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Biases in retrieving planetary signals in the presence of quasi-periodic stellar activity

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ABSTRACT

Gaussian process regression is a widespread tool used to mitigate stellar correlated noise in radial velocity (RV) time series. It is particularly useful to search for and determine the properties of signals induced by small-sized low-mass planets ($R_p < 4 R_\oplus$, $m_p < 10 M_\oplus$). By using extensive simulations based on a quasi-periodic representation of the stellar activity component, we investigate the ability in retrieving the planetary parameters in 16 different realistic scenarios. We analyse systems composed by one planet and host stars having different levels of activity, focusing on the challenging case represented by low-mass planets, with Doppler semi-amplitudes in the range $1\text{--}3 \text{ m s}^{-1}$. We consider many different configurations for the quasi-periodic stellar activity component, as well as different combinations of the observing epochs. We use commonly employed analysis tools to search for and characterize the planetary signals in the data sets. The goal of our injection-recovery statistical analysis is twofold. First, we focus on the problem of planet mass determination. Then, we analyse in a statistical way periodograms obtained with three different algorithms, in order to explore some of their general properties, as the completeness and reliability in retrieving the injected planetary and stellar activity signals with low false alarm probabilities. This work is intended to provide some understanding of the biases introduced in the planet parameters inferred from the analysis of RV time series that contain correlated signals due to stellar activity. It also aims to motivate the use and encourage the improvement of extensive simulations for planning spectroscopic follow-up observations.

Key words: methods: numerical – methods: statistical – techniques: radial velocities – stars: activity – planetary systems.

1 INTRODUCTION

Over the last two decades, ground and space-based transit surveys have unveiled the very rich and unexpected variety of distant worlds orbiting stars of different spectral type, age and activity levels in the Galaxy. Moreover, starting or upcoming surveys will dramatically increase the number of planet detections and the variety of the statistical planetary sample within the next decade. Most of the currently known exoplanets have been discovered through transit observations, which alone provide only the size of the planets. Unless transit timing variations (TTV) are detected (e.g. Agol & Fabrycky 2017), the planetary masses have to be measured through the analysis of the radial velocity (RV) time variations of the host star, induced by the gravitational interaction with the planets.

For transiting extrasolar planets with measured masses, the bulk densities can be determined, and through the analysis of the planetary mass–radius diagram one can infer the bulk composition and

structure of observed planets, and compare them with formation and evolution models. This in turn helps to put reliable constraints on the different migration mechanisms that have been proposed to describe the observed architectures of the planetary systems. Moreover, precise measurements of the bulk density can help in the prediction of the surface temperature of potentially habitable planets.

One of the most interesting results obtained thanks to the discoveries made by the Kepler/K2 mission is that the radii of small, close-in extrasolar planets ($R < 4 R_\oplus$ and $P < 100 \text{ d}$) follow a bi-modal distribution (Owen & Wu 2013; Fulton et al. 2017; Zeng et al. 2017a; Zeng, Jacobsen & Sasselov 2017b). Different studies have confirmed and strengthened this finding by improving the precision on the host star radii (Berger et al. 2018; Fulton & Petigura 2018). A gap located at $\sim 1.5\text{--}2 R_\oplus$ divides a population of super-Earth/Earth-sized planets from that of sub-Neptunes. This evidence could be the direct proof that photoevaporation is a major mechanism responsible for planetary mass-loss, as predicted by some theoretical studies (e.g. Owen & Wu 2013; Lopez & Fortney 2014). The smallest planets below the gap could have lost the outer gaseous envelope through an X-UV radiation-driven erosion, while

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those with larger radii could still retain a significant fraction of volatiles. In this context, the smallest planets are expected to have the highest bulk densities, indicative of a rocky composition, while planets above the gap should have lower densities as a consequence of their H_2/He gaseous envelopes (gas dwarfs) or H_2O -dominated ices/fluids (water worlds), according to two of the mainstream scenarios (e.g. Owen 2019; Wu 2019; Zeng et al. 2019).

The discovery of the ‘radius gap’ for small-sized planets makes the accurate and precise measurement of their masses a still more urgent matter. Measuring the masses of small-size, low-mass planets through the RV method is not an easy task for several reasons. First of all, currently only few high-resolution and high-stability spectrographs in use for several years (e.g. HARPS, HARPS-N, HIRES) are able to provide the RV precision necessary for precise measurements of the RV amplitude of low-mass exoplanets. The ‘weighing’ of low-mass planets is made an even more complex task by crucial aspects, such as the observing conditions, the magnitude, and spectral type of the host star, the orbital period of the planet, and the level of the stellar activity, which can have a major negative impact on the analyses (e.g. Dumusque 2016; Fischer et al. 2016; Dumusque et al. 2017). All these issues must be carefully accounted for when planning observing campaigns aimed at characterizing extrasolar planets, and some preparatory, target-tailored analyses are usually performed to define the best observing strategy to measure masses with the best precision possible (e.g. Damasso et al. 2018).

In this study we define a framework that could help the selection of the most promising targets for a spectroscopic follow-up with chances to provide exoplanet masses with good accuracy and precision. We investigate reliable scenarios typically faced by teams involved in characterization studies of exoplanets, and test tools for data analysis that are presently in the toolbox of every exoplanet hunter. We use extensive simulations of RV data sets, described in Section 2, for two types of analyses. In the first part of the paper (Section 3) we use statistics to investigate how accurately the planetary signals are retrieved in presence of a quasi-periodic stellar activity component. Here we consider: (i) systems with only one planet; (ii) different levels of stellar activity; (iii) stellar rotation periods P_{rot} close to or well-separated from the planetary orbital period P_{orb} ; (iv) short and long evolutionary time-scales of the correlated stellar activity signal included in the RV time series; (v) the case of a survey carried out with only one spectrograph during one and two observing seasons, in order to simulate a scenario representative of on-going and future planet characterization campaigns such as those focused on Kepler/K2 or TESS targets (the inclusion of RV measurements collected with more than one instrument would introduce a higher level of complexity that we decided to avoid in this work, nevertheless without making our simulations less realistic). The choice of simulating planets with $P_{\text{orb}} \sim P_{\text{rot}}$ originates from the intrinsic difficulties encountered in separating the stellar activity from the planetary signal in real RV data sets, when they have very similar periods (e.g. Vanderburg et al. 2016).

The blind detection of small-amplitude planetary signals is another challenging aspect related to RV time series affected by stellar activity. Simulated RV time series, containing signals due to stellar activity, have been used in previous works to test techniques for detecting planets (e.g. Feng et al. 2016; Dumusque et al. 2017), or to apply a variety of methods to estimate the Bayesian evidence for a range of planetary signals (Nelson et al. 2018). Pinamonti et al. (2017) studied the efficiency of different period-search approaches in retrieving small-amplitude planetary signals, making use of simulated data sets also containing simple modelling of the stellar activity. In this perspective, we exploit the mock data sets for a complementary analysis aimed at characterizing features appearing

in the periodograms that can be related to the different properties of the simulated quasi-periodic stellar activity scenarios. This second part of our study is described in Section 4. As done by Pinamonti et al. (2017), the frequency content of each data set is investigated by means of three common and publicly available softwares: the Generalized Lomb–Scargle periodograms (GLS; Zechmeister & Kürster 2009), the Bayesian Generalized Lomb–Scargle (BGLS; Mortier et al. 2015), and the FREquency DEComposer (FREDEC; Baluev 2013). The results of this analysis can be useful to interpret the morphology of the periodograms calculated on real data, which usually are the first to be investigated when searching for planetary signals.

2 SIMULATION SET-UP

In this work we aim to explore a number of realistic scenarios through a statistical analysis of a large number of samples. We simulated systems consisting of only one planet to keep the size of the parameter space limited, since the inclusion of additional planets would require a much larger set of simulations in order to cover many system architectures and draw statistically meaningful conclusions. We assume that all the data have been collected with the same instrument. In what follows, we summarize the main features that we have taken into account to simulate the RV data sets, and provide the justification for their adoption.

2.1 Planetary Doppler signals

We simulated planets on circular orbits, which is a reasonable assumption for low-mass planets with low P_{orb} (Van Eylen et al. 2019). The semi-amplitude of the Doppler planetary signal K_p was kept fixed to 1 m s^{-1} for all the cases. The planetary orbital periods P_{orb} were generated between ~ 10 and 20 d , either close or far apart from the stellar rotation period P_{rot} (see Section 2.2). Assuming $K_p = 1 \text{ m s}^{-1}$ and K-to-mid M dwarfs as host stars,¹ the corresponding planetary masses are in the range $1.5\text{--}4.0 M_{\oplus}$. Using the relations of Weiss & Marcy (2014) to provide likely estimates for the planet sizes, this mass interval corresponds to radii in the range $1.1\text{--}1.5 R_{\oplus}$. This is the interval that includes the first mode of the bi-modal distribution of close-in planet sizes (Fulton et al. 2017; Fulton & Petigura 2018). Therefore, we simulated systems that are particularly challenging for the state-of-the-art high-precision and high-stability spectrographs that can be accessed nowadays. None the less, they are among the more interesting scenarios for exoplanet characterization studies.

2.2 Stellar activity model

The stellar component in the RVs was simulated as a quasi-periodic signal, which is described by the kernel with the same name used in Gaussian process (GP) regression analysis. The quasi-periodic GP model is often used to effectively correct (mitigate) the stellar activity term in RV time series that contain signals modulated on P_{rot} (e.g. Affer et al. 2016; Damasso & Del Sordo 2017; Pinamonti et al. 2018), and the effective use of GP models in recovering small-amplitude planetary signals was demonstrated for the case of synthetic RV time series (e.g. Dumusque et al. 2017). As often

¹In this work we do not assume stars of some specific spectral type, since this information is not crucial for the simulation set-up. In general, we consider a typical star observed by space-based transit surveys as a representative target, i.e. a main-sequence star of spectral type between G and M, sufficiently bright to be selected for high-precision spectroscopic follow-up.

happens, the stellar rotation period can be measured from space- or ground-based photometry, or from time series of spectroscopic activity indicators. A quasi-periodic model can be assumed as a realistic, even if not necessarily complete, representation of the stellar activity contribution due to active regions. Our simulations do not have the same level of detail as those devised by Dumusque (2016), which also include contributions such as those due to stellar oscillations, granulation, and supergranulation. None the less, by injecting a quasi-periodic signal we are simulating a reliable scenario useful for a statistical study, despite being only one of several possible representations of the stellar component in RV time series.

The quasi-periodic kernel used in our analyses is described by the following covariance function and hyper-parameters

$$\mathcal{K}(t, t') = h^2 \times \exp \left[-\frac{(t - t')^2}{2\tau_{\text{AR}}^2} - \frac{\sin^2\left(\frac{\pi(t - t')}{P_{\text{rot}}}\right)}{2w^2} \right] + \sigma_{\text{RV}}^2(t) \times \delta_{t,t'}, \quad (1)$$

where $\mathcal{K}(t, t')$ represents the covariance matrix element between observation at time t and t' , h is the amplitude of the correlations; P_{rot} is the stellar rotation period of the star; w is the length-scale of the periodic component, describing the level of high-frequency variation within a complete stellar rotation; τ_{AR} is the correlation decay time-scale, that can be physically related to the lifetime of the active regions (AR); and $\sigma_{\text{RV}}(t)$ is the RV uncertainty at epoch t (see next section).

We explored two different ranges of P_{rot} , by adopting $P_{\text{rot}} \sim 10$ d for active stars and $P_{\text{rot}} \sim 20$ d for the low-activity sample. This choice is rather arbitrary but based on the known fact that more active stars tend to rotate faster (e.g. Stelzer et al. 2016; Mascareño et al. 2018).

Among the GP hyperparameters, τ_{AR} is particularly tricky, as it is not clear whether in general it carries some real physical information. This is true especially when a consistency check is not possible using contemporary photometric observations. For instance, several examples exist of RV data sets we have analysed using a quasi-periodic GP model for which estimates of τ_{AR} have values close to P_{rot} (e.g. Damasso et al. 2018; Haywood et al. 2018; Malavolta et al. 2018; Pinamonti et al. 2018). On the other hand, other studies cast doubts on this hypothesis, stating that much longer time-scales solutions should be more physically valid, especially for M dwarfs (e.g. Perger et al. 2017, and references therein). We explore here two different regimes for τ_{AR} , by simulating rapidly evolving correlations, $\tau_{\text{AR}} \sim P_{\text{rot}}$, and stars with activity evolving over longer time-scales, $\tau_{\text{AR}} \sim 10 \times P_{\text{rot}}$.

As for the amplitude of the stellar signals, h , we investigated two representative regimes of stellar activity. We defined them on the basis of the typical scatter observed in the RVs² for a low-activity star, $h \sim 3 \text{ m s}^{-1}$, and a high-activity star, $h \sim 15 \text{ m s}^{-1}$ (e.g. Santos et al. 2000; Suárez Mascareño et al. 2017; Mascareño et al. 2018; Damasso et al. 2019). In a more general sense, our definition of low and high stellar activity levels should be intended as relative to the small semi-amplitude of the planetary signal investigated in this work, i.e. $h \gtrsim K_p$ and $h \gg K_p$.

2.3 RV uncertainties

We assumed that the RV measurements are collected by a high-resolution and high-stability spectrograph, as HARPS or HARPS-

N, in order to simulate a realistic follow-up campaign in terms of access to the observing facilities. We took into account the expected average precision for such instruments³ and for a typical target eligible for follow-up observations (see e.g. Fischer et al. 2016). For instance, the RV precision expected with HARPS-N for a K0V star of magnitude $V = 10.5$, with 1800 s of exposure taken at air mass 1.2 and with a seeing of 1.2 arcsec, is $\sigma_{\text{RV}} \sim 1 \text{ m s}^{-1}$.

