopted Z floor that enhances H_2 production by a tiny amount in *all* the gas parcels. The cumulative result tends to an increase of Ω_{H_2} by a factor of a few at $z \gtrsim 12$. Results from the run including H_2 grain catalysis at $T_{\text{gr}} = 75$ K and time-dependent metallicity, $Z = Z(t)$, derived from consistent metal evolution and cooling from both resonant and fine-structure lines show a slightly larger Ω_{H_2} than the no-catalysis one (due to the generally increasing global metallicities) and an intermediate behaviour of the maximum H_2 fractions (resulting from early local Z values typically comprised within $\sim 10^{-2}\text{--}1 Z_{\odot}$; e.g. Maio et al. 2010). Ω_{neutral} is little affected.

Appendix D: Photoelectric heating

The photoelectric effect in the interstellar medium is caused by the absorption of UV radiation (usually produced by star formation events) from dust grains, which then re-emit electrons and heat up the surrounding medium. Therefore, the power density of photoelectric heating, Γ_{pe} , is a function of the UV field, parameterized through the dimensionless Habing (1968) parameter $G_0 \simeq 1.7$, gas temperature, T , and electron number fraction, n_e (Draine & Sutin 1987; Bakes & Tielens 1994; Weingartner & Draine 2001). The efficiency of the process, ε , depends on $G_0 \sqrt{T}/n_e$ which includes the effects of radiation, recombination rate, and electron number density:

$$\varepsilon(\psi) = \frac{0.0487}{1 + 0.004 \psi^{0.73}} + \frac{0.0365(T/10^4 \text{ K})^{0.7}}{1 + 0.0002 \psi}, \quad (\text{D.1})$$

where $\psi = G_0 \sqrt{T}/n_e$ in units of $\text{K}^{1/2} \text{ cm}^3$. The corresponding power density is

$$\Gamma_{\text{pe}} = C_{\text{pe}} \varepsilon(\psi) G_0 n_{\text{H}}, \quad (\text{D.2})$$

where $C_{\text{pe}} \simeq 10^{-24} \text{ erg/s}$ is a normalisation factor estimated in the nearby Universe and n_{H} is the H number density. Because of its dependencies, a quantitative assessment of photoelectric heating needs to be done for all the variety of conditions in which the cosmic gas could possibly be found. Qualitatively, since ε depends inversely on ψ for any fixed G_0 , gas at high (low) temperatures experiences limited (relevant) photoelectric heating. Similarly, for a given thermal state, high (low) UV fluxes lead to enhancement (quenching) of Γ_{pe} . Due to a lack of information about photoelectric heating in the distant Universe, G_0 is either kept constant or scaled by the SFR i.e. $G_0 \rightarrow G_0 \times \text{SFR}/\text{SFR}_{\odot}$, where $\text{SFR}_{\odot}$ is the Milky Way value. We tried both approaches without finding large differences. As we coupled photoelectric heating with the chemistry network in a flexible way, alternative prescriptions could be tested easily.

To understand the role of this process during cosmological structure formation, in Fig. C.2 we over-plot results for a run including both H_2 grain catalysis with Z given by the actual temporal metallicity evolution and photoelectric heating (dotted lines). The net effect on H_2 mass fractions and mass density parameters results from the trade-off between H_2 enhancement (due to dust grain catalysis) and H_2 dissociation

(due to the additional heating mechanism), as clear from the trends in the figure. Compared to the reference no-catalysis case, the final H_2 mass fractions reached (lower panel) in the presence of both photoelectric heating and H_2 grain catalysis is not larger than a factor of 2. Albeit modest, this enhancement involves regions that are increasingly enriched during cosmic time and progressively more abundantly distributed in cosmic space. The cumulative effect on Ω_{H_2} (upper panel) is marginal at $z \gtrsim 10$, but becomes visible later on, causing a steeper trend at $z \simeq 6$ -10. At $z \lesssim 6$, newly available free electrons from re-ionisation lead, also in this case, to H_2 formation.

Compared to the case including metal cooling (dot-dashed lines), the photoelectric effect is subdominant. Ω_{neutral} is little changed.

