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# Stellar intensity interferometry of Vega in photon counting mode

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## ABSTRACT

Stellar intensity interferometry is a technique based on the measurement of the second-order spatial correlation of the light emitted from a star. The physical information provided by these measurements is the angular size and structure of the emitting source. A worldwide effort is presently underway to implement stellar intensity interferometry on telescopes separated by long baselines and on future arrays of Cherenkov telescopes. We describe an experiment of this type, realized at the Asiago Observatory (Italy), in which we performed for the first time measurements of the correlation counting photon coincidences in post-processing by means of a single photon software correlator and exploiting entirely the quantum properties of the light emitted from a star. We successfully detected the temporal correlation of Vega at zero baseline and performed a measurement of the correlation on a projected baseline of  $\sim 2$  km. The average discrete degree of coherence at zero baseline for Vega is  $\langle g^{(2)} \rangle = 1.0034 \pm 0.0008$ , providing a detection with a signal-to-noise ratio  $S/N \gtrsim 4$ . No correlation is detected over the km baseline. The measurements are consistent with the expected degree of spatial coherence for a source with the 3.3 mas angular diameter of Vega. The experience gained with the Asiago experiment will serve for future implementations of stellar intensity interferometry on long-baseline arrays of Cherenkov telescopes.

**Key words:** instrumentation: interferometers – techniques: interferometric – stars: individual:  $\alpha$  Lyr (Vega).

## 1 INTRODUCTION

Ordinary (phase) interferometry is widely used in radio Astronomy to measure the size of radio sources and deals with the first-order spatial correlation of the radiation emitted from a source. Conversely, intensity interferometry exploits the second-order spatial correlation of light (Glauber 1963). A pioneering astronomical experiment of intensity interferometry using the wave nature of light and aiming at measuring stellar radii was performed from the '50s through the '70s of the last century by Hanbury Brown and Twiss (Hanbury Brown 1956, 1974; Brown & Twiss 1957, 1958; Hanbury Brown, Davis & Allen 1974). They measured the cross-correlation of the intensity fluctuations of the star signals collected with two photomultipliers at the foci of two 6.5-m telescopes separated by a baseline up to 180 m. The experiment led to the direct interferometric measurement of the radii of 32 single stars of O-F spectral type (Hanbury Brown et al. 1974), greatly improving the scant sample of measurements of K-M giants/supergiants previously obtained with the Michelson's phase interferometer (Pease 1931).

After some preparatory experimental activities carried out by some groups (Tan, Chan & KurtSiefer 2016; Zampieri et al. 2016; Matthews et al. 2018; Weiss, Rupert & Horch 2018), new successful stellar intensity interferometry (SII) measurements à la Hanbury Brown and Twiss have recently been realized using the particle nature of light and modern fast single-photon counters. The first intensity correlation

measured with starlight from conventional optical telescopes since the historical experiments of Hanbury Brown and Twiss has been performed by Guérin et al. (2017), and more recently by Rivet et al. (2020). The renewed interest for SII sparkled from the planned realization of extended arrays of Cherenkov telescopes for Very High Energy Astronomy. They will have both large collecting areas and a large number of baselines, from  $\sim 100$  m up to  $\sim 1$  km, thus indirectly providing a suitable infrastructure for performing SII measurements and visible image reconstruction with an unprecedented spatial resolution (Le Bohec & Holder 2006; Nuñez et al. 2012a, b; Dravins et al. 2013; Rou et al. 2013; Kieda et al. 2019). These measurements will allow us to do science that has not yet been possible before. Recently, the capability of performing SII measurements and the potential of the technique with the MAGIC and VERITAS Cherenkov telescopes has been convincingly demonstrated by Acciari et al. (2020) and Abeyssekara et al. (2020), respectively.

In this context, in 2015 and 2016 we started the first experimental runs of the Asiago Intensity Interferometer, using our fast photon counters Aqueye+ and Iqueye (Naletto et al. 2016; Zampieri et al. 2016). The instrumentation allows us both to detect the correlation of the signal at essentially zero baseline (exploiting the instrument internal sub-apertures) and to perform measurements on long separations, thus demonstrating the feasibility of km-baseline-long photon counting SII.

Between 2017 and 2018, we devoted several runs to reach an adequate control of the systematic errors and to implement an efficient approach for the single-photon data reduction and analysis.

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The final instrumental set-up and data analysis technique, which led to a successful implementation in 2019, are reported here.

Because of the small collecting area of the telescopes, we focused on a bright target. We selected Vega, the second brightest star in the Northern hemisphere ( $V = 0.03$ , Ducati 2002; A0Va spectral type, Gray et al. 2003). Its angular diameter is  $\simeq 3.3$  mas ( $3.28 \pm 0.01$  mas, Ciardi et al. 2001; 3.324 mas, Monnier et al. 2012). Despite being one of the brightest stars in the sky, Vega quite recently revealed new and unexpected properties. Optical interferometric observations showed that the star has the asymmetric brightness distribution of the slightly offset polar axis of a star rotating at 93 per cent of its breakup speed (Peterson et al. 2006).

The plan of the paper is the following. In Section 2, we describe our instrumental interferometric setup. In Section 3, we report the post-processing single-photon data analysis technique adopted for calculating the degree of correlation, and in Section 4 we list the Aqueye+ and IFI+Iqueye observations of Vega carried out in 2019 July–August and November. In Section 5, we discuss the instrument systematics and the final adopted calibration of our measurements. Finally, in Section 6 we show the results of our analysis and in Section 7 we shortly discuss the possible future implementations of our photon counting approach for measurements of SII.

## 2 THE ASIAGO STELLAR INTENSITY INTERFEROMETER

Aqueye+ and Iqueye<sup>1</sup> are narrow field-of-view photon counting photometers with sub-nanosecond absolute time accuracy (Barbieri et al. 2009; Naletto et al. 2009, 2013; Zampieri et al. 2015). Their main features are: a field of view of a few arcsec, a 4-split pupil optical design achieved using a pyramidal mirror, Single Photon Avalanche Diode (SPAD) detectors with tens of ps time resolution, an acquisition system capable of sub-ns time tagging accuracy with respect to UTC. The 4-split pupil optical design causes the incoming beam to be divided into four sub-apertures that are focused on four independent SPADs. The four sub-apertures allow us to perform a cross-correlation of the signal also at zero baseline (Naletto et al. 2016; Zampieri et al. 2016)<sup>2</sup>, which is crucial to calibrate the degree of coherence. In the following, we will refer to the sub-apertures of Aqueye+ and Iqueye with  $A$ ,  $B$ ,  $C$ , and  $D$ , where  $A - C$  and  $B - D$  represent the two baselines with face-to-face detectors.

The main observing facilities in Asiago (Italy), the 1.22-m Galileo telescope and the 1.82-m Copernicus telescope, are located in the resorts of Pennar and Cima Ekar, almost 4 km apart. Equipped with Aqueye+ and Iqueye, the two telescopes are well suited to realize a photon counting km-baseline intensity interferometer (see Table 1). Aqueye+ is directly mounted at the Copernicus telescope, while Iqueye is fiber-coupled with the Galileo telescope by means of a dedicated instrument, the Iqueye Fiber Interface (IFI; Zampieri et al. 2019).