However, to simulate a more realistic final error budget we adopted a lower average data precision of 2 m s^{-1} , which is equivalent to considering an additional noise term $\sim 1.7 \text{ m s}^{-1}$ added in quadrature to the nominal uncertainty. This can realistically represent what is expected for fainter targets, and takes into account possible worsening factors such as the cross-correlation function (CCF) noise, the rotational broadening of the CCF, and additional noise dependent on the specific RV-extraction algorithm. We generated the uncertainty for each data point from a normal distribution with mean equal to 2 m s^{-1} and standard deviation equal to 0.3 m s^{-1} .

2.4 Observing seasons and epochs

We simulated up to two consecutive observing seasons (or semesters). We analysed the time series with one and two seasons of observations as two separate cases, investigating the significance of the retrieved activity and planetary parameters as a function of the number of measurements.

To make the simulations realistic, the epochs of observation for the first semester have been generated adopting a typical schedule of nights with HARPS-N at the TNG telescope in La Palma allocated to the GTO collaboration⁴ and to the GAPS/GAPS2 programmes (Benatti et al. 2016), which are organized in shared risk mode. In our case, we adopted the real allocated observing time between the end of 2017 October and the end of 2018 March, consisting in 63 nights. We assumed that the target was visited once per night, and for each night we generated randomly an observing time from a normal distribution with mean equal to the midnight of that date and standard deviation equal to 0.01 d. Then, taking into account any loss due to bad weather, or Moon contamination constraints, or technical problems, we assumed a duty cycle equal to 65 per cent⁵ and randomly drawn 40 out of 63 epochs, which we define hereafter as the $N_{\text{epochs},s1}$ ensemble.

In the case of two semesters of observations, we added 40 additional time stamps to $N_{\text{epochs},s1}$. These new time stamps were randomly drawn from an array of equally spaced epochs delayed by 365 d with respect of the first semester. As before, the epochs were randomly shifted around the midnight of the date. Then, each final data set of epochs used to simulate two semesters consists of $N_{\text{epochs},s2} = 80$. Fig. 1 shows examples of randomly drawn $N_{\text{epochs},s1}$ and $N_{\text{epochs},s2}$ time stamps.

This procedure was repeated 50 times, resulting in 50 groups of simulated RV data sets, both for one and two observing seasons. Each group is composed of 100 RV time series that share the same time stamps, with 5000 simulated data sets for each scenario, and 80 000 mock data sets in total. By varying the epochs within each group, coupled to the randomly drawn values of P_{orb} and $T_{0,b}$,

³This can be estimated through the on-line exposure time calculators available at <https://www.eso.org/observing/etc/bin/gen/form?INS.NAME=HARPS+INS.MODE=spectro> and <http://www.tng.iac.es/instruments/harps/>
⁴<https://plone.unige.ch/HARPS-N/science-with-harps-n>

⁵This duty cycle is the typical percentage of useful time for the GAPS programme after five years of observations.

²Referring to the measurements collected with the kind of spectrographs considered in this work.

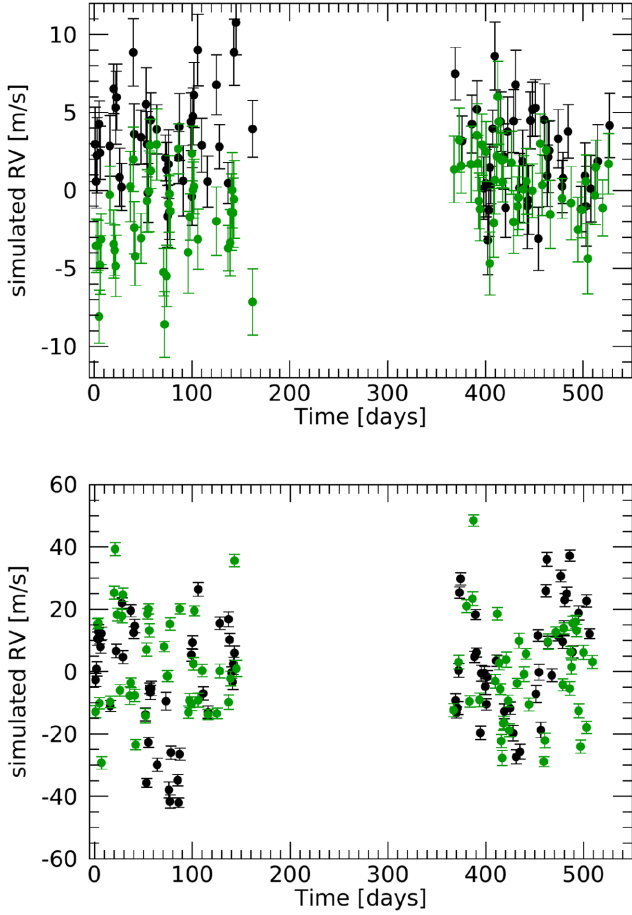


Figure 1. Examples of mock RV data sets used in this work. *Upper panel:* Two seasons of data for low activity stars with $P_{\text{rot}} \neq P_{\text{orb}}$ and $\tau_{\text{AR}} \gg P_{\text{rot}}$. *Lower panel:* Two seasons of data for active stars with $P_{\text{rot}} \sim P_{\text{orb}}$ and $\tau_{\text{AR}} \sim P_{\text{rot}}$.

we made the results independent from a particular choice of the observing sampling, as discussed in B, despite the epochs are drawn from the same ‘mold’ calendar. A more detailed investigation of the effects due to different samplings is beyond the scope of this paper.

2.5 Global model and generation of the mock data sets

The final model used to simulate each data set is the sum of one circular orbit (characterized by semi-amplitude K_b , period P_b , and time of inferior conjunction $T_{0,b}$) and a correlated quasi-periodic signal representing the stellar activity contribution. For each simulated time series, the model parameters have been randomly drawn from distributions as shown in Table 1, depending on the specific astrophysical scenario. Then, after injecting the two signals, each data point of the time series was randomly shifted within its error bar $\sigma_{\text{RV}}(t)$ (Table 1), using a normal distribution centred on zero and with $\sigma = \sigma_{\text{RV}}(t)$. Examples of simulated data sets are shown in Fig. 1. It is worth noticing that stellar and planetary parameters used to simulate the one season data sets and the corresponding two seasons data sets are not the same, since we were not interested in studying the effect of additional observations on a star-by-star basis, but only in a statistical sense.

A key point in our simulations is that, in each mock data set, the stellar activity term was randomly drawn using the `sample` function of the GP object implemented in the `GEORGEv0.2.1`

Table 1. Simulation set-up: how each parameter has been drawn to generate the total 80 000 data sets simulated in this work.

Parameter	Low activity	High activity
h (m s^{-1})	$\mathcal{N}(3, 0.5^2)$	$\mathcal{N}(15, 1^2)$
P_{rot} (d)	$\mathcal{N}(20, 1.5^2)$	$\mathcal{N}(10, 1^2)$
τ_{AR} (d)	$\mathcal{N}(\mu_{P_{\text{rot}}}, \sigma_{P_{\text{rot}}}^2)$ [short τ_{AR}]	$\mathcal{N}(10 \times \mu_{P_{\text{rot}}}, 10^2)$ [long τ_{AR}]
w	$\mathcal{N}(0.5, 0.2^2)$	
K_b (m s^{-1})		1, fixed
P_b (d)	$\mathcal{N}(\mu_{P_{\text{rot}}}, \sigma_{P_{\text{rot}}}^2)$ [$P_{\text{orb}} \sim P_{\text{rot}}$]	$\mathcal{N}(18, 1.5^2)$ [$P_{\text{orb}} \neq P_{\text{rot}}$]
$T_{0,b}$ (d)	$\mathcal{N}(13, 1.5^2)$ [$P_{\text{orb}} \neq P_{\text{rot}}$]	$\mathcal{N}(50, 5^2)$ [$P_{\text{orb}} \neq P_{\text{rot}}$]
σ_{RV} (m s^{-1})		$\mathcal{N}(2, 0.3^2)$

package (Ambikasaran et al. 2014) used to define the GP framework. Once the GP hyperparameters have been drawn, the `sample` function returns a randomly drawn list of predictions at the time stamps of the observations.⁶ This allows for simulations free from a particular representation of the stellar activity component given a set of hyperparameters and, within our working framework, this procedure makes our results statistically representative of what it is expected on average for an activity signal described by a quasi-periodic model.

The general properties of the distributions of the simulated parameters are summarized in Table A1. To define the final set of mock RV time series to be analysed, we adopted selection criteria in order to avoid overlaps (interchange) between samples with $P_{\text{rot}} \sim P_{\text{orb}}$ and those with $P_{\text{rot}} \neq P_{\text{orb}}$, so that they represent two distinct groups. We imposed constraints on $|P_{\text{rot}} - P_{\text{orb}}|$: concerning samples with $P_{\text{rot}} \sim P_{\text{orb}}$ we considered only those for which $|P_{\text{rot}} - P_{\text{orb}}| < 4$ d, while for samples with $P_{\text{rot}} \neq P_{\text{orb}}$ we analysed only samples for which $|P_{\text{rot}} - P_{\text{orb}}| > 4$ d. This selection resulted in a very low percentage of rejected samples for the case of active stars (< 1.5 per cent), while between 6 per cent and 8 per cent of the mock data sets were removed from the analysis for stars with low level of activity, ensuring a statistically large number of RV time series.

3 MONTE CARLO FITTING ANALYSIS

We first analysed the simulated data sets described in Section 2 from the perspective of someone interested in determining the mass of a transiting planet, within the framework of GP regression to model the stellar activity signal. Hereafter we describe the set-up used for a Monte Carlo (MC) analysis of the simulated RV data sets, then we summarize the results schematically by distinguishing among different scenarios.

3.1 Analysis set-up

Conservatively, we assumed that the planet orbital period is known from the transit analysis with a precision of 0.5 d, and that P_{rot} can be constrained with a precision of 5 d from photometry and/or from other activity diagnostics, as those derived from high-resolution spectra. We fit the planetary signal with a Keplerian with null eccentricity, and the stellar signal using the same GP kernel described in equation (1). Our working hypothesis is that the choice

⁶Details can be found in <http://betatim.github.io/posts/Gaussian-processes-with-george/>

Table 2. Priors used to recover the model parameters through an MC sampling combined with a GP regression.

Jump parameter	Low activity	High activity
h (m s ⁻¹)	$\mathcal{U}(0, 10)$	$\mathcal{U}(0, 30)$
τ_{AR} (d)		$\mathcal{U}(0, 1000)$
w		$\mathcal{U}(0, 1)$
P_{rot} (d)	$\mathcal{U}(P_{\text{rot, sim.}} - 5, P_{\text{rot, sim.}} + 5)$	
K_b (m s ⁻¹)		$\mathcal{U}(0, 5)$
P_{orb} (d)	$\mathcal{U}(P_{\text{orb, simul.}} - 0.5, P_{\text{orb, simul.}} + 0.5)$	
$T_{0, b}$ (d)		$\mathcal{U}(0, 100)$
σ_{jit} (m s ⁻¹)		$\mathcal{U}(0, 10)$

of a quasi-periodic kernel is justified, so that this representation can be used confidently to model the correlated stellar activity signal present in the RV time series. We supposed that the amplitude h of the stellar activity term cannot be well constrained a priori, but it could be as high as 30 m s⁻¹ for an active star. For the evolutionary time-scale τ_{AR} we adopted a large uninformative prior, since it is usually difficult to constrain this hyperparameter a priori (an alternative prior choice is discussed in Section 3.2.2). All these assumptions are at the basis of our choice of the prior distributions used in the MC analysis (Table 2).

Our fitting framework includes a constant jitter term σ_{jit} which is added in quadrature to the uncertainty $\sigma_{\text{RV}}(t)$, and takes into account any additional source of uncorrelated noise, instrumental, and astrophysical. Doing this we followed a common practice, therefore we included σ_{jit} in our analysis even if our simulated data were built without considering any additional uncorrelated noise, that is $\sigma_{\text{jit}} = 0$ m s⁻¹ in the mock RVs by construction. It is an interesting exercise to explore whether the fitting procedure results in non-negligible estimates for σ_{jit} and for which scenario this potentially occurs.

The data analysis was carried out with commonly used and well-tested tools to perform MC sampling within a GP framework. We used the open source Bayesian inference tool `MultiNestv3.1.0` (e.g. Feroz et al. 2013), through the `pymultinest` wrapper for `python` (Buchner et al. 2014), with 500 live points and a sampling efficiency of 0.8, which is a recommended value for the purpose of parameter estimation. The GP module is the same publicly available `GEORGEv0.2.1` library for `python` we used to generate the data sets.

3.2 Model parameter retrieval

We examined the outcomes of the MC analyses by studying separately the results for each simulated scenario. To assess their quality, we used the quantities defined in Table 3. We adopt the 16th, 50th, and 84th percentiles of their posterior distributions as our statistics.

The results are summarized in Table 4. We remind that, for each simulated scenario, the quantiles are calculated over all the selected mock RV time series, and they represent the average expectations over 50 different realizations of the observing epochs. Hereafter we discuss separately the different scenarios, as well as highlight selected interesting outcomes of our analysis.

Case I. Low-activity star; $P_{\text{orb}} \sim P_{\text{rot}}$. Concerning the planetary term $K_{b, \text{ratio } 50 \text{ per cent}}$, which represents the accuracy on the retrieved value of K_b , it increases by ~ 20 per cent after a second season of observations, but the detection significance $K_{b, 50 \text{ per cent}}/\sigma_{K_b}^-$ remains unchanged and stays below 2σ (therefore implying a non-detection) even with two seasons of data. There is evidence

Table 3. Description of quantities analysed in this work and derived from the MC sampling combined with a GP regression (Section 3.2 and Table 4).