Appendix E: Fitting formula for cosmic-ray ionisation rate $\zeta(N)$ and H_2 mass build-up

A fit for the [Padovani et al. \(2018\)](#) tabulated $\mathcal{L}$ model as a function of the gas column density, N , in units of 10^{19} cm^{-2} , $N_{19} = N/(10^{19} \text{ cm}^{-2})$, is given by:

$$\zeta(N_{19}) = a N_{19}^{\alpha} \left(1 + \frac{N_{19}}{b}\right)^{\beta} e^{-(N_{19}/c)^{\gamma}}, \quad (\text{E.1})$$

where $a = 3.7221566 \times 10^{-16} \text{ s}^{-1}$ is the normalisation required to reproduce the [Padovani et al. \(2018\)](#) ζ value at $N = 10^{19} \text{ cm}^{-2}$ ($N_{19} = 1$). The other dimensionless parameters are: $b = 10^2$, $c = 2 \times 10^6$, $\alpha = -1/2$, $\beta = 1/3$ and $\gamma = 7/10$. So, ζ scales as $N_{19}^{-1/2}$ at $N_{19} \ll b$, evolves roughly as $N_{19}^{-1/6}$ in the range $b \ll N_{19} \ll c$ and decays exponentially at $N_{19} \gg c$. Since this formulation is tested on the nearby Universe, it is customary to scale ζ , which is mostly related to SN events, by the gas SFR with respect to the local one, $\text{SFR}_{\odot}$, i.e. $\zeta \rightarrow \zeta \times \text{SFR}/\text{SFR}_{\odot}$ (e.g. [Narayanan & Krumholz 2017](#)).

We test the effects of cosmic-ray heating on the H_2 evolution by employing a constant homogeneous ionisation rate of $\zeta \simeq 10^{-17} \text{ s}^{-1}$ per H atom, as well as the density-dependent one by [Padovani et al. \(2018\)](#) (eq. E.1). We also run this latter case considering cosmic-ray heating only in star forming regions, in which ζ is scaled by the gas SFR. The resulting evolution of the H_2 mass density is displayed in Fig. E.1, where we additionally show the case with no cosmic-ray heating for comparison. In general, the presence of a cosmic-ray heating floor (as in e.g. the ζ constant case, dotted line) enhances the amounts of free electrons already at early times and this can increase the formation of H_2 at $z \gtrsim 12$ by a factor of ~ 4 . Nevertheless, the additional heating from ongoing structure formation at later times leads to negative feedback effects and causes the subsequent decrease of Ω_{H_2} . As a result, at $z < 12$ the system reaches a new equilibrium for H_2 creation and destruction processes and Ω_{H_2} stays below the reference no-heating trend by almost a factor of 3 at $z \simeq 4$. The [Padovani et al. \(2018\)](#) rate is stronger by up to more than 1 dex, and therefore, if applied to all particles, creates a heating floor that easily ionises gas and dissociates H_2 even at higher redshifts. At lower redshift the resulting Ω_{H_2} behaviour converges to the constant ζ case. Applying such a model to star forming particles only smooths the extreme behaviour at early times and allows us to recover an evolution of Ω_{H_2} at low z that is similar to, although slightly smaller than (by less than a factor of 2), the reference one at $z < 6$. We conclude that cosmic-ray heating may affect H_2 abundances during the epoch of reionisation and afterwards. The impact is up to a few tens

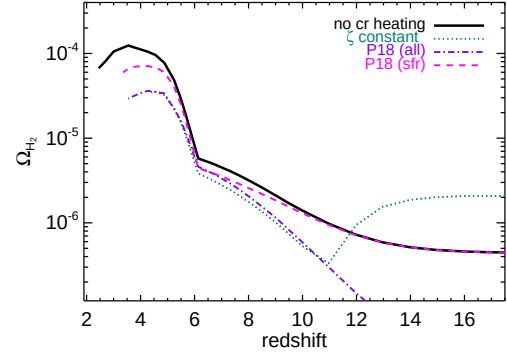


Fig. E.1. Ω_{H_2} evolution when cosmic-ray heating included in the reference implementation (black solid line, HM-HISSmed). The case of a constant homogeneous $\zeta = 10^{-17} \text{ s}^{-1}$ (turquoise dotted line, HM-HISSmed-cr) is displayed together with two cases in which [Padovani et al. \(2018\)](#)'s ζ is adopted either for all gas parcels (violet dot-dashed line, HM-HISSmed-crP18) or scaled by the local gas SFR (magenta dashed line, HM-HISSmed-crP18sfr).