The measurements were performed using two different sets of filters, an  $H\alpha$  filter plus a  $\times 10$  neutral density filter (ND1) and a narrow band interferometric filter (hereafter referred to as II filter; see Table 2). All the acquired data are stored for the post-processing analysis.

<sup>1</sup><http://web.oapd.inaf.it/zampieri/aqueye-iqueye/index.html>

<sup>2</sup>See also Capraro et al. (2010) for a preliminary measurement at zero baseline performed at the New Technology Telescope, in Chile.

**Table 1.** Coordinates, distance, and baseline of the Galileo (T122) and Copernicus (T182) telescopes in Asiago. Coordinates refer to the intersections of the hour angle and declination axes.

|                                                 | Geographic                    | Cartesian (m) |
|-------------------------------------------------|-------------------------------|---------------|
| Geographic and Cartesian geocentric coordinates |                               |               |
| T122                                            | 11 31 35.14 E (Long)          | 4360008.6 (X) |
|                                                 | 45 51 59.22 N (Lat)           | 889148.3 (Y)  |
|                                                 | 1094.6 m (Elev <sup>1</sup> ) | 4555709.2 (Z) |
| T182                                            | 11 34 08.397 E (Long)         | 4360935.4 (X) |
|                                                 | 45 50 54.894 N (Lat)          | 892712.8 (Y)  |
|                                                 | 1376.2 m (Elev <sup>1</sup> ) | 4554527.8 (Z) |
| Distance T182-T122 (m)                          |                               |               |
| 281.6 (Elev <sup>1</sup> )                      |                               |               |
| 3867.8 (Total)                                  |                               |               |
| Maximum projected baseline T182-T122 (m)        |                               |               |
| 3213.8 (E-W)                                    |                               |               |
| 2133.6 (N-S)                                    |                               |               |
| 3857.6 (Total)                                  |                               |               |

<sup>1</sup>Elevation measured from sea level.

**Table 2.** Filters used for the 2019 Aqueye+ and IFI+Iqueye observations of Vega.

| Filters          |                    |                        |                              |
|------------------|--------------------|------------------------|------------------------------|
| Filter           | $\lambda_c^a$ (nm) | FWHM <sup>b</sup> (nm) | peak transmission (per cent) |
| H $\alpha$ + ND1 | 656.7              | 3                      | 62                           |
| II               | 510.5              | 0.3                    | 35                           |

<sup>a</sup>Central wavelength.

<sup>b</sup>full width at half-maximum.

## 3 DISCRETE DEGREE OF COHERENCE AND PHOTON-COUNTING SOFTWARE CORRELATOR

The main observable for SII is the second-order (discrete) degree of coherence  $g^{(2)}(\tau, d)$  of a star, that measures the degree of correlation of its light and depends on the telescopes/sub-apertures separation  $d$  and the relative delay  $\tau$  between them. We calculate  $g^{(2)}(\tau, d)$  in post-processing using the expression (e.g. Naletto et al. 2016; Zampieri et al. 2016):

$$g^{(2)}(\tau, d) = \frac{N_{XY}N}{N_X N_Y}, \quad (1)$$

where  $N_X$  and  $N_Y$  are the number of photons detected on the sub-apertures  $X$  and  $Y$  (of the same telescope or of two different telescopes) in a time interval  $T_s$ ,  $N_{XY}$  is the number of simultaneous detections (coincidences) in both sub-apertures in a small time bin  $dt$ , and  $N = T_s/dt$  is the total number of bins in time  $T_s$ . The major contribution to  $N_{XY}$  comes from random uncorrelated coincidences. The signal is a tiny excess of coincidences related to the quantum nature of light (bosons giving a joint detection probability greater than that for two independent events).

A dedicated software package (AQUEYE+IQUEYE SOFTWARE CORRELATOR, written in LINUX BASH SHELL, FORTRAN, PYTHON) was developed for determining the number of coincidences  $N_{XY}$  and the degree of coherence  $g^{(2)}$  of our event lists. The correlation is entirely performed in post-processing using the following procedure:

(i) The (non-barycentred) event lists are divided in  $N_s$  segments of duration  $T_s = 8.64$  s and then searched for coincidences  $N_{XY}$  in time

bins of duration  $dt \simeq 400$  ps. The choice of the time bin is discussed below.

(ii) The degree of coherence  $g^{(2)}$  is then calculated in each segment using equation (1) and the values are then averaged out over the various segments of an acquisition. An additional average is performed over all possible combinations  $X - Y$  of the sub-apertures. To calculate the temporal correlation a delay  $\tau$  is added or subtracted to the photons of one sub-aperture and the calculation is then repeated. The delay is taken in steps of  $\simeq 200$  ps in the interval between  $-20.5$  ns and  $+20.5$  ns. The average value of  $g^{(2)}(\tau, d)$  for the  $k$ -th acquisition is then:

$$g_k^{(2)}(\tau, d) = \frac{1}{N_b N_s} \sum_{j=1}^{N_b} \sum_{i=1}^{N_s} g_{ij}^{(2)}, \quad (2)$$

where  $i$  is the summation index over the  $N_s$  time segments and  $j$  that over the  $N_b$  sub-apertures.

(iii) The final calibrated value of  $g^{(2)}(\tau, d)$  is calculated subtracting the measurement averaged over the acquisitions with the H $\alpha$ +ND1 filters from the measurement averaged over the acquisitions with the II filter, i.e.

$$< g^{(2)}(\tau, d) > = 1 + < g^{(2)}(\tau, d) >_{II} - < g^{(2)}(\tau) >_{H\alpha+ND1}, \quad (3)$$

where the average is over the acquisitions.

(iv) If the amount of data is sufficient, the calculation is done independently for each observing night and a final average of  $g^{(2)}(\tau, d)$  is then performed using the measurements acquired each night. For the observations reported here, this was possible only for the zero baseline data acquired with Aqueye+.

The search for coincidences in step (1) is performed after binning the event lists. Therefore, two photons are considered coincident in time bin  $dt$  if their arrival time is within the bounds of the time bin. If two photons do not fall inside the same bin, they are not considered coincident, even if the difference of their arrival times is smaller than  $dt$ . The algorithm is optimized to record only the time bins in which a photon detection actually occurs, discarding all the others. As discussed below, the exquisite accuracy of our timing allows us to push the sampling time  $dt$  to the limit and we eventually selected  $dt \simeq 400$  ps.