Quantity	Description
h_{ratio}	Ratio between the retrieved amplitude of the activity term and the corresponding injected value for each mock RV data set;
$P_{\text{rot, ratio}}$	Ratio between the retrieved stellar rotation period in the activity term and the corresponding injected value for each mock RV data set;
$\tau_{\text{AR, ratio}}$	Ratio between the retrieved active region evolutionary time-scale and the corresponding injected value for each mock RV data set;
σ_{ratio}	Average of the ratio between the total error budget in the retrieved model and the injected uncertainty (at epoch t) for each mock RV data set (see equation 2);
$K_{b, \text{ratio } 50 \text{ per cent}}$	Ratio between the 50th percentile of the planetary semi-amplitude retrieved from each mock data set (i.e. the best-fitting value obtained for K_b) and the corresponding injected semi-amplitude;
$K_{b, \text{ratio } 68.3 \text{ per cent}}$	Ratio between the 68.3th percentile of the planetary semi-amplitude K_b retrieved from each mock data set and the corresponding injected value;
$K_{b, 50 \text{ per cent}}/\sigma_{K_b}^-$	Ratio between the 50th percentile of the posterior of the planetary semi-amplitude K_b and its lower uncertainty. We assume this parameter to quantify the significance of the retrieved planetary Doppler semi-amplitude with respect to a null value.

for a broadening of its distribution towards higher values for the scenario with long τ_{AR} ($K_{b, 50 \text{ per cent}}/\sigma_{K_b}^- \sim 3$ at $+1\sigma$), for which the length-scale of the stellar activity correlated signal is longer than P_{rot} . Concerning the stellar component, with only one season of data τ_{AR} comes strongly overestimated when $\tau_{\text{AR}} \sim P_{\text{rot}}$. The accuracy improves after two seasons, even though a tail at longer τ_{AR} persists, as can be seen in Fig. 2. A similar tendency is seen when $\tau_{\text{AR}} \gg P_{\text{rot}}$, but the overestimate is smaller and the posterior distributions for τ_{AR} appear more symmetrical. This result can be partially explained taking into account the small amplitude of the stellar component, which makes the signal reconstruction more difficult in presence of activity evolving on short-term time-scales, especially with a scarce number/sampling of data (cf. with *case III*). We show in Section 3.2.2 that a different choice of the prior on τ_{AR} has a positive impact on the accuracy of the retrieved values.

Case II. Low-activity star; $P_{\text{orb}} \neq P_{\text{rot}}$. The main outcome is that, while the detection significance generally stays below 2σ , it increases to $\sim 2\sigma$ for the case $\tau_{\text{AR}} \gg P_{\text{rot}}$ with two seasons of data, with the distribution moving towards higher values (Fig. 3). This result represents a slight improvement with respect the corresponding scenario where $P_{\text{orb}} \sim P_{\text{rot}}$, suggesting that there should be an effect due to how close the stellar rotation and orbital periods are. The distribution of $K_{b, \text{ratio } 50 \text{ per cent}}$ remains unaffected passing from $N_{\text{epochs}, s1}$ to $N_{\text{epochs}, s2}$ observations, and there are no appreciable differences for the stellar component compared to *Case I*, especially for the distributions of τ_{AR} that are similar to those in Fig. 2.

Case III. Active star; $P_{\text{orb}} \sim P_{\text{rot}}$. The semi-amplitude K_b is overestimated by 100 per cent or more when $\tau_{\text{AR}} \sim P_{\text{rot}}$, even with $N_{\text{epochs}, s2}$ data. The overestimate of $K_{b, 50 \text{ per cent}}$ decreases to 20 per cent for the case with $N_{\text{epochs}, s2}$ data and long τ_{AR} , but with a relative uncertainty of ~ 66 per cent. The significance $K_{b, 50 \text{ per cent}}/\sigma_{K_b}^-$, which is ~ 1.5 – 1.6σ in all cases, has narrower distributions for $\tau_{\text{AR}} \sim P_{\text{rot}}$, while for $\tau_{\text{AR}} \gg P_{\text{rot}}$ the distributions

Table 4. Summary of the main results of the analysis performed with MultiNest (Section 3.2). The estimates are given as 16th, 50th, and 84th percentiles of the various distributions we have examined.

Parameter	$P_{\text{rot}} \sim P_{\text{orb}}$		$P_{\text{rot}} \neq P_{\text{orb}}$	
	Short τ_{AR}	Long τ_{AR}	Short τ_{AR}	Long τ_{AR}
One observing season				
Low-activity star				
h_{ratio}	1.0 ± 0.4	1.1 ± 0.5	1.01 ± 0.4	$1.1^{+0.5}_{-0.4}$
$P_{\text{rot, ratio}}$	1.01 ± 0.09	1.00 ± 0.02	1.0 ± 0.09	1.00 ± 0.02
$\tau_{\text{AR, ratio}}$	$10.1^{+15.5}_{-8.7}$	$2.7^{+0.4}_{-0.7} 11$	$9.5^{+16.3}_{-8.1}$	$2.7^{+0.4}_{-0.7}$
σ_{ratio}	$1.2^{+0.3}_{-0.1}$	$1.05^{+0.09}_{-0.02}$	$1.2^{+0.4}_{-0.1}$	$1.06^{+0.1}_{-0.04}$
$K_{\text{b, ratio 50 per cent}}$	$1.2^{+0.9}_{-0.5}$	$1.08^{+0.7}_{-0.5}$	$0.9^{+0.7}_{-0.3}$	$0.8^{+0.5}_{-0.4}$
	$[1.2^{+0.9}_{-0.5}, 886 \text{ samples}]^a$	$[1.6 \pm 0.7, 910 \text{ samples}]^a$		
$K_{\text{b, ratio 68.3 per cent}}$	$1.6^{+0.9}_{-0.6}$	$1.4^{+0.9}_{-0.6}$	$1.2^{+0.7}_{-0.4}$	$1.1^{+0.5}_{-0.4}$
$K_{\text{b, 50\%}/\sigma_{K_{\text{b}}^-}}$	$1.6^{+0.7}_{-0.1}$	$1.6^{+0.6}_{-0.1}$	$1.60^{+0.71}_{-0.09}$	$1.7^{+0.9}_{-0.2}$
	$[1.6^{+0.56}_{-0.09}]^a$	$[1.6^{+0.5}_{-0.1}]^a$		
Active star				
h_{ratio}	1.0 ± 0.2	1.2 ± 0.3	1.0 ± 0.2	1.3 ± 0.3
$P_{\text{rot, ratio}}$	$1.02^{+0.12}_{-0.08}$	1.000 ± 0.004	$1.02^{+0.12}_{-0.08}$	$1.00^{+0.07}_{-0.06}$
$\tau_{\text{AR, ratio}}$	$1.3^{+4.7}_{-0.4}$	$1.3^{+0.8}_{-0.3}$	$1.3^{+7.3}_{-0.4}$	$1.3^{+0.8}_{-0.3}$
σ_{ratio}	$2.2^{+2.0}_{-1.0}$	$1.1^{+0.18}_{-0.05}$	$2.0^{+2.1}_{-0.8}$	$1.11^{+0.18}_{-0.07}$
$K_{\text{b, ratio 50 per cent}}$	$2.14^{+0.5}_{-0.4}$	$1.4^{+0.8}_{-0.7}$	$1.9^{+0.6}_{-0.3}$	$0.9^{+0.6}_{-0.3}$
	$[2.2 \pm 0.4, 1395 \text{ samples}]^a$	$[2.1^{+0.4}_{-0.3}, 1360 \text{ samples}]^a$		
$K_{\text{b, ratio 68.3 per cent}}$	3.0 ± 0.5	$1.8^{+1.2}_{-0.8}$	$2.6^{+0.6}_{-0.5}$	$1.2^{+0.6}_{-0.4}$
$K_{\text{b, 50 per cent}/\sigma_{K_{\text{b}}^-}}$	$1.58^{+0.07}_{-0.05}$	$1.64^{+0.3}_{-0.07}$	$1.6^{+0.08}_{-0.06}$	$1.6^{+0.6}_{-0.1}$
	$[1.58^{+0.07}_{-0.05}]^a$	$[1.54^{+0.11}_{-0.06}]^a$		
Two observing seasons				
Low activity star				
h_{ratio}	$1.0^{+0.2}_{-0.3}$	$1.1^{+0.4}_{-0.3}$	$1.0^{+0.2}_{-0.3}$	1.1 ± 0.3
$P_{\text{rot, ratio}}$	1.00 ± 0.07	1.00 ± 0.01	$1.00^{+0.09}_{-0.08}$	1.00 ± 0.01
$\tau_{\text{AR, ratio}}$	$1.5^{+10.2}_{-0.5}$	$1.8^{+1.2}_{-0.2}$	$1.5^{+8.1}_{-0.5}$	$1.7^{+1.2}_{-0.7}$
σ_{ratio}	$1.07^{+0.24}_{-0.04}$	$1.03^{+0.05}_{-0.02}$	$1.05^{+0.12}_{-0.04}$	$1.04^{+0.08}_{-0.02}$
$K_{\text{b, ratio 50 per cent}}$	$1.0^{+0.7}_{-0.4}$	$0.9^{+0.6}_{-0.4}$	$0.8^{+0.6}_{-0.3}$	$0.8^{+0.5}_{-0.4}$
	$[1.1^{+0.7}_{-0.4}, 955 \text{ samples}]^a$	$[1.4^{+0.8}_{-0.5}, 917 \text{ samples}]^a$		
$K_{\text{b, ratio 68.3 per cent}}$	$1.3^{+0.7}_{-0.5}$	$1.2^{+0.7}_{-0.5}$	$1.0^{+0.6}_{-0.3}$	1.0 ± 0.4
$K_{\text{b, 50 per cent}/\sigma_{K_{\text{b}}^-}}$	$1.6^{+0.8}_{-0.1}$	$1.7^{+1.2}_{-0.2}$	$1.6^{+0.9}_{-0.1}$	$1.9^{+1.5}_{-0.4}$
	$[1.6^{+0.6}_{-0.1}]^a$	$[1.6^{+0.7}_{-0.1}]^a$		
Active star				
h_{ratio}	0.9 ± 0.1	1.1 ± 0.2	1.0 ± 0.1	1.1 ± 0.2
$P_{\text{rot, ratio}}$	$1.00^{+0.05}_{-0.04}$	1.000 ± 0.002	$1.00^{+0.05}_{-0.04}$	0.999 ± 0.002
$\tau_{\text{AR, ratio}}$	$1.1^{+0.3}_{-0.2}$	1.1 ± 0.2	$1.1^{+0.4}_{-0.2}$	1.1 ± 0.2
σ_{ratio}	$1.7^{+1.7}_{-0.5}$	$1.03^{+0.04}_{-0.02}$	$1.4^{+1.6}_{-0.2}$	$1.07^{+0.12}_{-0.04}$
$K_{\text{b, ratio 50 per cent}}$	$1.9^{+0.5}_{-0.4}$	$1.2^{+0.8}_{-0.7}$	$1.5^{+0.7}_{-0.4}$	$0.8^{+0.5}_{-0.3}$
	$[2.0^{+0.4}_{-0.3}, 1374 \text{ samples}]^a$	$[1.9 \pm 0.3, 1368 \text{ samples}]^a$		
$K_{\text{b, ratio 68.3 per cent}}$	2.7 ± 0.5	$1.6^{+1.2}_{-0.8}$	$2.1^{+0.8}_{-0.5}$	$1.0^{+0.5}_{-0.4}$
$K_{\text{b, 50 per cent}/\sigma_{K_{\text{b}}^-}}$	$1.5^{+0.06}_{-0.05}$	$1.5^{+0.5}_{-0.08}$	$1.54^{+0.10}_{-0.05}$	$1.7^{+1.1}_{-0.2}$
	$[1.54^{+0.06}_{-0.04}]^a$	$[1.50^{+0.08}_{-0.06}]^a$		

^aDerived from posteriors related to simulated data sets that satisfy the condition $|P_{\text{rot}} - P_{\text{orb}}| \leq 0.5$ d.

shift towards higher values, i.e. towards slightly more significant detections. Concerning the stellar component, the hyperparameter τ_{AR} is well recovered after two observing seasons (indicating that an uninformative prior performs well in these cases), while with one season of data and for $\tau_{\text{AR}} \sim P_{\text{rot}}$ the distribution of τ_{AR} is skewed towards values larger than unity, but to a less extent than for quiet stars, confirming that the level of activity determines how accurately τ_{AR} is fitted (as discussed for *Case I*).

Case IV. Active star; $P_{\text{orb}} \neq P_{\text{rot}}$. While K_{b} is overestimated by 100 per cent with only one season of data and for $\tau_{\text{AR}} \sim P_{\text{rot}}$, it

becomes more accurate for stationary stellar activity ($\tau_{\text{AR}} \gg P_{\text{rot}}$). The overestimate observed for short τ_{AR} reduces to 50 per cent by doubling the number of RVs. The detection significance stays below 2σ , but it begins to increase sensibly for stars with $\tau_{\text{AR}} \gg P_{\text{rot}}$ and $N_{\text{epochs, s2}}$ observations, similarly to what is observed for low-activity stars. As for *Case III*, the hyperparameter τ_{AR} is well recovered after two observing seasons.