of per cent for the more realistic SFR-linked case. We note that cosmic-ray heating in the early Universe typically inhibits the H_2^+ channel. Indeed, through interactions with cosmic-ray protons, H_2^+ is quickly converted into H_3^+ . This latter is an unimportant coolant that contributes no more than a few per cent of the total cooling ([Glover & Savin 2009](#)) and at large densities, where the gas tends to become fully neutral, suffers from H^+ removal, dissociative recombination, and H-impact dissociation. Maximum molecular fractions reached are consistent with those derived in the previous cases as well as the density parameters of HI/neutral gas for the SFR-linked case. In the other cases, Ω_{neutral} values at $z < 5$ converge to slightly lower values than the reference ones. While the homogeneous presence of cosmic-ray heating is an idealized test case, we can consider as a fiducial model the one including cosmic-ray heating in star forming regions according to the [Padovani et al. \(2018\)](#) description.

Appendix F: H_2 formation channels

H_2 formation can be led by different pristine-chemistry processes. To understand which of these is the main driver of Ω_{H_2} evolution, we examine the effects of the H_2^+ , H^- and three-body channels (for the latter we follow [Forrey 2013](#), which improves on previous studies by e.g. [Palla et al. 1983](#), [Orel 1987](#), [Abel et al. 2002](#) and [Flower & Harris 2007](#)). In all the runs we include HI shielding (eq. B.1) and H_2 shielding ([Draine & Bertoldi 1996](#)). Figure F.1 displays the evolution of Ω_{H_2} (top panel) and of the maximum H_2 mass fraction (bottom panel). Three-body interactions dominate H_2 formation in dense, cold regions, where HI atoms are abundant, however they do not impact significantly the global Ω_{H_2} values reached by H_2^+ and H^- channels (upper panel). Compared to the case with only H_2^+ and H^- channels, three-body processes locally enhanced H_2 formation by a factor of almost 10 at $z \lesssim 8$, raising the H_2 mass fractions to about 50% by the end of reionisation (lower panel). To understand better the relative role played by the H^- and H_2^+ channels, in Fig. F.1 we show results from simulations including only the H_2^+ channel or neither. When no H_2 formation channel is considered, both Ω_{H_2} and H_2 fractions remain practically constant at the initial-condition values. Adding the H_2^+ formation channel increases both the H_2 density parameter and the H_2 fraction, but resulting values are still well below the required ones. Reliable values are obtained by including, besides the H_2^+ , the H^-

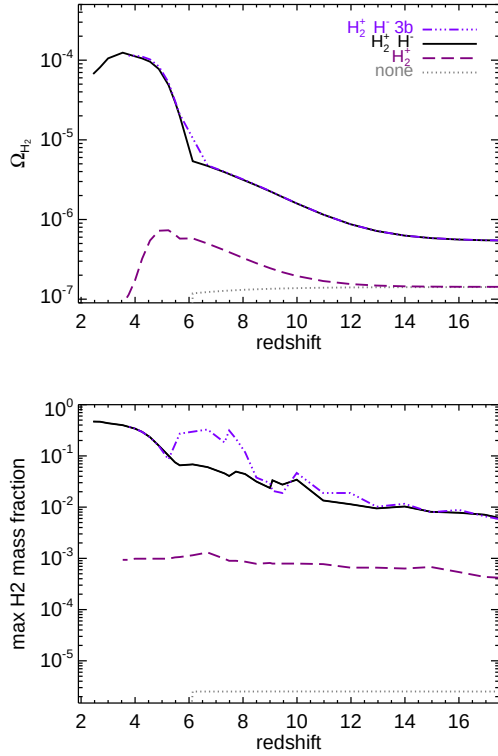


Fig. F.1. Redshift evolution of Ω_{H_2} (upper panel) and H_2 (lower) fractions obtained in the reference run (black solid line; HM-HISSmed in Table 1), as well as in simulations including also three-body processes (violet triple-dot-dashed line; HM-HISSmed-3b), only the H_2^+ channel (purple dashed line; HM-HISSmed- H_2^+), and none of the H_2 channels (grey dotted line; HM-HISSmed-none).

channel, which appears to be crucial for H_2 pristine chemistry. This can be understood in light of the sparsity of high-density regions (this limits the role of three-body processes), the large amount of cosmic gas at moderate densities (above $0.1\text{--}1\text{ cm}^{-3}$) with temperatures $\lesssim 10^4\text{ K}$ and the larger reaction rates of the H^- channel with respect to the H_2^+ .