The expected theoretical signal-to-noise ratio of a measurement of  $g^{(2)}(0, d)$  in a time interval  $T$  and with a sampling time  $dt$  is (e.g. Nalletto et al. 2016; Zampieri et al. 2016)

$$S/N = n(\lambda/c)(\lambda/\Delta\lambda)\alpha|\gamma(0, d)|^2[T/(2dt)]^{1/2}, \quad (4)$$

where  $n$  is the geometric average of the source count rate over two sub-apertures (or telescopes) in photons per second in the optical bandpass  $\Delta\lambda$ ,  $\lambda$  is the central wavelength of the bandpass,  $\alpha$  the detector efficiency, and  $|\gamma(0, d)|^2$  the square modulus of the degree of coherence at zero delay. Plugging in the values for our measurement/instrumental set-up ( $n \sim 1$  Mc/s,  $\lambda = 510.5$  nm,  $\Delta\lambda = 0.3$  nm,  $\alpha = 0.5$ ,  $T \sim 30$  min,  $dt \sim 400$  ps) and assuming full correlation at zero baseline ( $|\gamma(0, d)|^2 = 1$ ), we obtain  $S/N \sim 4$  at  $d = 0$ . Thus, despite the short acquisition time, we expected to be able to obtain a significant measurement of  $g^{(2)}$ .

### 3.1 Choice of the time bin $dt$

An important technical aspect of the measurement is the choice of the time bin  $dt$ . The very high time accuracy of the acquisition chain of Aqueye+ and Iqueye allows us to push this parameter at the limit and gain on the signal-to-noise ratio of the measurement. For

the zero baseline measurement, we are limited only by the relative time accuracy among the sub-apertures, which is  $\simeq 100$  ps. The most stringent constraints come from the absolute time accuracy when correlating the data from the two telescopes. The error induced by the correction for the light traveltime delay between them is typically  $\simeq 200$  ps. The time dispersion induced by the multimode optical fiber injecting the starlight into Iqueye is  $\lesssim 250$  ps (see equation 6 in Zampieri et al. 2016).<sup>3</sup> Therefore, the final choice is dictated mainly by the absolute accuracy of the photon arrival times with respect to UTC, which is  $\leq 1.5$ – $2$  ns for the typical clock drift and acquisition length of the observations used here. With a time bin  $dt \simeq 400$  ps correlated photons will then spread over 4–5 adjacent time bins, leading to a decrease of the signal-to-noise ratio by a factor  $\simeq 2$  (equation 4). This would not allow us to achieve a significant detection of any potential correlation between the two telescopes, but is sufficient to exclude that a correlation exists, as shown in Section 6. On the other hand, for the measurement at zero baseline, a time bin  $dt \simeq 400$  ps allows us to achieve a signal-to-noise ratio adequate for a detection (equation 4). The actual time bin was set to 16 times the resolution of the time-to-digital-converter (24.2 ps) and is then  $dt \simeq 387$  ps.

## 4 OBSERVATIONS AND DATA ANALYSIS

We report on the results of two runs devoted to intensity interferometry observations of Vega in Asiago, the first performed on 2019 July 31–August 1 and the second on 2019 November 25–28. The log of the acquisitions is shown in Table 3. During the 2019 July–August run, we specifically aimed at detecting the temporal correlation of the light from Vega using the sub-apertures of Aqueye+, and hence no IFI+Iqueye observation was carried out. Simultaneous acquisitions with both instruments were done during the November run.

We retained only the acquisitions for which sky conditions were good (no significant veils or clouds). A total of 38 min of useful data with both the H $\alpha$  and the II filters were acquired with Aqueye+ on 2019 July 31–August 1. The total duration of the simultaneous Aqueye+/IFI+Iqueye acquisitions (Nov 25+28) was 28 min with the H $\alpha$  filter and 39 min with the II filter. The average count rate measured with Aqueye+/IFI+Iqueye was  $\sim 1.9/0.1$  Mc/s in the H $\alpha$  filter and  $\sim 2.7/0.2$  Mc/s in the II filter.

The preliminary reduction of the data was performed using a dedicated software (Zampieri et al. 2015). The whole acquisition and reduction chain ensures an absolute time accuracy of  $\sim 0.5$  ns with respect to UTC and a relative accuracy in a single acquisition of  $\sim 100$  ps (Nalletto et al. 2009). The intensity interferometry data analysis was done in post-processing as described in Section 3.

## 5 INSTRUMENT SYSTEMATICS

Before presenting the results of our analysis, in this section we discuss how we reached an adequate control of the instrumentation and the observational strategy after identifying a number of systematic effects in our measurements. These are crucial issues to investigate, especially when performing low signal-to-noise SII measurements in photon counting and post-processing.

Fig. 1 shows the temporal correlation at zero baseline for the Aqueye+ observations of Vega taken on 2019 November 28. As can be seen in panel A,  $g^{(2)}$  exceeds dramatically the expected value of 1

<sup>3</sup>The focal length of the lens injecting light into the optical fiber was changed and is now 100 mm.

**Table 3.** Log of the 2019 July 31–August 1 and 2019 November 25–28 observations of Vega taken with Aqueye+ at the Copernicus telescope and IFI+Iqueye at the Galileo telescope in Asiago.