Upper limits as defined by the 68th percentile. Due to the small amplitude of the planetary signal injected in the simulated data sets, the posterior distributions of K_{b} for each single RV data set tend to

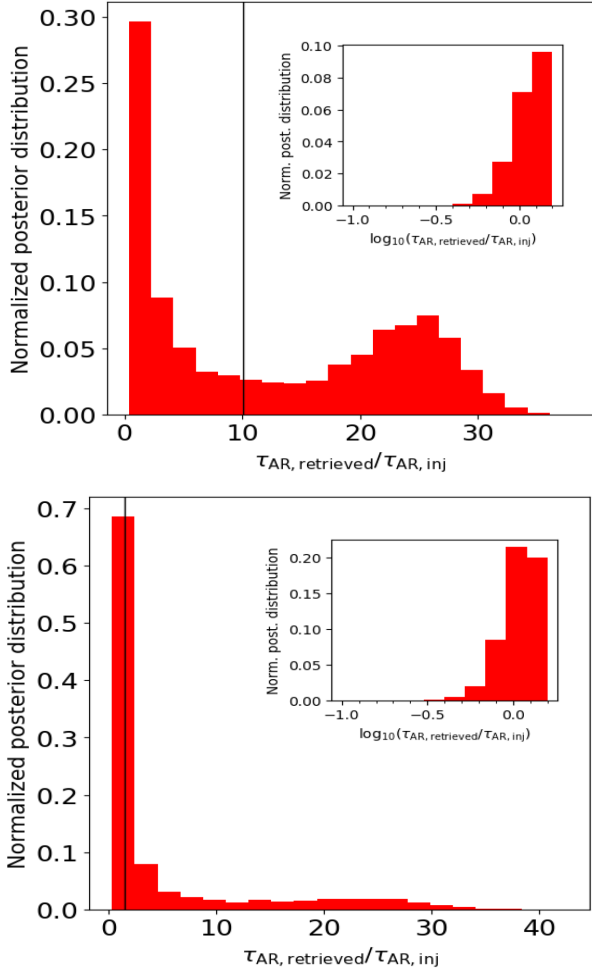


Figure 2. Posterior distributions for $\tau_{\text{AR, ratio}} = \frac{\tau_{\text{AR, retrieved}}}{\tau_{\text{AR, injected}}}$ for the scenario represented by a star with low and quickly variable activity (short τ_{AR}) hosting a planet with $P_{\text{orb}} \sim P_{\text{rot}}$. The upper and lower panels show the results for one and two seasons of data, respectively. The vertical lines indicate the median of each distribution. The inset plots are a zoomed in view around $\tau_{\text{AR, ratio}} = 1$ in logscale, showing that there are very few cases where τ_{AR} is underestimated. Similar results were obtained for the case $P_{\text{orb}} \neq P_{\text{rot}}$.

peak typically to very low values close to 0 m s^{-1} . When working with real planetary systems, in such cases the 68.3th percentile is commonly used to provide an upper limit for K_b instead of considering the median of the posterior distribution. Therefore, for each scenario we analysed the distributions $K_{b, \text{ratio } 68.3}$ per cent of the ratio between the 68.3th percentile of the K_b posterior and the injected semi-amplitude, for each data set. From Table 4 we note that the 68.3th percentile appears as a more accurate estimate for K_b than the 50th percentile for low-active stars when $P_{\text{orb}} \neq P_{\text{rot}}$ and with $N_{\text{epochs, s2}}$ observations. All things being equal, the same conclusion is also valid for active stars but only for the cases with long evolutionary time scales τ_{AR} .

The role of the uncorrelated jitter. One issue often debated when fitting RV time series is how the results for the uncorrelated jitter σ_{jit} should be interpreted. As mentioned in Section 3.1, we did not include any uncorrelated noise term when building the simulated RV data sets, but we use it as a free parameter σ_{jit} in the fitting analysis. To quantify the relevance of the uncorrelated jitter in determining

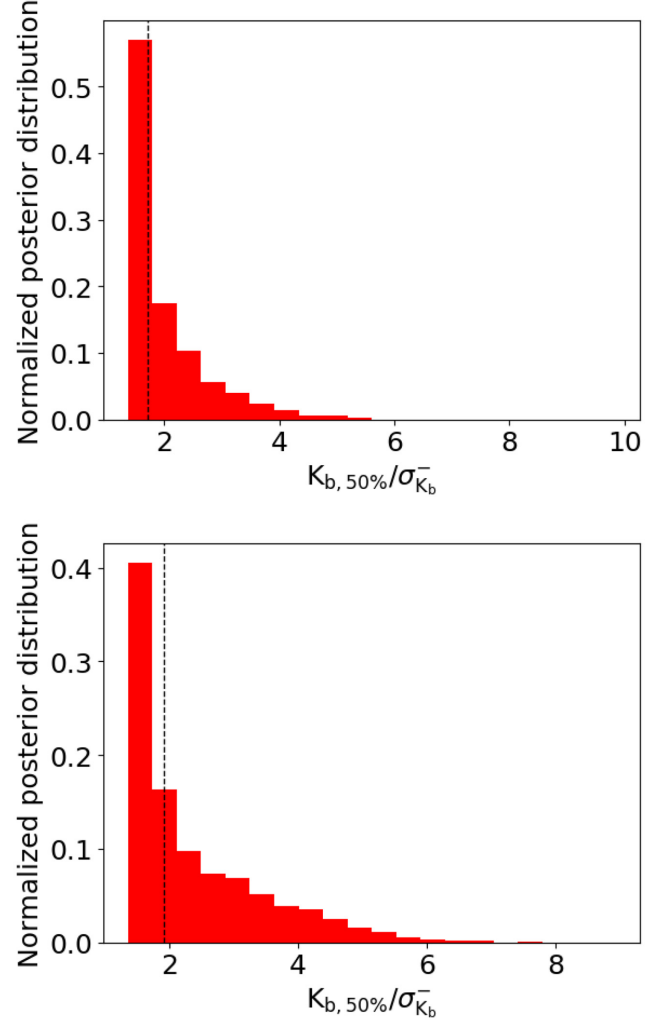


Figure 3. Posterior distributions for the planet detection significance $K_b, 50 \text{ per cent} / \sigma_{K_b}$ concerning the scenario represented by a star with low and slowly variable activity (long τ_{AR}) hosting a planet with $P_{\text{orb}} \neq P_{\text{rot}}$. The upper plot shows the result for one season of data, and the lower plot that for two seasons of observations. The vertical lines indicate the median of each distribution.

our results, we define the ratio:

$$\sigma_{\text{ratio}} = \left\langle \frac{\sqrt{\sigma_{\text{RV}}^2(t) + \sigma_{\text{jit}}^2}}{\sigma_{\text{RV}}(t)} \right\rangle \quad (2)$$

for each mock data set and consider the posterior distribution of this quantity for each simulated scenario (Table 4). For a low-activity star σ_{ratio} is very close to one, especially for the case with longer τ_{AR} , pointing out that the fitted σ_{jit} is negligible, in agreement with the injected $\sigma_{\text{jit}} = 0$. This effect is even more evident after two observing seasons. Even though the activity term is not well fitted for the cases with short τ_{AR} , the amplitude of the stellar signal is comparable to the average uncertainty of the RVs, implying that an additional uncorrelated noise is not required to improve the fit, which is likely limited by the sampling.

For stars with high activity and short τ_{AR} , with $N_{\text{epochs, s1}}$ data the fitted σ_{jit} determines a total error budget which is on average typically twice the uncertainty, increasing nearly up to four times $\sigma_{\text{RV}}(t)$ at 1σ level. For the sample with long τ_{AR} the distribution of

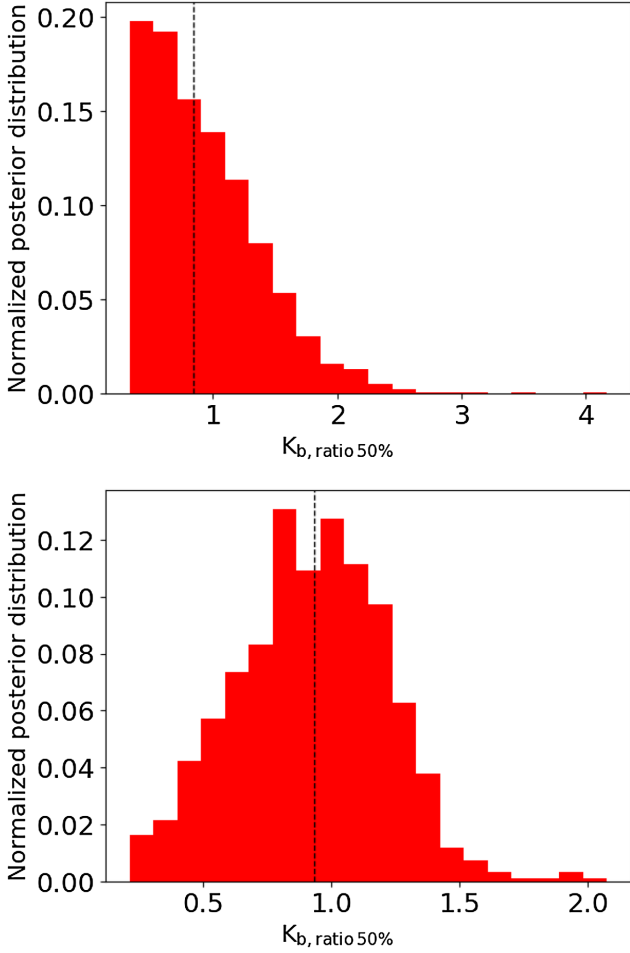


Figure 4. Distributions of the posterior $K_{b, \text{ratio } 50 \text{ per cent}} = \frac{K_{b, \text{retrieved}}}{K_{b, \text{injected}}}$ for the scenario represented by a star with low and stable activity (long τ_{AR}) hosting a planet with $P_{\text{orb}} \neq P_{\text{rot}}$. The results refer to the case of data sets composed by one semester of observations. The injected planetary signals have $K_{b, \text{inj}} = 1 \text{ m s}^{-1}$ (upper plot), and $K_{b, \text{inj}} = 2 \text{ m s}^{-1}$ (lower plot). The vertical lines indicate the median of each distribution.

σ_{ratio} is much closer to one. Besides the effects of a larger amplitude of the stellar activity term, this result reveals that there is also a dependence of the fitted σ_{jit} from τ_{AR} . In fact, with only one season of data τ_{AR} is poorly fitted, especially for the cases with short τ_{AR} , and this corresponds to the highest values for σ_{ratio} (with some influence due to the choice of the prior for τ_{AR}). The highest σ_{jit} correspond to the cases where $P_{\text{rot, ratio}}$ is retrieved with less precision. These results point out that a higher uncorrelated jitter occurs in presence of a large stellar activity signal, in particular that higher uncorrelated jitter values can be expected for active stars with activity changing over short time-scales.

3.2.1 SELECTED SCENARIOS WITH INJECTED $K_B > 1 \text{ MS}^{-1}$

Using a lower number of mock data sets, we conducted an exploratory analysis on some selected scenarios, limited to $N_{\text{epochs, s1}}$ data, to see how the results change by injecting planetary signals with semi-amplitudes greater than 1 m s^{-1} . We have simulated 1000 mock RV data sets, corresponding to 10 groups with different time sampling realizations, each composed of 100 RV time series.

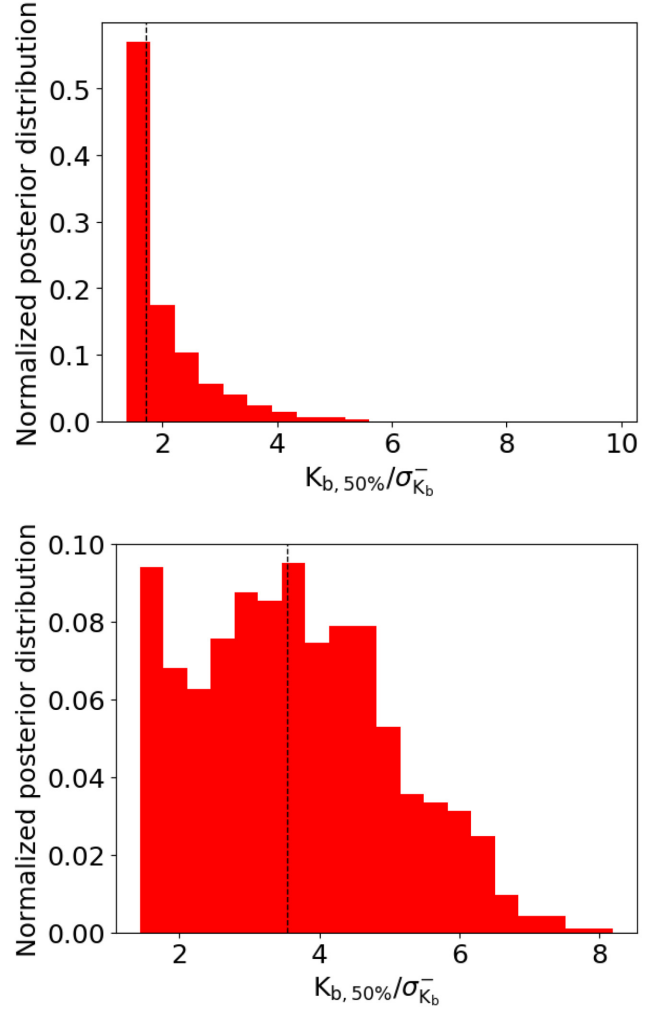


Figure 5. Posterior distributions of the quantity $K_{b, 50 \text{ per cent}} / \sigma_{K_b}$ for the scenario represented by a star with low and stable activity (long τ_{AR}) hosting a planet with $P_{\text{orb}} \neq P_{\text{rot}}$. The results refer to the case of data sets composed by one semester of observations. The injected planetary signals have $K_{b, \text{inj}} = 1 \text{ m s}^{-1}$ (upper plot), and $K_{b, \text{inj}} = 2 \text{ m s}^{-1}$ (lower plot). The vertical lines indicate the median of each distribution.