Appendix G: Comparison of UV background effects

In Fig. G.1 we quantify the impact of different UV backgrounds on the amount of cold gas, showing the evolution of Ω_{neutral} and Ω_{H_2} for un-shielded HM, P19 and FG20 runs with the basic implementation. For all the UV background scenarios, Ω_{neutral} is higher than Ω_{H_2} at all redshifts. At high z , before the onset of photoheating processes, the HI content is much larger than the one of H_2 , reflecting the primordial chemical composition of a mostly neutral cosmic gas with neutral fractions close to the baryon fraction ($\Omega_{0,b} \approx 0.045$) and molecular fractions around 10^{-6} . At later times, Ω_{neutral} decreases and Ω_{H_2} increases with a relative ratio shrinking by a few dex. The displayed trends are sensitive to the onset of the UV background at $z \approx 6, 8.3, 15.1$ for HM, FG20 and P19, respectively, when the transition from a neutral to an ionised phase is initiated. Then, Ω_{neutral} deviates from its initial value ~ 0.045 , while molecular gas responds to the new thermal conditions. The HM and FG20 scenarios produce similar results at $z \gtrsim 8$ (when neither background is turned on), but at lower z the larger FG20 rates are able to ionise gas and dissociate molecules more efficiently than the HM. For example, FG20 HI and HeI rates at $z \approx 6$ are $\sim 10^{-12}\text{ s}^{-1}$, while HM

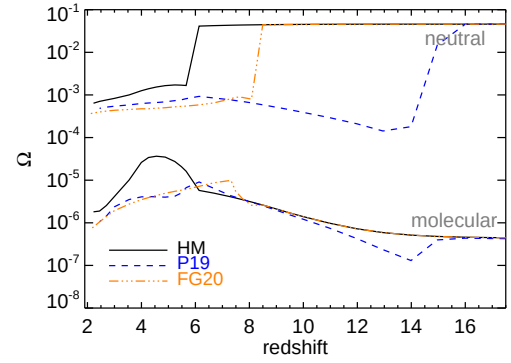


Fig. G.1. Redshift evolution of the neutral and molecular density parameters for the HM (solid black lines), P19 (dashed blue) and FG20 (dot-dot-dashed orange) simulations, respectively.

rates are below 10^{-15} s^{-1} . At the same z , FG20 HI and HeI heating power is above 10^{-24} erg/s , while the HM ones are below 10^{-26} erg/s . A peculiarity of the P19 model is its strength at early times, which causes H photoionisation by $z \approx 14$, when minimal levels of $\Omega_{\text{neutral}} \sim \text{few } 10^{-4}$ and $\Omega_{\text{H}_2} \sim 10^{-7}$ are reached. Later on, with gas cooling re-balancing heating, some HI reforms and H_2 catches up.

Appendix H: Impact of SNe

In Fig. H.1, we show Ω_{neutral} and Ω_{H_2} as extracted from simulations including different SN efficiencies with a standard HM background, complementing our previous discussion of Fig. 2. Efficiencies larger than the reference 0.1 value are suited for extremely powerful population-III sources, which would inhibit H_2 and star formation in the first few Gyr. When compared to the reference 0.1 case, values of the molecular-gas density parameters, Ω_{H_2} , are lower (higher) for SN efficiencies of 0.5-1 (0.01). That is a result of the more (less) efficient molecular-gas removal from star forming regions by stronger (weaker) feedback and the major (minor) destruction of H_2 into HI. Correspondingly, Ω_{neutral} values increase smoothly until $z \lesssim 6$ at slightly lower (higher) levels when weaker (stronger) feedback is active. Qualitatively, these conclusions hold independently from the UV background (e.g. P19, which is not shown for clarity) and the variations found are comparable to those from other effects, such as cosmic-ray heating in star forming regions.

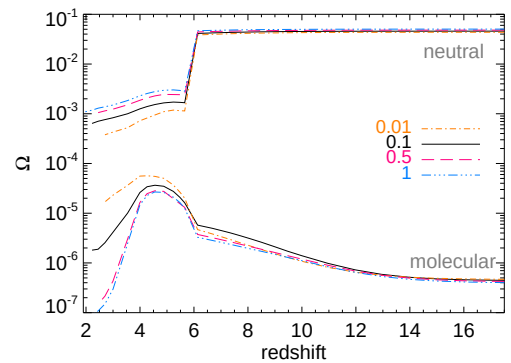


Fig. H.1. Redshift evolution of the neutral and molecular density parameters in models with SN efficiency of 0.1 (black solid line, HM), 0.01 (yellow dot-dashed line, HM-0.01), 0.5 (magenta-red dashed line, HM-0.5) and 1 (azure dot-dot-dot-dashed line, HM-1).