| 2019 July 31–August 1 <sup>1</sup> |                 |                              | 2019 November 25 <sup>2</sup> |                 |                              | 2019 November 28 <sup>3</sup> |                 |                              |
|------------------------------------|-----------------|------------------------------|-------------------------------|-----------------|------------------------------|-------------------------------|-----------------|------------------------------|
| Observation ID                     | Filter          | Duration <sup>4</sup><br>(s) | Observation ID <sup>5</sup>   | Filter          | Duration <sup>6</sup><br>(s) | Observation ID <sup>5</sup>   | Filter          | Duration <sup>6</sup><br>(s) |
| 20190731–215000                    | II              | 12                           | 20191125–191218               | II              | 60                           | 20191128–192237               | II              | 60                           |
| 20190731–215642                    | II              | 61                           | 20191125–191351               | II              | 60                           | 20191128–192406               | II              | 60                           |
| 20190731–220359                    | II              | 63                           | 20191125–191522               | II              | 60                           | 20191128–193750 (A+I)         | II              | 60 (52)                      |
| 20190731–221812                    | H $\alpha$ +ND1 | 60                           | 20191125–191723               | II              | 60                           | 20191128–193926 (A+I)         | II              | 60 (52)                      |
| 20190731–222450                    | H $\alpha$ +ND1 | 121                          | 20191125–191856               | II              | 60                           | 20191128–194157               | II              | 60                           |
| 20190731–223128                    | H $\alpha$ +ND1 | 89                           | 20191125–192030               | II              | 60                           | 20191128–194406               | II              | 60                           |
| 20190731–224153                    | II              | 155                          | 20191125–192208               | II              | 60                           | 20191128–194542 (A+I)         | II              | 60 (43)                      |
| 20190731–224839                    | II              | 32                           | 20191125–192340               | II              | 60                           | 20191128–194716 (A+I)         | II              | 60 (43)                      |
| 20190731–225518                    | II              | 32                           | 20191125–192521               | II              | 60                           | 20191128–194853 (A+I)         | II              | 60 (52)                      |
| 20190731–230447                    | H $\alpha$ +ND1 | 60                           | 20191125–192652               | II              | 60                           | 20191128–195028 (A+I)         | II              | 60 (52)                      |
| 20190731–231122                    | H $\alpha$ +ND1 | 63                           | 20191125–192827               | II              | 60                           | 20191128–195203 (A+I)         | II              | 60 (52)                      |
| 20190731–231756                    | H $\alpha$ +ND1 | 127                          | 20191125–192957               | II              | 60                           | 20191128–195339 (A+I)         | II              | 60 (52)                      |
| 20190731–233324                    | II              | 22                           | 20191125–193130               | II              | 60                           | 20191128–195518 (A+I)         | II              | 60 (52)                      |
| 20190731–234119                    | II              | 62                           | 20191125–193312               | II              | 60                           | 20191128–195702 (A+I)         | II              | 60 (52)                      |
| 20190731–234757                    | II              | 61                           | 20191125–193552               | H $\alpha$ +ND1 | 60                           | 20191128–195839 (A+I)         | II              | 60 (52)                      |
| 20190731–235904                    | H $\alpha$ +ND1 | 14                           | 20191125–193724               | H $\alpha$ +ND1 | 60                           | 20191128–200019 (A+I)         | II              | 60 (52)                      |
| 20190801–000547                    | H $\alpha$ +ND1 | 63                           | 20191125–194412               | H $\alpha$ +ND1 | 60                           | 20191128–200153 (A+I)         | II              | 60 (52)                      |
| 20190801–001322                    | H $\alpha$ +ND1 | 96                           | 20191125–194543               | H $\alpha$ +ND1 | 60                           | 20191128–200326 (A+I)         | II              | 60 (52)                      |
| 20190801–002259                    | II              | 14                           | 20191125–194718               | H $\alpha$ +ND1 | 60                           | 20191128–200457 (A+I)         | II              | 60 (52)                      |
| 20190801–002940                    | II              | 63                           | 20191125–194853               | H $\alpha$ +ND1 | 60                           | 20191128–200840               | H $\alpha$ +ND1 | 60                           |
| 20190801–003628                    | II              | 63                           | 20191125–195026               | H $\alpha$ +ND1 | 60                           | 20191128–201010               | H $\alpha$ +ND1 | 60                           |
| 20190801–004723                    | H $\alpha$ +ND1 | 102                          | 20191125–195158               | H $\alpha$ +ND1 | 60                           | 20191128–201141               | H $\alpha$ +ND1 | 60                           |
| 20190801–005407                    | H $\alpha$ +ND1 | 90                           | 20191125–195337               | H $\alpha$ +ND1 | 60                           | 20191128–201321               | H $\alpha$ +ND1 | 60                           |
| 20190801–010044                    | H $\alpha$ +ND1 | 61                           | 20191125–195640               | H $\alpha$ +ND1 | 60                           | 20191128–201547 (A+I)         | H $\alpha$ +ND1 | 60 (43)                      |
| 20190801–011050                    | II              | 68                           | 20191125–195815               | H $\alpha$ +ND1 | 60                           | 20191128–201742 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–011727                    | II              | 60                           | 20191125–195951               | H $\alpha$ +ND1 | 60                           | 20191128–201914 (A+I)         | H $\alpha$ +ND1 | 60 (43)                      |
| 20190801–012402                    | II              | 58                           | 20191125–200125               | H $\alpha$ +ND1 | 60                           | 20191128–202055 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–013512                    | H $\alpha$ +ND1 | 84                           | 20191125–200257               | H $\alpha$ +ND1 | 60                           | 20191128–202230 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–014148                    | H $\alpha$ +ND1 | 91                           | 20191125–200501               | II              | 60                           | 20191128–202403 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–014824                    | H $\alpha$ +ND1 | 62                           | 20191125–200633               | II              | 60                           | 20191128–202541 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–015849                    | II              | 13                           | 20191125–200807               | II              | 60                           | 20191128–202714 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–020547                    | II              | 58                           | 20191125–200936               | II              | 60                           | 20191128–202900 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–021220                    | II              | 58                           | 20191125–201107               | II              | 60                           | 20191128–203034 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–022326                    | H $\alpha$ +ND1 | 24                           | 20191125–201251               | II              | 60                           | 20191128–203224 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–023002                    | H $\alpha$ +ND1 | 121                          | 20191125–201431               | II              | 60                           | 20191128–203406 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–023642                    | H $\alpha$ +ND1 | 119                          | 20191125–201606               | II              | 60                           | 20191128–203543 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–024913                    | II              | 86                           | 20191125–201738               | II              | 60                           | 20191128–203723 (A+I)         | H $\alpha$ +ND1 | 60 (43)                      |
| 20190801–025558                    | II              | 59                           | 20191125–201911               | II              | 60                           | 20191128–203857 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      |
| 20190801–030259                    | II              | 30                           | 20191125–202044               | II              | 60                           | 20191128–204118               | II              | 60                           |
| 20190801–031310                    | H $\alpha$ +ND1 | 60                           | 20191125–202227               | II              | 60                           | 20191128–204250               | II              | 60                           |
| 20190801–031945                    | H $\alpha$ +ND1 | 62                           | 20191125–202403               | II              | 60                           | 20191128–204437               | II              | 60                           |
| 20190801–032621                    | H $\alpha$ +ND1 | 58                           | 20191125–202552               | II              | 60                           | 20191128–204615               | II              | 60                           |
| 20190801–033728                    | II              | 122                          | 20191125–202725               | II              | 60                           | 20191128–204759               | II              | 60                           |
| 20190801–034405                    | II              | 58                           | 20191125–202944 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–204939 (A+I)         | II              | 60 (52)                      |
| 20190801–035042                    | II              | 89                           | 20191125–203305 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–205122 (A+I)         | II              | 60 (52)                      |
| 20190801–040026                    | H $\alpha$ +ND1 | 176                          | 20191125–203441 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–205253 (A+I)         | II              | 60 (52)                      |
| 20190801–040702                    | H $\alpha$ +ND1 | 62                           | 20191125–203618 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–205428 (A+I)         | II              | 60 (52)                      |
| 20190801–041344                    | H $\alpha$ +ND1 | 93                           | 20191125–203757               | H $\alpha$ +ND1 | 60                           | 20191128–205603 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–203941 (A+I)         | H $\alpha$ +ND1 | 60 (43)                      | 20191128–205743 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–204119 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–205920 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–204256 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–210056 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–204429 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–210244 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–204607 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–210418 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–204758 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–210552 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–204935 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–210725 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–205112 (A+I)         | H $\alpha$ +ND1 | 60 (43)                      | 20191128–211053 (A+I)         | II              | 60 (43)                      |
|                                    |                 |                              | 20191125–205253 (A+I)         | H $\alpha$ +ND1 | 60 (52)                      | 20191128–211237 (A+I)         | II              | 60 (52)                      |
|                                    |                 |                              | 20191125–205536               | II              | 60                           |                               |                 |                              |
|                                    |                 |                              | 20191125–205703               | II              | 60                           |                               |                 |                              |
|                                    |                 |                              | 20191125–205833               | II              | 60                           |                               |                 |                              |
|                                    |                 |                              | 20191125–210001               | II              | 60                           |                               |                 |                              |
|                                    |                 |                              | 20191125–210133               | II              | 60                           |                               |                 |                              |