We first consider the likely best-case scenario for detecting the planetary signal, represented by a star with low and stable activity (long τ_{AR}) hosting a planet with $P_{\text{orb}} \neq P_{\text{rot}}$, by injecting a Keplerian with $K_b = 2 \text{ m s}^{-1}$. In this case we get $K_{b, \text{ratio } 50 \text{ per cent}} = 0.9 \pm 0.3$ (68.3th percentile = 1.04) and $K_{b, 50 \text{ per cent}} / \sigma_{K_b} = 3.5 \pm 1.5$. Compared with the same scenario where $K_{b, \text{inj}} = 1 \text{ m s}^{-1}$, the posterior distribution for $K_{b, \text{ratio } 50 \text{ per cent}}$ appears nearly symmetrical around 0.9–1 m s^{-1} , while for $K_{b, \text{inj}} = 1 \text{ m s}^{-1}$ the distribution is asymmetric, with the peak shifted towards $\sim 0.5 \text{ m s}^{-1}$ (Fig. 4). The typical significance of the detection is twice than for the case with $K_{b, \text{inj}} = 1 \text{ m s}^{-1}$, with a relative uncertainty of $\sim 50 \text{ per cent}$ (Fig. 5).

For the likely worst-case scenario, represented by an active star with rapidly variable activity (short τ_{AR}) hosting a planet with $P_{\text{orb}} \sim P_{\text{rot}}$, we injected a signal with $K_b = 3 \text{ m s}^{-1}$, and retrieved $K_{b, \text{ratio } 50 \text{ per cent}} = 0.7^{+0.2}_{-0.1}$ (68.3th percentile = 1.01) and $K_{b, 50 \text{ per cent}} / \sigma_{K_b} = 1.57^{+0.09}_{-0.05}$. While the significance of the detection does not change with respect to the case $K_b = 1 \text{ m s}^{-1}$, the distribution for $K_{b, \text{ratio } 50 \text{ per cent}}$ is symmetrical with a median below 1, pointing out that, even though the semi-amplitude is

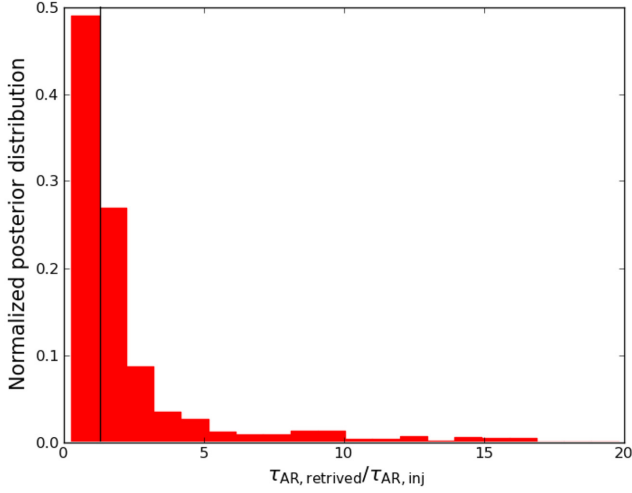


Figure 6. Posterior distribution of the $\tau_{\text{AR, ratio}} = \frac{\tau_{\text{AR, retrieved}}}{\tau_{\text{AR, injected}}}$ for the scenario represented by stars with low and quickly variable activity (short τ_{AR}), hosting a planet with $P_{\text{orb}} \sim P_{\text{rot}}$, and with $N_{\text{epochs, s1}}$ data. The vertical lines indicate the median of the distribution. Here we show the result for the alternative priors on τ_{AR} and P_{rot} (Section 3.2.2), which has to be compared with the upper plot in Fig. 2.

on average underestimated by 30 per cent, it is closer to the true value.

Finally, we explored the case of a quiet star with short τ_{AR} hosting a planet with $P_{\text{orb}} \sim P_{\text{rot}}$ and $K_b = 2 \text{ m s}^{-1}$. We get $K_{b, \text{ratio}} 50 \text{ per cent} = 0.9^{+0.5}_{-0.4}$ (68.3th percentile = 1.09) and $K_{b, 50 \text{ per cent}}/\sigma_{K_b}^- = 1.9^{+1.4}_{-0.3}$. These results indicate that the planet is retrieved with higher precision and increasing significance with respect to the case where $K_b = 1 \text{ m s}^{-1}$.

An interesting result, common to all the three cases analysed here, is that the 68.3th percentile is substantially equal to the injected K_b . Looking at Table 4, when $K_b = 1 \text{ m s}^{-1}$ the same situation happens only for the scenarios (i) low-activity stars and decoupled periodicities, with K_b (68.3th percentile) equal exactly to 1 m s^{-1} with $N_{\text{epochs, s2}}$ data, independently from the value of τ_{AR} ; and (ii) active stars, $P_{\text{orb}} \neq P_{\text{rot}}$, long τ_{AR} , and $N_{\text{epochs, s2}}$ data.

3.2.2 DEPENDENCE OF THE RESULTS ON THE CHOICE OF THE PRIORS

In our simulations the only parameter we explored over a significantly large scale is τ_{AR} , which we have assumed to be unconstrained from possible ancillary data. As previously discussed (Section 3.2, *case D*), the hyperparameter τ_{AR} is poorly fitted for the case of low-activity stars and $\tau_{\text{AR}} \sim P_{\text{orb}}$, especially with $N_{\text{epochs, s1}}$ data, since the distribution of $\tau_{\text{AR, ratio}}$ is bi-modal, as shown in Fig. 2 (the bi-modality being much less pronounced with $N_{\text{epochs, s2}}$ data). In principle this fact may impact the accuracy and precision of the retrieved planetary signal. Since by adopting that prior we are assuming to be ignorant about the order of magnitude (or scale) of τ_{AR} , a potentially better choice for the prior is adopting an uninformative distribution on $\ln(\tau_{\text{AR}})$ within the range [0,6.9] corresponding to the interval [1,1000] d of the linear scale. To investigate the effects of changing the prior, we first analysed with the logarithmic prior 1000 mock data sets with $N_{\text{epochs, s1}}$ RV measurements concerning the scenario of low-activity stars, short

τ_{AR} , and $P_{\text{orb}} \neq P_{\text{rot}}$. Moreover, we restricted the range of the prior on P_{orb} to $\pm 0.05 \text{ d}$ to simulate the case of better known transit ephemeris. From the new analysis we find that $\tau_{\text{AR, ratio}} = 1.3^{+1.7}_{-0.6}$, which represents a significant improvement of the MC fitting analysis for the stellar component (Fig. 6). However, for $K_{b, \text{ratio}} 50 \text{ per cent}$ and $K_{b, 50 \text{ per cent}}/\sigma_{K_b}^-$ we do not find any difference with respect to the original set of priors. This shows that in our case a more correct fitting of the stellar signal does not improve the determination of the planetary parameters. We get similar results when analysing data sets with $N_{\text{epochs, s2}}$ RVs, finding $\tau_{\text{AR, ratio}} = 1.1^{+0.7}_{-0.4}$, i.e. the stellar activity signal is better represented, but this does not come with a better statistical result for the planetary component.

Using the same set of new priors, we also considered the case with long τ_{AR} . We get $\tau_{\text{AR, ratio}} = 1.3^{+0.7}_{-0.8}$, which is an improvement in the ability of retrieving the injected τ_{AR} since the median of $\tau_{\text{AR, ratio}}$ is half that found using the original prior. However, even in this case there is no improvement for the parameters $K_{b, \text{ratio}} 50 \text{ per cent}$ and $K_{b, 50 \text{ per cent}}/\sigma_{K_b}^-$.

Finally, as an additional check we considered the case of low-activity stars, short τ_{AR} , and $P_{\text{orb}} \sim P_{\text{rot}}$, in particular to test the effects of the tighter prior on P_{orb} . As expected, we found a significant improvement in fitting the hyperparameter τ_{AR} , getting $\tau_{\text{AR, ratio}} = 1.3^{+2.4}_{-0.6}$. For $K_{b, \text{ratio}} 50 \text{ per cent}$ and $K_{b, 50 \text{ per cent}}/\sigma_{K_b}^-$ we do not find any improvement with respect to the values tabulated in Table 4.

In conclusion, we find that using a uniform logarithmic prior on τ_{AR} provides more realistic representations for the quasi-periodic stellar activity signal than adopting a uniform linear prior, but more accurate values for τ_{AR} does not correspond to more accurate retrieved planetary signals, even restricting the prior on P_{orb} .

3.2.3 EXPLORING THE EFFECTS OF ORBITAL PERIODS VERY CLOSE TO STELLAR ROTATION PERIODS

Here we focus on the scenarios for which $P_{\text{orb}} \sim P_{\text{rot}}$ and consider only the data sets for which the injected values satisfy the condition $|P_{\text{orb}} - P_{\text{rot}}| \leq 0.5 \text{ d}$. We choose the range of $\pm 0.5 \text{ d}$ because this is the interval we have adopted to define the prior for P_{orb} (Table 2). In this case, values for P_{orb} are sampled within a parameter space which includes P_{rot} . We are interested in the analysis of those subsets to assess possible effects on the retrieved planetary signals due to the very close proximity between the orbital and stellar rotations periods. We note that the range of 0.5 d is 3–4 times smaller than 1σ associated with the $P_{\text{orb}} - P_{\text{rot}}$ input distributions for these scenarios (Table A1). Results are shown in Table 4 between square brackets. Typically, they are derived from $\sim 20 \text{ per cent}$ of the total samples, a number which allows a good statistics. The only difference we note with respect to the results for the total sample is that $K_{b, \text{ratio}} 50 \text{ per cent}$ shifts to higher values by an amount of $\sim 50 \text{ per cent}$ for the case $\tau_{\text{AR}} \gg P_{\text{rot}}$, both for low- and high-activity stars and independently from the number of observations. This indicates that the fitting procedure tends to absorb part of the stellar signal in the planetary component of the model and, not surprisingly, this happens for stars with the longer evolutionary time-scale τ_{AR} , in that the stellar term has properties closer to those of a circular Keplerian. The result suggests that alternative recipes to model the stellar activity term should be considered in addition to GP regression when P_{orb} and P_{rot} are very close.

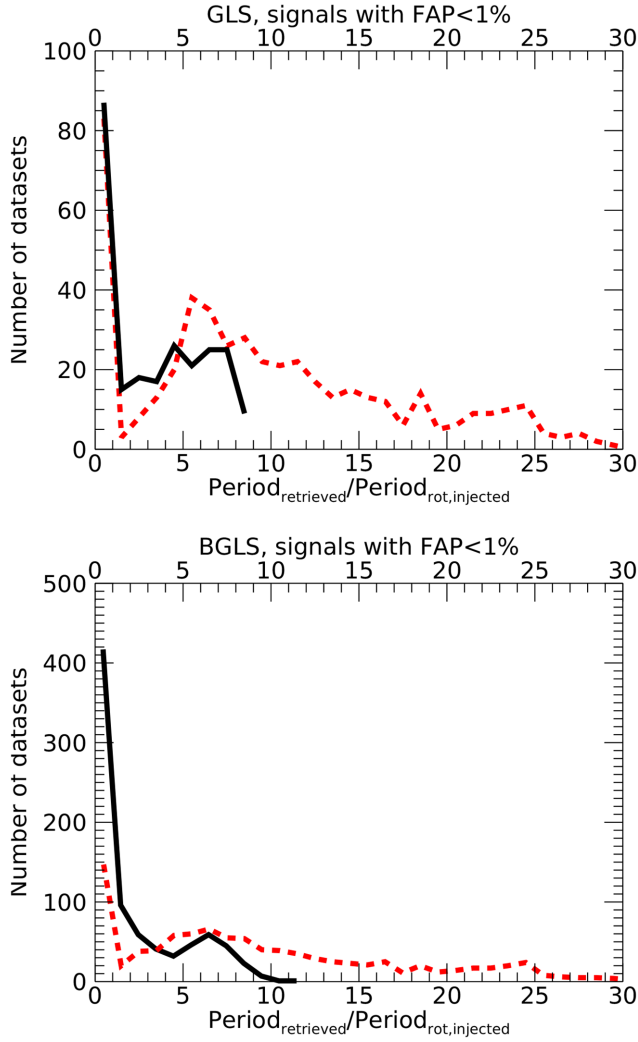


Figure 7. Distributions of the retrieved/simulated period ratios (the injected periods correspond to P_{rot}) for the cases of active stars, $P_{\text{rot}} \neq P_{\text{orb}}$, short τ_{AR} , $N_{\text{epochs}, s1}$ (solid black line), and $N_{\text{epochs}, s2}$ (dashed red line) data. Here we show the results for GLS and BGLS algorithms.

3.2.4 EFFECTS OF NEGLECTING TO MODEL THE STELLAR ACTIVITY WITH A GP REGRESSION

Here we consider the case where the stellar activity is fitted by including only the uncorrelated jitter term in the global model, to explore the effects of using a simpler model than the GP regression, as is often done when dealing with real systems. We focus the attention to the scenario corresponding to a quiet star with $P_{\text{rot}} \neq P_{\text{orb}}$, since fitting the activity with a correlated-noise model (like the GP regression) is expected to be more convenient and effective a priori for active stars. We analysed a subset of $N = 500$ RV data sets for each scenario with $K_{b, \text{inj}} = 1 \text{ m s}^{-1}$ (short and long τ_{AR} ; $N_{\text{epochs}, s1}$ and $N_{\text{epochs}, s2}$ RV measurements), and compared the Bayesian evidences of the models with and without the GP term. Table 5 shows the results for the difference of the logarithm of the Bayesian evidences for the two models, $\Delta \ln \mathcal{Z} = \ln \mathcal{Z}_{\text{GP}+1 \text{ planet}} - \ln \mathcal{Z}_{1 \text{ planet}}$, and lists the values of $K_{b, \text{ratio 50 per cent}}$ and $K_{b, 50 \text{ per cent}} / \sigma_{K_b}^-$ derived from using the model without GP and uncorrelated jitter only. We assume that $\Delta \ln \mathcal{Z} \geq 5$ denotes strong evidence in favour of the GP + 1 planet model (see e.g. table 1

Table 5. Model comparison analysis, with or without a GP quasi-periodic kernel included in the global model. Here we consider the case of quiet stars with $P_{\text{rot}} \neq P_{\text{orb}}$. The values of $K_{b, \text{ratio 50 per cent}}$ and $K_{b, 50 \text{ per cent}} / \sigma_{K_b}^-$ are derived from fitting the model without using GP. $\sigma_{\text{jit, no GP}} / \sigma_{\text{jit, with GP}}$ is the ratio between the values of the fitted uncorrelated jitter without and with the GP term included in the model. $\Delta \ln \mathcal{Z} = \ln \mathcal{Z}_{\text{GP}+1 \text{ planet}} - \ln \mathcal{Z}_{1 \text{ planet}}$.