Appendix I: The role of IMF and winds

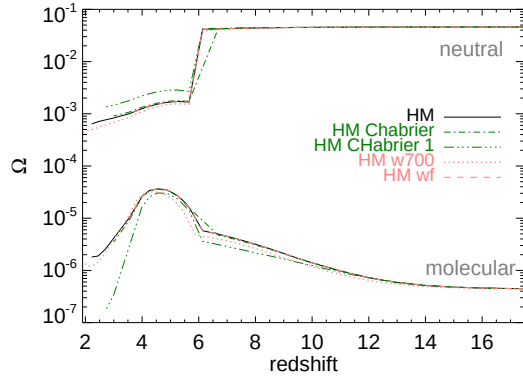


Fig. I.1. Redshift evolution of the neutral and molecular density parameters for the HM background setup, having wind velocity of 350 km/s, wind delay time of 0.025 Hubble time and a Salpeter IMF (black solid lines, HM). Results obtained by increasing the wind velocity to 700 km/s (pink dotted lines, HM-w700), the wind delay time to 0.1 Hubble time (pink dashed lines, HM-wf) and by adopting a Chabrier IMF (green dot-dashed lines, HM-Chabrier) or a Chabrier IMF with unitary SN efficiency (green dot-dot-dot-dashed lines, HM-1-Chabrier) are shown, too.

In Fig. I.1, we compare the effects of different IMFs for various feedback schemes. We consider as reference a simulation with HM background, Salpeter IMF, SN efficiency of 0.1, 350 km/s wind velocity and wind delay time of 0.025 the Hubble time. This simulation is re-run with variations including: a Chabrier IMF, a Chabrier IMF with unitary SN efficiency, a wind velocity of 700 km/s and a longer wind delay time 0.1 the Hubble time. Effects of a Chabrier IMF are small and results tend to follow the evolution of the corresponding runs with a Salpeter IMF. The small effects due to changes of the IMF originate from the small difference in the injected entropy and the SN rates varying only by a factor of 1.4. The model with Chabrier IMF and unitary SN efficiency features some departures from the reference for both Ω_{neutral} and Ω_{H_2} , indicating a more relevant role of the

feedback scheme. In the case with wind velocity of 700 km/s, the results are very close to those of the reference model. Changing other wind parameters, such as the wind delay time to get re-coupled to hydrodynamic, has no dramatic effect. Similar conclusions hold for different-UV scenarios, too.

Appendix J: Estimates of the dynamical time

A test mass released from rest at distance r from the center of the gravitational potential of a constant density field, ρ , under assumption of spherical symmetry, moves according to the equation of motion of a harmonic oscillator:

$$\ddot{r} = -\frac{GM(r)}{r^2} = -\frac{4\pi G\rho}{3}r, \quad (\text{J.1})$$

being G the gravitational constant and $M(r)$ the mass enclosed within r . The angular frequency ω satisfies the relation $\omega^2 = 4\pi G\rho/3$ and the period is

$$T = \frac{2\pi}{\omega} = \sqrt{\frac{3\pi}{G\rho}}. \quad (\text{J.2})$$

The test mass reaches the center in 1/4 the oscillation period, i.e. in a dynamical time, t_{dyn} (e.g. Binney & Tremaine 2008):

$$t_{\text{dyn}} \equiv \frac{T}{4} = \sqrt{\frac{3\pi}{16G\rho}}. \quad (\text{J.3})$$

If, at any given redshift, $\rho \equiv \Delta\rho_{\text{crit}}$, the critical density is $\rho_{\text{crit}} = 3H^2/(8\pi G)$, and the Hubble time is $t_{\text{H}} = 1/H$, then

$$t_{\text{dyn}} = \sqrt{\frac{3\pi}{16G\Delta\rho_{\text{crit}}}} = \frac{\pi}{\sqrt{2\Delta}} t_{\text{H}}, \quad (\text{J.4})$$

For $\Delta \simeq 100$ up to 2000, t_{dyn} decreases from $t_{\text{dyn}} \simeq 0.2 t_{\text{H}}$ down to $0.05 t_{\text{H}}$. A typical value of $\Delta \simeq 500$ (corresponding to ~ 1800 times the mean matter density, or about 10^4 times the mean baryon density) leads to $t_{\text{dyn}} \simeq 0.1 t_{\text{H}}$.