Table 3 – continued

| 2019 July 31–August 1 <sup>1</sup> |        |                              | 2019 November 25 <sup>2</sup> |        |                              | 2019 November 28 <sup>3</sup> |        |                              |
|------------------------------------|--------|------------------------------|-------------------------------|--------|------------------------------|-------------------------------|--------|------------------------------|
| Observation ID                     | Filter | Duration <sup>4</sup><br>(s) | Observation ID <sup>5</sup>   | Filter | Duration <sup>6</sup><br>(s) | Observation ID <sup>5</sup>   | Filter | Duration <sup>6</sup><br>(s) |
|                                    |        |                              | 20191125–210307 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–210446 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–210620 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–210753 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–210931 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–211114 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–211246 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–211422 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–211556 (A+I)         | II     | 60 (52)                      |                               |        |                              |
|                                    |        |                              | 20191125–211729 (A+I)         | II     | 60 (52)                      |                               |        |                              |

<sup>1</sup>Start time (UTC): MJD 58695.826400, stop time (UTC): MJD 58696.093971 – <sup>2</sup>Start time (UTC): MJD 58812.757486, stop time (UTC): MJD 58812.846181 – <sup>3</sup>Start time (UTC): MJD 58815.765716, stop time (UTC): MJD 58815.842789 – <sup>4</sup>Rounded to 1 s – <sup>5</sup>(A+I) identifies simultaneous Aqueye and IFI+Iqueye observations – <sup>6</sup>The number in round brackets is the simultaneous acquisition time used in the analysis, rounded to 1 s.

for delays in the intervals  $\tau \simeq [-12, -1]$  ns and  $\tau \simeq [1, 12]$  ns. This sharp excess is the consequence of a systematic effect. Aqueye+ and Iqueye are affected by spurious photon coincidences caused by secondary photons emitted when a primary photon hits a SPAD detector (e.g. Rech et al. 2007). Even if we paid particular care in minimizing this effect (by inserting diaphragms and antireflective coatings), a tiny fraction of the secondary photons can still be channelled along the optical path back to another SPAD.

We noted that spurious coincidences affect in a significant way the measurement of  $g^{(2)}$  on adjacent baselines of the same instrument ( $A - B$ ,  $B - C$ ,  $C - D$ ,  $D - A$ ), while the cross-baselines ( $A - C$ ,  $B - D$ ) are much less affected. This fact is a consequence of the internal structure of Aqueye+ and Iqueye, which channels secondary photons mostly in the direction of the detector in front. Indeed, we found that the most pronounced peaks of  $g^{(2)}$  at a delay of a few ns (Fig. 1) are present in the temporal correlation of the cross-baselines. As a consequence, the burst of secondary photons impinging on a detector has a certain probability to produce a spurious coincidence with a real photon that, during the burst interval, hits an adjacent detector.

For this reason, in the 2019 July–August run we opted for a dedicated set-up, inserting an additional filter in the sub-aperture  $D$  of Aqueye+, with the purpose of suppressing the flux of secondary photons and the related background contamination. The test performed that night showed that spurious coincidences affect the photon flux in each channel at the level of  $\gtrsim 1$  per cent. Inserting an additional filter solved the problem, but it caused a significant suppression of the flux on the sub-aperture  $D$  with the additional II filter, that has a peak transmission of only 35 per cent (see Table 2). For 2019 July–August, we then considered the less noisy measurement with the baselines made only by high counting statistics sub-apertures ( $A - B$ ,  $A - C$ ,  $B - C$ ; Table 4).

Conversely, in the 2019 November run we mounted the two available II filters separately in the two instruments. Therefore, we could not decrease the secondary-photons-induced noise but, in principle, we could take advantage of the high counting statistics of all sub-apertures for the measurement of the correlation at zero baseline. However, on November 25 the baseline  $B - C$  and on November 28 the baselines  $A - B$  and  $B - C$  showed an anomalous behaviour and we had to remove them (Table 4).

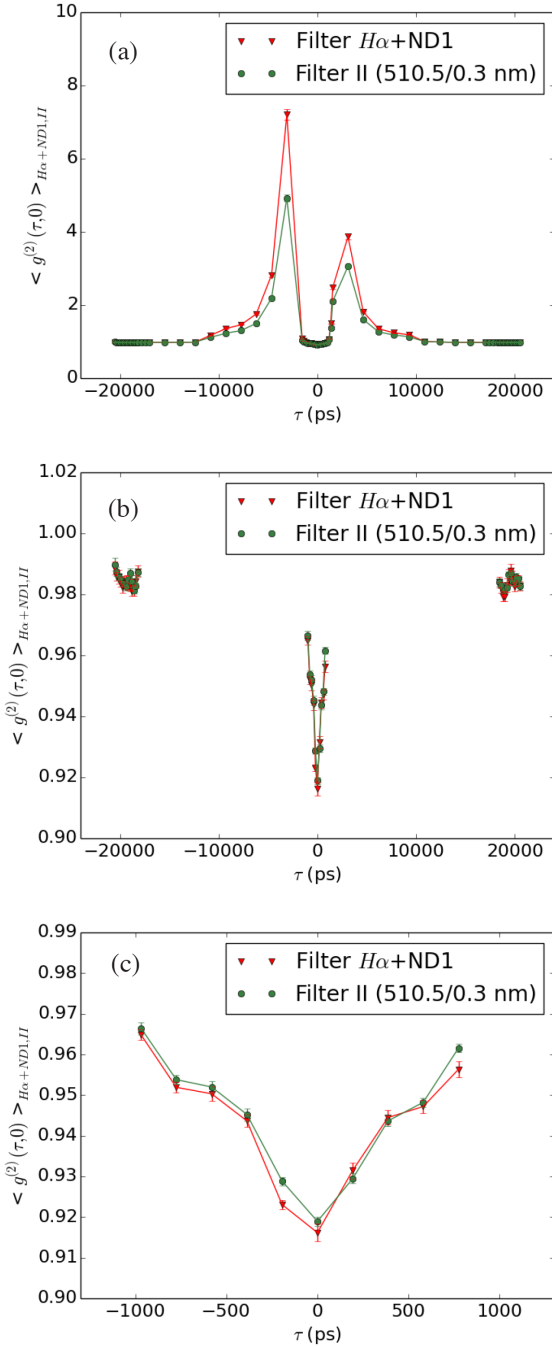
The reason behind this anomalous behaviour is related to another important instrumental systematics, the spurious (anti-)correlations between different channels of the front-end electronics that reads the signals from all the detectors at a given telescope. Eventually, most of

them turned out to produce rather stable patterns in the measurement of  $g^{(2)}$  and we succeeded in removing them by subtracting the measurements performed with two different filters (see below). The residual systematic offset induced by this effect is  $\lesssim 0.0005$ . However, at times, two baselines ( $A - B$  and  $B - C$ ) appear to have a variable response on a rather short time-scale (up to a few minutes), significantly dependent on ambient conditions (e.g. temperature). Therefore, on these baselines, variations of the average value of  $g^{(2)}$  measured in observations taken only a few minutes apart can be anomalously large ( $\sim 1$  per cent). In this case, the two-filters approach is not successful in removing the spurious (anti-)correlations patterns. The reason for which this happens is still unclear (maybe an anomalous coupling/variation of the frequency of the jitter of channels  $A$  and  $B$ , or  $B$  and  $C$ ) but, when the problem appeared during an observing night, we discarded the corresponding baseline from the final average of the measurements. As mentioned above, this was the case for baseline  $B - C$  on November 25, and for baselines  $A - B$  and  $B - C$  on November 28.