One season of observations		
	Short τ_{AR}	Long τ_{AR}
$K_{b, \text{ratio 50 per cent}}$	$0.95^{+0.87}_{-0.35}$	$0.98^{+0.68}_{-0.41}$
$K_{b, 50 \text{ per cent}} / \sigma_{K_b}^-$	$1.6^{+0.6}_{-0.1}$	$1.6^{+0.5}_{-0.1}$
median $\sigma_{\text{jit, no GP}} / \sigma_{\text{jit, with GP}}$	2.3	3.6
median $\Delta \ln \mathcal{Z}$	2.2	5.2
number of data sets for which $\Delta \ln \mathcal{Z} > 5$	28 per cent	51 per cent
median $\sigma_{\text{jit, no GP}} / \sigma_{\text{jit, with GP}}$	2.3	3.6
Two seasons of observations		
	Short τ_{AR}	Long τ_{AR}
$K_{b, \text{ratio 50 per cent}}$	$0.86^{+0.58}_{-0.35}$	$0.74^{+0.53}_{-0.26}$
$K_{b, 50 \text{ per cent}} / \sigma_{K_b}^-$	$1.6^{+0.7}_{-0.1}$	$1.6^{+0.5}_{-0.08}$
median $\sigma_{\text{jit, no GP}} / \sigma_{\text{jit, with GP}}$	3.6	4.9
median $\Delta \ln \mathcal{Z}$	6.7	20.9
number of data sets for which $\Delta \ln \mathcal{Z} > 5$	57 per cent	85 per cent
median $\sigma_{\text{jit, no GP}} / \sigma_{\text{jit, with GP}}$	3.6	4.9

in Feroz, Balan & Hobson 2011). With $N = 40$ measurements the use of the GP regression can be considered generally unnecessary for short values of τ_{AR} , since only ~ 30 per cent of the samples are better fitted by a GP + 1 planet model. With $N = 80$ measurements the GP + 1 planet model provides a better fit in ~ 60 per cent of the cases. However, comparing with Table 4, we see that $K_{b, \text{ratio 50 per cent}}$ and $K_{b, 50 \text{ per cent}} / \sigma_{K_b}^-$ are in agreement with those obtained fitting a GP + 1 planet model. For the case of long τ_{AR} , the evidence is by far in favour of the GP + 1 planet model, in particular with $N = 80$ measurements, as also confirmed by the fact that a σ_{jit} five times larger is required if a GP term is not included in the model. This is expected, since the activity term is more stable over time and easier to characterize. None the less, within the framework of our simulations, even in this case the use of the GP regression does not bring better results than a simpler model in terms of planetary semi-amplitude.

4 PERIODOGRAM ANALYSIS

Here we present the results of a blind statistical analysis performed on a large sub-sample of the simulated data sets, using different periodogram algorithms commonly used to investigate the frequency content of RV time series. The goal of this section is to examine and characterize some statistical properties, described in Table 6, of periodograms for RV data sets containing quasi-periodic stellar activity signals.

As done by Pinamonti et al. (2017), the data sets were analysed with softwares that calculate the frequency content in time series: the Generalized Lomb–Scargle periodograms (GLS; Zechmeister & Kürster 2009); the Bayesian Generalized Lomb–Scargle (BGLS; Mortier et al. 2015); and the FREquency DEComposer (FREDEC; Baluev 2013). GLS performs a simple sinusoidal fit of the data, weighting them on the measurements errors. BGLS generalizes this approach taking into account Bayesian probability. FREDEC performs a multifrequency analysis of the data, decomposing a

Table 6. Description of quantities analysed in this work to characterize the performances of the GLS, BGLS, and FREDEC algorithms to search for periodic signals in the mock RV data sets (Section 4, Tables 7 and 8).

Quantity	Description
$N_{\text{FAP} < 1 \text{ per cent}}, N_{\text{FAP} 1-10 \text{ per cent}}$	Number of solutions detected with $\text{FAP} < 1 \text{ per cent}$ and $1 \text{ per cent} < \text{FAP} < 10 \text{ per cent}$, respectively, relative to a total of 1000 examined periodograms.
$C_{P_{\text{rot}}} \equiv \text{completeness } P_{\text{rot}} \text{ (per cent)}$	Ratio between the number of data sets with the highest peak in the periodograms (i) with $\text{FAP} < 1 \text{ per cent}$, and (ii) within $\pm 10 \text{ per cent}$ of the injected P_{rot} , and the total number of the analysed data sets. The same quantity is calculated for the first harmonic $P_{\text{rot}}/2$.
$C_{P_{\text{orb}}} \equiv \text{completeness } P_{\text{orb}} \text{ (per cent)}$	Same as for $C_{P_{\text{rot}}}$, but for the injected orbital period P_{orb} .
$R \equiv \text{reliability (per cent)}$	Ratio between the number of data sets with the highest peak in the periodograms (i) with $\text{FAP} < 1 \text{ per cent}$, and (ii) within $\pm 10 \text{ per cent}$ of the injected P_{rot} , and the number of analysed data sets with highest peaks in the periodograms having $\text{FAP} < 1 \text{ per cent}$. We calculated the same ratio for the first harmonic of the stellar rotation period $P_{\text{rot}}/2$ (indicated between brackets in Tables 7 and 8).

time series into a number of sinusoids. The algorithm first selects candidate frequencies, then computes the statistical significance for each frequency tuple, providing as solution the most significant multifrequency combination. We refer the reader to the indicated references for more details about each algorithm.

Contrary to the analysis described in Section 3.2, here we assume that nothing is known a priori about the signal content in the RV time series. This part of the work should be considered an extension of the comparative analysis discussed in Pinamonti et al. (2017), in that here we analysed more thoroughly the performances of the algorithms on data sets containing a realistic description of stellar activity RV signals. To assess the detectability of the simulated planetary signals, we can adopt the K/N ratio, defined as in Dumusque et al. (2017)

$$K/N = \frac{K_b}{\text{RV}_{\text{rms}}} \times \sqrt{N_{\text{obs}}}, \quad (3)$$

where $N_{\text{obs}} = 40, 80$ are the number of observations for the one and two seasons cases, respectively. We see from Table A1 that K/N is generally well below the $K/N = 7.5$ threshold proposed by Dumusque et al. (2017), making planet detection a very challenging task.

The GLS periodograms are computed using the code implementation in the `ASTROPY2.0.2` library for `PYTHON3.5`. The false alarm probabilities (FAP), or p -values, are computed with a bootstrap with replacement analysis using 10 000 RV mock data sets. The BGLS periodograms have been calculated with an IDL version of the publicly available `PYTHON` code,⁷ developed for the analysis discussed in Pinamonti et al. (2017). The FAPs for the Bayesian periodograms are computed as described in Pinamonti et al. (2017). The analysis with FREDEC has been carried out with the publicly available C++ version of the code.⁸ The FAPs associated with the output frequency tuples are computed with the built-in function of the code.

We computed periodograms for subsets composed of 1000 mock RV data sets, one for each of the 16 different simulated scenarios described in Section 2. To ease the automatic identification of the main periodicities in the time series, we calculated the periodograms exploring periods longer than 5 d. This cut helps avoiding the daily aliases in the spectral window, which would be discarded in a real single-target analysis. Moreover, this threshold should not affect the retrieval of the injected signals, since no values of $P_{\text{rot}} \leq 5 \text{ d}$ or $P_{\text{orb}} \leq 5 \text{ d}$ have been simulated. For the sake of robustness of period

detection, we set the upper limit of the period search interval to half the time span of the data, in order to ensure at least two full cycles for every test frequency.

We defined the parameters described in Table 6 as figure of merit for assessing the performances of the algorithms. In the case of FREDEC, we considered for the purpose of computing the completeness C and reliability R all the significant solution tuples with at least one of the output periods within 10 per cent of the input period, even in the presence of additional output periodicities. In the following, we present some major outcomes of the analysis, selected from the complete list of results shown in Tables 7 and 8. First, we organize the discussion into subgroups according to the different simulated scenarios (e.g. different stellar activity levels), then focusing on the comparison among the algorithms. This way of presenting should allow for an easier identification, and therefore better exploitation of the results.

We note that for all the cases with $P_{\text{rot}} \sim P_{\text{orb}}$ we do not report the completeness $C_{P_{\text{orb}}}$ for the orbital period. In fact, we do not consider this as an informative quantity for our purposes, since the input periods P_{rot} and P_{orb} used to build the data sets are too close to be disentangled by a periodogram analysis.

4.1 Dependence of the algorithm performances from the stellar activity properties

Case I. Low-activity stars. In general, the reliability R decreases (or does not improve) passing from $N_{\text{epochs}, s1}$ to $N_{\text{epochs}, s2}$ data, independently from the values of τ_{AR} , except for BGLS (cases with long τ_{AR}). Instead the fraction of significant signals $N_{\text{FAP} < 1 \text{ per cent}}$ increases considerably with two semesters of measurements, and this implies that the algorithms find a larger number of false positives when more RVs are available. In general, the completeness for P_{orb} ($C_{P_{\text{orb}}}$) and the reliability are higher for the cases with long τ_{AR} , both for $P_{\text{rot}} \sim P_{\text{orb}}$ and $P_{\text{rot}} \neq P_{\text{orb}}$. This is not surprising, in that a quasi-periodic activity signal with long τ_{AR} is expected to approach a periodic signal over the time span considered here, therefore a sinusoid (or a combination of sinusoids) can fit the data more efficiently.

Case II. Active stars. As for *case I*, we note that in general the performances, in terms of completeness and reliability, are higher when τ_{AR} is longer (see Fig. 7 showing retrieved/injected ratio distributions for cases with short τ_{AR}). In absolute terms, this behaviour is more clear than for low-activity stars with $N_{\text{epochs}, s1}$ data, where R is high and close to 100 per cent for GLS and FREDEC and $> 90 \text{ per cent}$ for GLS, including the term for the first harmonic of P_{rot} the calculation. This is not surprising, since the

⁷<https://www.astro.up.pt/exoearth/tools.html>

⁸<https://sourceforge.net/projects/fredec/>

Table 7. Summary of the main results of the analysis performed on the periodograms calculated with GLS, BGLS, and FREDEC (Section 4) for the cases where $P_{\text{rot}} \sim P_{\text{orb}}$. The statistics concerns the peaks detected with an FAP < 1 per cent. The results are given as 16th, 50th, and 84th percentiles of the parameter distributions.

		$P_{\text{rot}} \sim P_{\text{orb}}$					
Parameter		GLS ^a	Short τ_{AR} BGLS ^a	FREDEC ^b	GLS ^a	Long τ_{AR} BGLS ^a	FREDEC ^b
One observing season							
Low-activity star	$N_{\text{FAP} < 1 \text{ per cent}}$	24.0 per cent	7.1 per cent	27.1 per cent	50.5 per cent	9.0 per cent	47.1 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	33.1 per cent	17.7 per cent	23.0 per cent	21.2 per cent	16.6 per cent	18.0 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}/2}})^c$ (per cent)	12.4 (1.0)	2.0 (1.6)	12.8 (1.3)	42.5 (6.1)	4.1 (3.1)	40.4 (4.1)
	$R (+P_{\text{rot}/2})^c$ (per cent)	51.5 (+ 4.0)	28.4 (+ 22.4)	54.6 (+ 4.4)	84.1 (+ 12.1)	45.9 (+ 35.3)	88.1 (+ 8.7)
Active star	$N_{\text{FAP} < 1 \text{ per cent}}$	23.0 per cent	83.2 per cent	27.9 per cent	72.8 per cent	90.3 per cent	66.6 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	40.0 per cent	7.9 (per cent)	30.7 per cent	11.5 per cent	4.9 per cent	15.6 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}/2}})^c$ (per cent)	5.1 (0.4)	22.2 (3.3)	8.8 (0.6)	66.5 (6)	76.4 (7.2)	64.8 (1.5)
	$R (+P_{\text{rot}/2})^c$ (per cent)	22.3 (+ 1.7)	26.7 (+ 4.0)	37.6 (+ 1.8)	91.3 (+ 8.3)	84.6 (+ 8)	97.3 (+ 2.2)
Two observing seasons							
Low activity star	$N_{\text{FAP} < 1 \text{ per cent}}$	47.9 per cent	45.7 per cent	36.5 per cent	74.4 per cent	58.2 per cent	56.0 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	31.7 per cent	20.2 per cent	35.0 per cent	16.2 per cent	16.9 per cent	30.9 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}/2}})^c$ (per cent)	14.6 (1.1)	10.3 (1.5)	15.8 (1.5)	54.7 (5.5)	37.1 (3.4)	49.1 (2.5)
	$R (+P_{\text{rot}/2})^c$ (per cent)	30.5 (+ 2.2)	22.5 (+ 3.3)	52.6 (+ 3.8)	73.5 (+ 7.3)	63.7 (+ 5.9)	88.0 (+ 4.5)
Active star	$N_{\text{FAP} < 1 \text{ per cent}}$	45.8 per cent	95.9 per cent	33.5 per cent	89.4 per cent	97.7 per cent	65.8 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	34.6 per cent	1.9 per cent	42.7 per cent	5.6 per cent	1.1 per cent	28.9 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}/2}})^c$ (per cent)	5.1 (0.4)	8.9 (1.3)	12.9 (0.6)	60.2 (4.5)	49.2 (3.9)	63.6 (1.1)
	$R (+P_{\text{rot}/2})^c$ (per cent)	11.2 (+ 0.9)	9.3 (+ 1.4)	43.9 (+ 1.5)	67.4 (+ 5.1)	50.4 (+ 4.0)	96.7 (+ 1.7)

^aThe false alarm probability (FAP) has been evaluated through a bootstrap with replacement.^bThe FAP is the one provided by the code.^cThe percentage in parenthesis is related to the first harmonic of P_{rot} . For FREDEC, this percentage corresponds to the number of data sets for which only $P_{\text{rot}/2}$ is found as significant peak in the periodogram, while P_{rot} is not.

stellar activity signal is stronger and more influenced by the value of τ_{AR} . Passing from short to long τ_{AR} , a great relative improvement in detecting correct signals is also observed for data sets with $N_{\text{epochs}, s2}$ RVs, which is higher than that observed for low-activity stars.