### 5.1 Calibration of the measurements

As can be seen in Fig. 1 (panel a), the cross-talk effects caused by the flux of secondary photons induce a spurious correlation with a minimum characteristic delay  $\tau_{dd}$  equal to the light traveltime delay between SPADs. As the full path is  $\simeq 40$  cm,  $\tau_{dd} \simeq 1.3$  ns. This value is in agreement with the observed start of the rising edge of the peak (Fig. 1), while the decay has a characteristic time-scale of 4–5 ns that depends on the intrinsic physical properties of the SPAD detectors. For this reason, we decided to remove the intervals  $\tau \simeq [-18, -1]$  ns and  $\tau \simeq [1, 18]$  ns from the analysis (Fig. 1, panel b). We conservatively considered  $-18$  ns and  $+18$  ns as lower and upper bounds of these intervals to be sufficiently far away from the tails of the distribution of secondary photons.

After removing the intervals  $\tau \simeq [-18, -1]$  ns and  $\tau \simeq [1, 18]$  ns, the measurements of  $g^{(2)}$  with the two filters have a similar pattern and show clearly a deep ( $\sim 10$  per cent) anticorrelation at  $\tau \simeq 0$  delay with a characteristic width of  $\sim 1$  ns, and smaller oscillations and an overall loss of efficiency (of the order of 1 per cent) at large delays (Fig. 1, panel b). This problem was already identified in the preliminary measurements reported in Zampieri et al. (2016). This behaviour does not appear in the measurement of  $g^{(2)}$  between the two telescopes and originates from spurious (anti-)correlations between the acquisition channels of the single front-end electronic board that



**Figure 1.** Temporal correlation at zero baseline for the Aqueye+ observations of Vega taken on 2019 November 28, calculated with a sampling time  $dt \simeq 400$  ps and for the two adopted combinations of filters,  $H\alpha$ +ND1 and II. The properties of the two sets of filters are reported in Table 3. *Panel (a):* measurements for delays  $\tau = [-20.5, 20.5]$  ns. *Panel (b):* measurements after removing the intervals  $\tau = [-18, -1]$  ns and  $\tau = [0.8, 18]$  ns. *Panel (c):* measurements for delays  $\tau = [-1, 0.8]$  ns.

reads the signals from all the detectors. These (anti-)correlations and oscillations of the electronics produce rather stable patterns in the measurement of  $g^{(2)}$  over an entire night of observation. Despite these effects, Fig. 1 (panel c) shows that a clear ‘excess correlation’ between  $-400$  ps and  $0$  is present in the data acquired with the II filter compared to those acquired with the  $H\alpha$ +ND1 filter. Indeed, this is what we are looking for, as the coherence of the photons acquired

**Table 4.** Combination of Aqueye+ sub-apertures used for the measurement of the correlation at zero baseline.

| Observing night       | Baselines <sup>1</sup>              |
|-----------------------|-------------------------------------|
| 2019 July 31–August 1 | $A - B, A - C, B - C$               |
| 2019 November 25      | $A - B, A - C, A - D, B - D, C - D$ |
| 2019 November 28      | $A - C, A - D, B - D, C - D$        |

<sup>1</sup>  $A, B, C$ , and  $D$  are the instrument sub-apertures (see text for details).

with the very narrow band II filter is approximately 10 times larger than that of the photons acquired with the  $H\alpha$ +ND1 filter (being the II filter width 10 times smaller).<sup>4</sup> Therefore, to remove these systematics and extract the actual signal, we subtracted the average values of  $g^{(2)}$  measured with the  $H\alpha$ +ND1 filter (used for calibration) from those measured with the II filter (see equation 3). The residual systematic error on  $g^{(2)}$  after applying this procedure is typically  $\lesssim 0.0005$ .

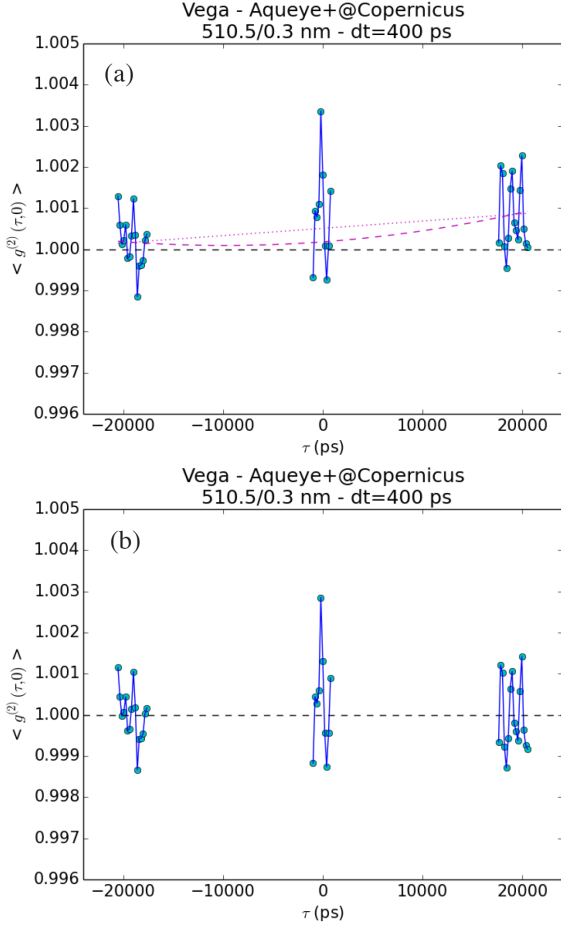
## 6 RESULTS

### 6.1 Temporal correlation at zero baseline

For the measurement of the correlation at zero baseline, we considered only the observations performed with Aqueye+, that have significantly higher counting statistics. As explained in the previous section, we successfully removed some systematics and cross-talk effects subtracting the average value of  $g^{(2)}$  measured with the  $H\alpha$ +ND1 filter from that measured with the II filter (equation 3), and considering only the delay intervals  $\tau = [-20.5, -18]$  ns,  $\tau = [-1, 0.8]$  ns, and  $\tau = [18, 20.5]$  ns. The final calibrated value of  $g^{(2)}$  for all the Aqueye+ observations of Vega is shown in Fig. 2. A peak in the degree of correlation at around zero delay is clearly visible. The value is:  $\langle g^{(2)}(0, 0) \rangle = 1.0034$ . At large delays  $\langle g^{(2)}(\tau, 0) \rangle$  shows large random oscillations with root mean square (rms)  $\sigma_{|\tau| \geq 18000 \text{ ps}} = 0.0008$ . These fluctuations are dominated by the statistical uncertainty of the measurements, as they show the  $t^{-1/2}$  decrement expected if the error is dominated by counting statistics. The estimated signal-to-noise ratio is then  $S/N = (\langle g^{(2)}(0, 0) \rangle - 1) / \sigma_{|\tau| \geq 18000 \text{ ps}} \simeq 4.2$ .

A residual systematic offset of  $\langle g^{(2)}(\tau, 0) \rangle$  (that is larger at positive delays) is visible in the data and is fit with a first-order polynomial  $p(\tau)$  (excluding all the points around the peak). Subtracting  $1 - p(\tau)$ , the value at the peak decreases ( $\langle g^{(2)}(\tau, 0) \rangle = 1.0029$ ), as well as the rms at large delays ( $\sigma_{|\tau| \geq 18000 \text{ ps}} = 0.0007$ ; Fig. 2, panel b). A parabolic fit including all but 5 points around the peak is equally acceptable and gives similar results. The origin of this small residual systematics has to do with different factors, such as residual calibration uncertainties, spectral dependences of the delay distributions of the secondary photons produced by the detectors, and/or rate-dependent effects (there are small differences in the average rates with the two filters). The systematic offset visible in Fig. 2 may be considered as the ultimate limit for the accuracy achievable with our present instrumentation. After correcting for it (using different fitting functions and number of points in the fit), the estimated signal-to-noise ratio of the measurement is in the range  $S/N \simeq 3.8\text{--}4.3$ . This value is consistent with that calculated above

<sup>4</sup>The ND1 filter was inserted only for the purpose of limiting the rate to manageable values, and comparable to those of the measurements with the II filter.



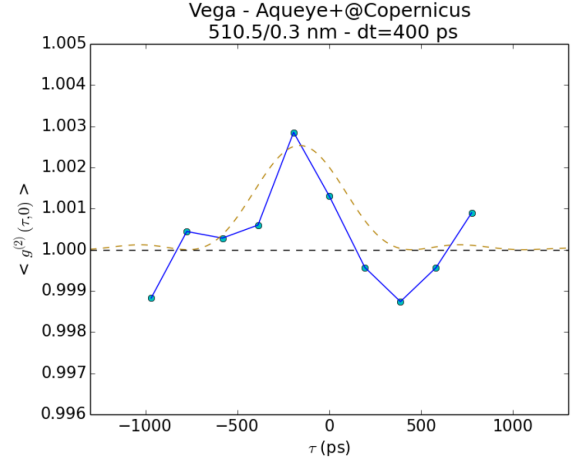
**Figure 2.** Calibrated temporal correlation at zero-baseline  $\langle g^{(2)}(\tau, 0) \rangle$  for all the Aqueye+ observations of Vega reported in Table 3. The time bin is  $dt = 400$  ps. Panel (a):  $\langle g^{(2)}(\tau, 0) \rangle$  fitted with a first-order polynomial  $p(\tau)$  (excluding all the points around the peak; magenta dashed line) and a parabola (excluding only 5 points around the peak; magenta dotted line). Panel (b):  $\langle g^{(2)}(\tau, 0) \rangle$  after correcting with  $1 - p(\tau)$  (see text for details).

and with the expected  $S/N$  reported in equation (4), confirming that the measurement is significant.

Fig. 3 shows an enlargement of  $\langle g^{(2)}(\tau, 0) \rangle$  around the peak [after subtracting  $1 - p(\tau)$ ], along with the expected profile of the temporal correlation (not fitted but simply overplotted, assuming an effective bandpass 25 per cent wider than the nominal FWHM of the II filter). The peak is clearly shifted by 160 ps towards negative delays (because of a residual difference of a few cm in the length of the cables connecting the detectors to the readout electronics), but the overall agreement is very good.

## 6.2 Temporal correlation on a 4-km baseline

In 2019 November, we performed simultaneous observations of Vega with both Aqueye+ at the Copernicus telescope and IFI+Iqueye at the Galileo telescope, forming an interferometer with a baseline of 1–4 km (Table 1). To calculate the degree of coherence between the signals of the two telescopes, they have to be properly corrected for the light traveltime delays at the two sites. The relative delay is mostly caused by the light traveltime distance projected along the direction of the star, with additional instrumental delays induced by differences in the focal lengths, position of the mirrors of the two telescopes,



**Figure 3.** Calibrated temporal correlation at zero baseline  $\langle g^{(2)}(\tau, 0) \rangle$  in the interval of delays  $\tau = [-1, 0.8]$  ns for all the Aqueye+ observations of Vega reported in Table 3. The time bin is  $dt = 400$  ps and the curve is corrected with  $1 - p(\tau)$  (see text for details). The dashed (yellow) line shows the expected profile of the temporal correlation.

**Table 5.** Instrumental delays between IFI+Iqueye@Galileo and Aqueye+@Copernicus.

|                                       | Difference <sup>1</sup> (mm) | Delay <sup>1</sup> (ns) |
|---------------------------------------|------------------------------|-------------------------|
| Equivalent focal lengths <sup>2</sup> | −4215.5                      | −14                     |
| Mirror distances <sup>3</sup>         | 1000                         | 3                       |
| IFI (instrument)                      | 1450                         | 5                       |
| IFI (optical fiber)                   | 20 000                       | 67                      |
| Electric cables                       | −12 000                      | −40                     |
| GPS antenna <sup>4</sup>              | —                            | —                       |
| Total                                 | 6234.5                       | 21                      |

<sup>1</sup>IFI+Iqueye − Aqueye+.

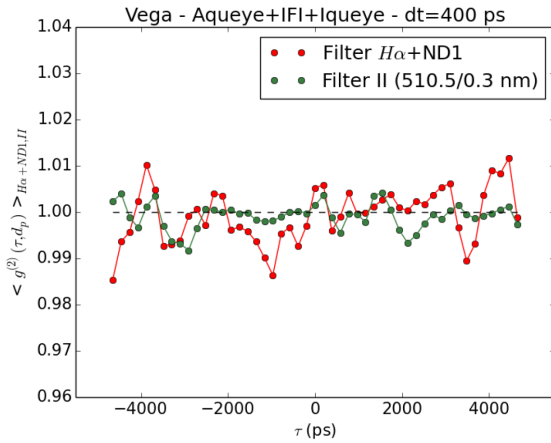
<sup>2</sup>Copernicus telescope 16315.5 mm, Galileo telescope 12100 mm.

<sup>3</sup>Referred to the intersection of the hour angle and declination axes.