Case III. Low-activity versus active stars for short τ_{AR} values. When the stellar activity signal is rapidly evolving, the reliability R is higher for quiet stars, independently from the number of observations. One possible explanation is that the simulated P_{rot} are shorter for active stars (Table 1) and, the sampling being similar on average for all the cases, it is more difficult modelling strong and rapidly variable signals, taking into account that τ_{AR} is even shorter for active stars by construction. Moreover, we note that for active stars a high percentage of data sets with $N_{\text{epochs}, s2}$ RVs, patterns are generated that are mistaken for long-term modulations when fitting the data with single sinusoids, coupled with a larger range of test periods (Fig. 8). This is the main reason why the reliability is low. A lower number of spurious long-period signals is found in simulated data sets with $N_{\text{epochs}, s1}$ data, but this is also due to the shorter range of test periods explored by the algorithms. Analogously to the active star case, R decreases with increasing number of RVs in low-activity stars, again due to an artificial long-term modulation introduced in the data. Fig. 8 shows two examples of simulated data sets for stars with low- and high-activity levels, for which the algorithms return a peak at a period much larger than the injected P_{rot} .

Case IV. Orbital period completeness $C_{P_{\text{orb}}}$ for data sets with $P_{\text{rot}} \neq P_{\text{orb}}$. The results in Table 8 show that the $C_{P_{\text{orb}}}$ is in general less than 3 per cent, and lower than $C_{P_{\text{rot}}}$ (much lower for stars with long τ_{AR}). For the case of low-activity stars with long τ_{AR} there is a slight improvement passing from $N_{\text{epochs}, s1}$ to $N_{\text{epochs}, s2}$ data, since $P_{\text{orb}} < P_{\text{rot}}$ for construction, and one could expect the

detection in the periodogram to be eased. However, the percentages of $C_{P_{\text{orb}}}$ stay low, and this denote that a simple frequency analysis of the RVs does not allow to infer the existence of the planetary signal. For low-activity stars, the combination of the sampling and internal precision used in our work can prevent higher values for $C_{P_{\text{orb}}}$.

4.2 DIRECT COMPARISON OF THE ALGORITHM PERFORMANCES

In all the cases discussed in this work, we note that the reliability R of GLS decreases passing from $N_{\text{epochs}, s1}$ to $N_{\text{epochs}, s2}$ data. This is a consequence of the increased number of significant peaks $N_{\text{FAP} < 1 \text{ per cent}}$ with increasing RV measurements. For low-activity stars, the decrease in R is accompanied by an increase in the completeness $C_{P_{\text{rot}}}$ with an increasing number of RV data, i.e. GLS retrieves P_{rot} easier despite it results to be less reliable. In almost all the cases discussed in this work, FREDEC algorithm performs more reliably than GLS and BGLS, as shown by the values of the R parameter, i.e. it is less affected by false-positive signals. This is in line with the results of Pinamonti et al. (2017). Opposite to GLS, R does not change appreciably passing from $N_{\text{epochs}, s1}$ to $N_{\text{epochs}, s2}$ measurements. For those cases where $N_{\text{FAP} < 1 \text{ per cent}}$ increases (e.g. low-active stars with $P_{\text{rot}} \sim P_{\text{orb}}$), this translates to an increased number of correct detections. In all the cases of active stars with long τ_{AR} , the reliability R is close to 100 per cent, even without including those cases where only the first harmonic $P_{\text{rot}/2}$ is recovered. For active stars with short τ_{AR} , R is significantly higher for FREDEC, showing that this algorithm is more effective with quasi-periodic signals variable over short time-scales, that are difficult to model with single sinusoids, as done by GLS and BGLS.

Table 8. Summary of the main results of the analysis performed on the periodograms obtained with GLS, BGLS, and FREDEC (Section 4) for the case where $P_{\text{rot}} \neq P_{\text{orb}}$. The statistics concern the peaks detected with an FAP < 1 per cent. The results are given as 16th, 50th, and 84th percentiles of the parameter distributions.

		$P_{\text{rot}} \neq P_{\text{orb}}$					
	Parameter	GLS ^a	Short τ_{AR} BGLS ^a	FREDEC ^b	GLS ^a	Long τ_{AR} BGLS ^a	FREDEC ^b
One observing season							
Low activity star	$N_{\text{FAP} < 1 \text{ per cent}}$	19.1 per cent	8.5 per cent	23.0 per cent	42.4 per cent	10.9 per cent	38.5 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	35.5 per cent	18.6 per cent	25.6 per cent	26.7 per cent	17.8 per cent	23.2 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}}/2})^c$ (per cent)	7.8 (2.7)	1.2 (2.2)	8.7 (2.5)	33.9 (6.3)	5.2 (3.2)	32.1 (4.6)
	$C_{P_{\text{orb}}} \text{ (per cent)}$	1.6	1.4	2.3	1.6	0.9	2.3
	$R (+P_{\text{rot}}/2)^c$ (per cent)	49.2 (+ 14.1)	30.4 (+ 25.3)	44.8 (+ 6.5)	83.8 (+ 14.9)	54.9 (+ 29.4)	86.2 (+ 10.4)
Active star	$N_{\text{FAP} < 1 \text{ per cent}}$	24.8 per cent	84.3 per cent	31.8 per cent	69.7 per cent	90.3 per cent	64.2 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	36.0 per cent	8.6 per cent	29.8 per cent	15.2 per cent	4.9 per cent	17.7 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}}/2})^c$ (per cent)	5.6 (0.3)	18.1 (2.7)	8.7 (0.5)	62.3 (6.5)	74.0 (7.9)	60.8 (2.6)
	$C_{P_{\text{orb}}} \text{ (per cent)}$	0.8	3.0	1.3	0.5	2.7	1.4
	$R (+P_{\text{rot}}/2)^c$ (per cent)	25.9 (+ 1.2)	25.0 (+ 3.1)	31.1 (+ 1.6)	90.0 (+ 9.3)	84.9 (+ 8.8)	95.6 (+ 4.0)
Two observing seasons							
Low activity star	$N_{\text{FAP} < 1 \text{ per cent}}$	46.9 per cent	45.7 per cent	38.1 per cent	71.6 per cent	57.8 per cent	54.7 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	30.9 per cent	20.4 per cent	33.4 per cent	18.2 per cent	16.0 per cent	30.5 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}}/2})^c$ (per cent)	8.2 (0.8)	5.7 (1.1)	12.5 (1.1)	52 (7.1)	38.6 (3.7)	46.2 (3.2)
	$C_{P_{\text{orb}}} \text{ (per cent)}$	1.3	0.9	2.9	2.2	1.2	5.2
	$R (+P_{\text{rot}}/2)^c$ (per cent)	20.2 (+ 1.6)	14.3 (+ 2.4)	38.1 (+ 2.1)	75.8 (+ 10.0)	68.8 (+ 6.4)	87.4 (+ 4.0)
Active star	$N_{\text{FAP} < 1 \text{ per cent}}$	48.0 per cent	95.2 per cent	34.8 per cent	88.4 per cent	98.0 per cent	65.5 per cent
	$N_{\text{FAP} 1-10 \text{ per cent}}$	29.2 per cent	2.2 per cent	40.0 per cent	5.9 per cent	1.0 per cent	28.2 per cent
	$C_{P_{\text{rot}}} (C_{P_{\text{rot}}/2})^c$ (per cent)	4.8 (0.3)	7.4 (0.8)	11.7 (0.5)	59 (5.6)	48.5 (3.8)	63.3 (0.8)
	$C_{P_{\text{orb}}} \text{ (per cent)}$	0.3	0.6	0.6	0.1	0.4	0.3
	$R (+P_{\text{rot}}/2)^c$ (per cent)	10.5 (+ 0.6)	8.4 (+ 0.9)	34.5 (+ 1.1)	66.9 (+ 6.3)	49.9 (+ 3.9)	96.6 (+ 1.2)

^aThe false alarm probability (FAP) has been evaluated through a bootstrap with replacement.

^bThe FAP is the one provided by the code.

^cThe percentage in parenthesis is related to the first harmonic of P_{rot} . For FREDEC, this percentage corresponds to the number of data sets for which only $P_{\text{rot}}/2$ is found as significant peak in the periodogram, while P_{rot} is not.

Concerning BGLS, we note that for low-activity stars and $N_{\text{epochs}, s1}$ measurements, $C_{P_{\text{rot}}}$ and R are much lower than for GLS and FREDEC, indicating lower performance in retrieving the stellar signal, both for short and long time-scale τ_{AR} . At the same time, BGLS is particularly sensitive to the first harmonic $P_{\text{rot}}/2$, which is detected more often with respect to the number of significant signals $N_{\text{FAP} < 1 \text{ per cent}}$, that is less than the corresponding for GLS and FREDEC. This is due to the definition of the FAP for the BGLS algorithm, which is based on the relative probabilities of the peaks in a periodogram (Pinamonti et al. 2017). When less data are available, several signals are retrieved with similar probabilities, determining high-FAP values. This feature is relaxed for $N_{\text{epochs}, s2}$ data.

For active stars in general, BGLS finds more significant signals ($N_{\text{FAP} < 1 \text{ per cent}}$ is much higher than for GLS and FREDEC), but the reliability R is comparable to, or even lower than that of the other algorithms. This implies that BGLS finds more false-positive signals in these cases.

5 SUMMARY

In this work we presented the results of a statistical analysis of an extended sample of simulated RV data sets⁹ including stellar activity and planetary signals, devised as representations of realistic

measurements for typical spectroscopic exoplanet surveys, in terms of state-of-the-art instrumentation and observing sampling. We simulated different levels and variability time-scales of the stellar activity RV term, assumed as quasi-periodic correlated signal, with two goals: (i) testing the performances of widespread RV modelling techniques in retrieving Doppler signals of small semi-amplitude caused by low-mass planets (Section 3.2), and (ii) exploring the properties of periodograms calculated with three different algorithms, in order to statistically characterize and compare their performances as a function of the stellar activity properties (Section 4). By pursuing the first goal, we assume that the existence of the planet is already demonstrated. This is the case of planets discovered with the transit technique, for which a mass estimate is pursued.

As for the second goal, since we assume that nothing is known a priori, both for the stellar activity and planetary signals, that is a problem of *blind search*, that we have already dealt with in Pinamonti et al. (2017) for different scenarios. As done in that work, we tested the performances of the GLS, BGLS, and FREDEC algorithms for a blind search of planetary signals in presence of stellar activity with well-defined properties. Our mock data sets represent a hard challenge for these algorithms as the injected Doppler signal, which is consistent to what is expected for terrestrial planets, is small compared to the activity signal. Based on our results, there is no unique algorithm which out-performs the others in this case, and the discussion has been necessarily focused on how the stellar signals are recovered. However, within the same

⁹The simulated data sets are freely available for testing other analysis tools and methods, upon request to the authors.

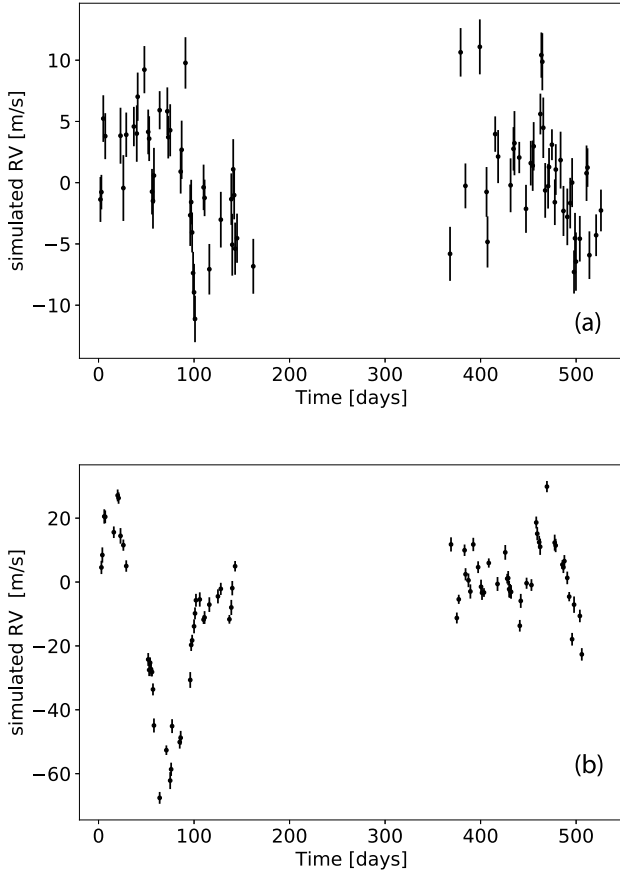


Figure 8. Examples of mock RV data sets spanning two seasons for which the injected active regions evolutionary time scale τ_{AR} is close to the stellar rotation period. (Plot *a*: Low-activity star with $P_{rot} \neq P_{orb}$. Plot *b*: active star with $P_{rot} \sim P_{orb}$). When searched for periodicities using algorithms that fit a sinusoid or a linear combination of sinusoids, the periodograms of such data sets show the main peak ranging between ~ 10 and 20 times P_{rot} .

general framework we defined in this work, new simulations can be devised to move the focus on planetary signals, for instance by increasing their semi-amplitude, or considering more precise RVs, or simulating very-low activity stars.

We analysed specific cases and presented the results schematically, in order to provide quick references to those interested in modelling RV time series for planetary studies. Tables 4, 7, and 8 contain the results for all the addressed scenarios. Among them, we highlight the following outcomes:

(i) generally, the data sets containing more stable activity signals ($P_{rot} \ll \tau_{AR}$) are easier to model, with improved performances in retrieving planetary signals;

(ii) the correlation time-scale τ_{AR} is not always well recovered. When not much data are available (e.g. one semester of observations) it can be easily overestimated, especially in the case of stars with low and quickly variable activity. A tendency towards overestimation is also seen for active stars, but this is less pronounced. This result should be kept in mind when interpreting the fitted values for τ_{AR} astrophysically, in particular when there are no ancillary data available for supporting the reality of long correlation time-scale observed in the RVs;

(iii) the 68.3th percentile appears as a more accurate estimate for K_b than the 50th percentile for low-activity stars when $K_{b, inj} = 1 \text{ m s}^{-1}$, $P_{rot} \neq P_{orb}$ and with two semesters of observations. Same happens for the selected scenarios with $K_{b, inj} > 1 \text{ m s}^{-1}$ discussed in Section 3.2.1;

(iv) for stars with low-activity levels and $P_{rot} \neq P_{orb}$, Bayesian model comparison shows that in general the use of the GP regression provides a significantly better fit to the data, especially with observations spanning two semesters, but this does not always correspond to a better identification of the planetary semi-amplitude, in the studied case of small-amplitude signals;

(v) the different algorithms for periodogram analysis studied in Section 4 follow similar behaviours depending on the hyperparameters of the stellar activity model, being most effective when the star is quiet and τ_{AR} is long;

(vi) highly variable stellar activity (short τ_{AR}) affects significantly the performances of algorithms to search for periodic signals, especially for active stars. Their reliability, as defined in Table 6, is not very high due to the presence of a significant number of false-positive signals that does not decrease after increasing the number of measurements;

(vii) in the cases with strong and highly variable stellar activity, which produces the most complex signal structures, the multifrequency approach applied by FREDEC proves to be most effective, as proved by the higher R value with respect to the other algorithms. This is consistent with the findings of Pinamonti et al. (2017), which highlighted FREDEC to be less prone to false detections in the analysis of time series containing multiple complex signals.

It is worth noticing that the performances of all the periodogram algorithms in retrieving the planetary signals are quite poor in all the analysed scenarios, with $C_{P_{orb}} \lesssim 5$ per cent. This once again highlights the importance of applying high-level analysis techniques when trying to model planetary signals around active stars (e.g. see Dumusque et al. 2017, and references therein, for a review of different methods to deal with stellar activity).

Even though they must be considered mostly valid within the framework defined for our simulations, these results could be of some interest in a more general context, and could be used for devising diversified statistical studies aimed at optimizing follow-up strategies for different targets, number of planets, and system architectures. They can be also extended to next generation high-resolution spectrographs, as for instance the operating VLT/ESPRESSO (Pepe et al. 2014), the upcoming EXPRES (Jurgenson et al. 2016), NEID (Schwab et al. 2016), and ELT-HIRES (Marconi et al. 2016), or NIR spectrographs such as CARMENES (Quirrenbach et al. 2016), SPIRou (Artigau et al. 2014), HPF (Mahadevan et al. 2014), or NIRPS (Wildi et al. 2017), that are expected to provide more precise RV measurements. Presently, the operating TESS mission is already detecting new transiting planets, and it is expected to discover ~ 1000 planets with $R < 4 R_{\oplus}$ at short-time cadence (2 min), 250 of which smaller than $2 R_{\oplus}$ (Barclay, Pepper & Quintana 2018). Taking into account planets that can actually be characterizable, i.e. are most suitable for mass measurements through precise RV observations, Barclay et al. (2018) predict a distribution of detected orbital periods with a median of 7–8 d, likely less than 29–35 d at 95 per cent significance level. Therefore, our simulations are particularly useful for planning the spectroscopic follow-up of small-size, low-mass planets discovered right now by TESS, and in the near future by the PLATO 2.0 mission (Rauer et al. 2014).

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APPENDIX A: SIMULATIONS PROPERTIES

Table A1 shows some relations existing between the injected model parameters considered in this work, generated as described in Section 2.

Table A1. Relations between some of the injected model parameters considered in this work, and typical rms of the data sets. Each value is given as 16th, 50th, and 84th percentiles of each distribution consisting of 5000 samples.

Parameter		$P_{\text{rot}} \sim P_{\text{orb}}$		$P_{\text{rot}} \neq P_{\text{orb}}$	
		Short τ_{AR}	Long τ_{AR}	Short τ_{AR}	Long τ_{AR}
One observing season					
Low-activity star	$P_{\text{rot}} - P_{\text{orb}}$ (d)	-0.03 ± 2.13	-0.1 ± 2.1	6.9 ± 2.1	7.1 ± 2.1
	$\tau_{\text{AR}} - P_{\text{rot}}$ (d)	0.0016 ± 2.1	$179.9^{+10.4}_{-9.6}$	-0.006 ± 2.1	$179.7^{+10.4}_{-10.2}$
	RV_{rms} (m s^{-1})	$3.4^{+0.7}_{-0.6}$	$2.9^{+0.8}_{-0.5}$	$3.4^{+0.7}_{-0.5}$	$2.9^{+0.8}_{-0.5}$
Active star	$P_{\text{rot}} - P_{\text{orb}}$ (d)	0.02 ± 1.4	$-0.03^{+1.43}_{-1.39}$	-8.0 ± 1.8	-8.0 ± 1.8
	$\tau_{\text{AR}} - P_{\text{rot}}$ (d)	-0.005 ± 1.4	$90.4^{+10.1}_{-10.2}$	0.02 ± 1.4	$90.2^{+9.7}_{-9.9}$
	RV_{rms} (m s^{-1})	$14.2^{+2.6}_{-2.3}$	$10.9^{+4.1}_{-3.3}$	$14.1^{+2.6}_{-2.3}$	$10.9^{+3.9}_{-3.2}$
Two observing seasons					
Low-activity star	$P_{\text{rot}} - P_{\text{orb}}$ (d)	-0.04 ± 2.2	0.03 ± 2.1	7.0 ± 2.1	6.9 ± 2.1
	$\tau_{\text{AR}} - P_{\text{rot}}$ (d)	0.06 ± 2.1	$180.1^{+10.4}_{-10.1}$	0.008 ± 2.1	180.3 ± 10.1
	RV_{rms} (m s^{-1})	$3.5^{+0.6}_{-0.5}$	$3.2^{+0.7}_{-0.6}$	$3.5^{+0.6}_{-0.5}$	$3.2^{+0.7}_{-0.5}$
Active star	$P_{\text{rot}} - P_{\text{orb}}$ (d)	-0.01 ± 1.4	$0.04^{+1.39}_{-1.42}$	-8.0 ± 1.8	$-8.0^{+1.8}_{-1.7}$
	$\tau_{\text{AR}} - P_{\text{rot}}$ (d)	0.0035 ± 1.4	$90.2^{+9.9}_{-10.0}$	0.0006 ± 1.4	89.9 ± 9.7
	RV_{rms} (m s^{-1})	$14.7^{+2.0}_{-1.8}$	$13.0^{+3.4}_{-3.0}$	$14.7^{+1.9}_{-1.8}$	$12.9^{+3.3}_{-2.9}$

APPENDIX B: ASSESSING POSSIBLE BIASES INTRODUCED BY THE OBSERVING CALENDAR

We verified whether our particular choice of the 63-nights calendar could have introduced biases in our results through three different checks: (i) we calculated the median window functions for each scenario, and they do not show significant peaks at specific frequencies (except for the expected 1-yr alias for $N_{\text{epochs},s2}$ data), which would indicate the presence of aliases introduced by the sampling (Fig. B1); (ii) we found that the orbits of the simulated planets are on average uniformly covered in phase by the RV

measurements, i.e. there are no parts of the orbit systematically over/undersampled (Fig. B2); (iii) we simulated 200 RV data sets by randomly generated 40 epochs from a uniform distribution over a range of one semester, and then adding 40 more epochs randomly drawn within a time range shifted by 365 d. This implies that each data set has a different observing calendar which does not stem from the same array of epochs. We considered the case of a quiet star with $P_{\text{rot}} \neq P_{\text{orb}}$, long τ_{AR} , and two seasons of observations. We found that the results of a GP-based MC analysis are similar to those presented in Section 3, indicating that the latter are free from biases due to a particular choice of the mold calendar.

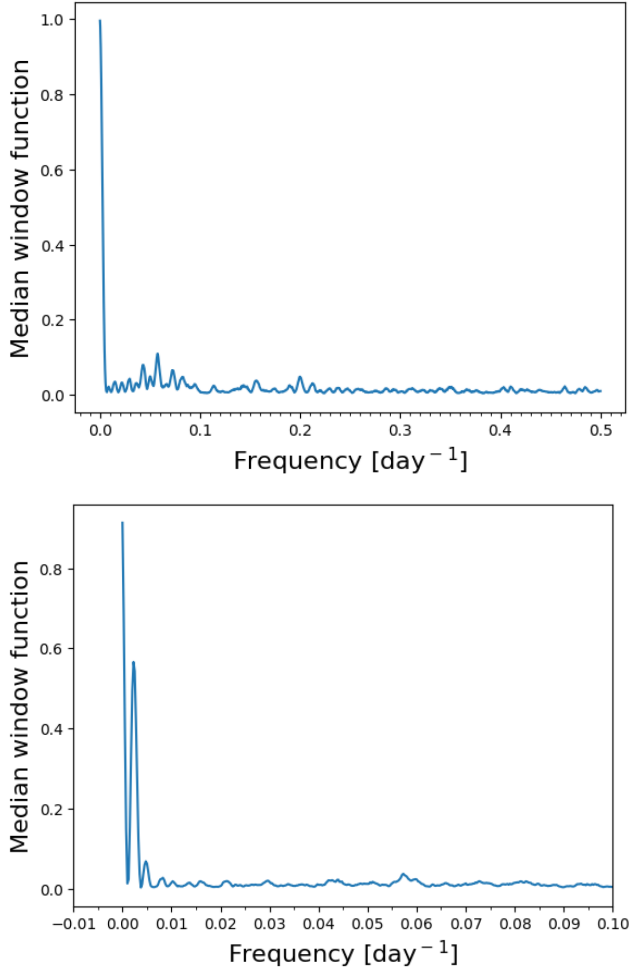


Figure B1. Examples of median window functions for different simulated scenarios. *Upper panel:* quiet star with $P_{\text{rot}} \sim P_{\text{orb}}$, long τ_{AR} , and one season of observations. *Lower panel:* active star with $P_{\text{rot}} \neq P_{\text{orb}}$, long τ_{AR} , and two seasons of observations.

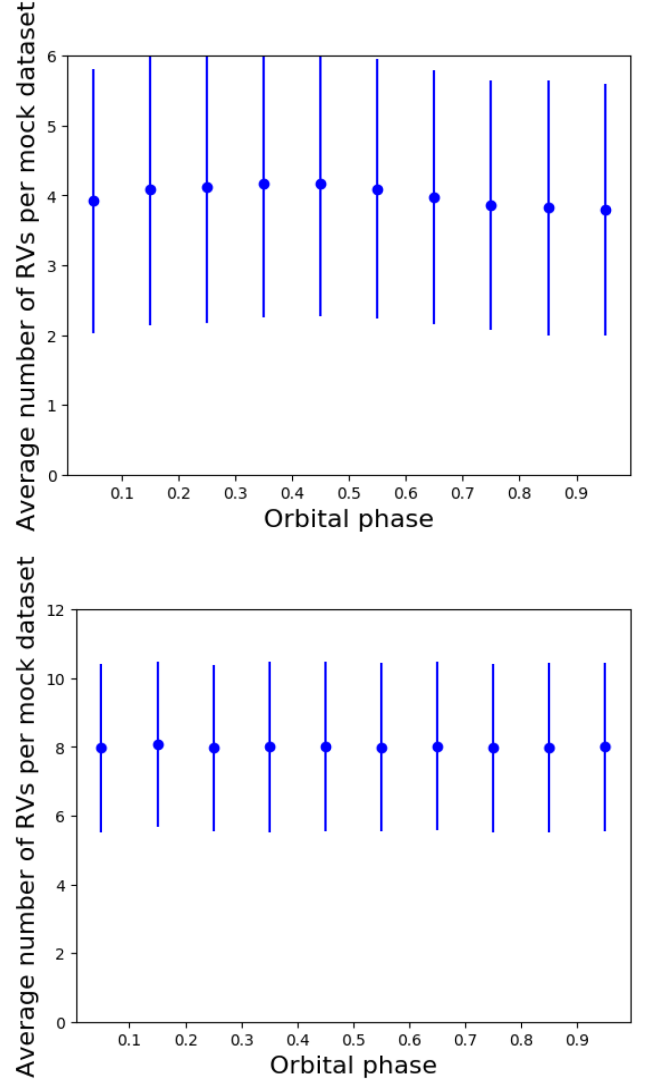


Figure B2. Examples showing how the number of RV data distributes on average (per single RV data set) within phase bins of size 0.1, for different simulated scenarios. *Upper panel:* quiet star with $P_{\text{rot}} \sim P_{\text{orb}}$, long τ_{AR} , and one season of observations. *Lower panel:* quiet star with $P_{\text{rot}} \neq P_{\text{orb}}$, long τ_{AR} , and two seasons of observations. The error bars represent the rms of the number of RV measurements within each phase bin.

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