<sup>4</sup>Difference of the GPS antenna height relative to the intersection of the hour angle and declination axes.

length of the electric cables, height of the GPS antenna (the GPS receiver is part of the acquisition and timing system of Aqueye+ and Iqueye, e.g. Barbieri et al. 2009) and, for Iqueye, by the additional optical path inside IFI and the optical fiber. The light traveltime delay and the projected distance between the two telescopes are calculated as a function of the position of the star on the sky and of the telescope coordinates (Table 1), while the instrumental delays are summarized in Table 5. The total delay is continuously added to the photon arrival times of IFI+Iqueye before performing the correlation. The projected telescope separation during the 2019 November 25 and 28 observing nights was varying in the range 1589–2023 m and 1535–2418 m, respectively.

The average value of the discrete degree of coherence for all the simultaneous acquisitions obtained with the H $\alpha$ +ND1 and the II filters is shown in Fig. 4. The adopted time bin is  $dt \simeq 400$  ps and the average is performed over all the combinations of the instrumental sub-apertures. The calculation of  $g^{(2)}$  was performed as described in Section 3. None of the systematic effects that affect the Aqueye+ measurements at zero baseline and discussed in Sections 5 and 6.1 is visible in Fig. 4. Since in this case we used two independent front-end electronic boards and acquisition systems, it is clear that all systematic effects that appear at zero baseline originate from



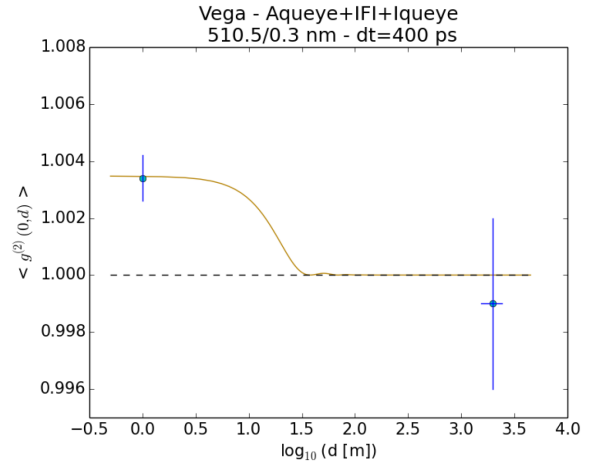
**Figure 4.** Temporal correlation on a  $\sim$ km baseline  $\langle g^{(2)}(\tau, d_p) \rangle_{H\alpha+ND1, II}$  for all the Aqueye+IFI+Iqueye 2019 November observations of Vega reported in Table 3 and for the two adopted combinations of filters,  $H\alpha+ND1$  and II. The time bin is  $dt = 400$  ps. Data are corrected for the light traveltime delay between telescopes. The projected baseline  $d_p$  varied in the range 1535–2418 m.

spurious (anti-)correlations between different channels intrinsic to a single front-end electronics.

For consistency with the approach adopted for zero baseline, we calibrated the measurements subtracting the average values of  $g^{(2)}$  measured with the  $H\alpha+ND1$  filter from those measured with the II filter (equation 3). No peak in the degree of correlation at around zero delay is visible and the fluctuations of  $g^{(2)}$  are dominated by statistical uncertainty. However, because of the variable observing conditions, during the 2019 November run the total simultaneous acquisition time (and the average count rate) with the  $H\alpha+ND1$  filter was shorter than that with the II filter (28 min versus 40 min). Therefore, the random noise on the calibrated  $\langle g^{(2)}(\tau, d_p) \rangle$  (difference between the two filters) is significantly larger than that on the II measurements  $\langle g^{(2)}(\tau, d_p) \rangle_{II}$ . As no systematic effect is visible in Fig. 4, we decided to use only the ‘uncalibrated’ measurements taken with the sole II filter to place a more stringent constraint on the absence of correlation. Given that no prominent peak is present in the II measurements in Fig. 4 and assuming that they are randomly distributed in  $\tau$ , we consider them as representative of a series of measurements at zero delay and estimate  $g^{(2)}(0, d_p)$  taking the average for all  $\tau$ . The resulting value of the degree of coherence for the simultaneous Aqueye+IFI+Iqueye measurements of 2019 November is:  $\langle g^{(2)}(0, d_p) \rangle_{A+I} = 0.999$ . We estimated the uncertainty of the measurement from the standard deviation of  $g^{(2)}$  at all delays, obtaining  $\sigma_{A+I} = 0.003$ . Despite the non-negligible uncertainty, our measurement is thus consistent with the absence of correlation, as expected for Vega on a projected baseline of  $\sim 2$  km (see below).

### 6.3 Spatial correlation

Fig. 5 shows the two measurements of the degree of coherence for Vega reported in the two previous subsections as a function of telescope separation. The zero baseline refers to the separation of the centroids of the mirror segments, which is approximately 1 m, while the long baseline corresponds to a telescope separation between 1535 m and 2418 m, varying with the star position on the sky. As it can be seen from Fig. 5, the measurements are fully consistent with the expected degree of spatial coherence for a source with the



**Figure 5.** Spatial correlation  $\langle g^{(2)}(0, d) \rangle$  for the Aqueye+IFI+Iqueye 2019 observations of Vega. The yellow solid line represents the theoretical  $g^{(2)}$  for a uniform brightness disc of 3.3 mas (angular size of Vega; Ciardi et al. 2001; Monnier et al. 2012).

angular diameter of Vega ( $3.28 \pm 0.01$  mas, Ciardi et al. 2001; 3.324 mas, Monnier et al. 2012), with a positive detection at zero baseline and no detection at a comparable level on a  $\sim$ km baseline.

## 7 DISCUSSION AND CONCLUSIONS

Our detection of the temporal correlation of a star at zero baseline and the measurement on long baseline represents another proof of principle for SII. Unlike the original Hanbury Brown and Twiss experiment, that correlated in real-time the photon intensities measured at two telescopes, the measurement reported here is obtained for the first time counting photon coincidences in post-processing by means of a single photon software correlator and exploiting entirely the quantum properties of the light emitted from a star. Working in post-processing has also the non-negligible advantage that the data reduction chain can be repeated more times (as, in fact, we did in Asiago), enabling the possibility to check for systematics, tune the parameters of the analysis, optimize the procedure, and increase the accuracy of the results. In principle, it could also enable the computation of correlations among three or more telescopes.

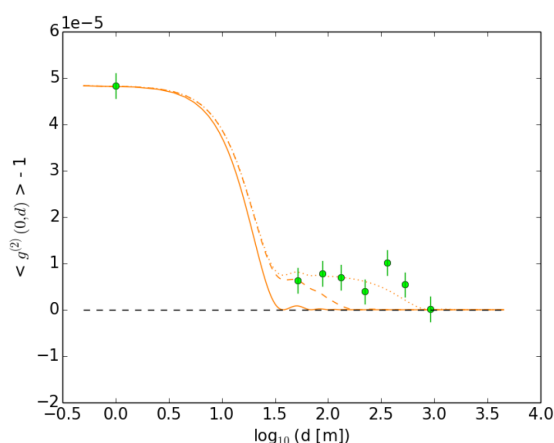
Unfortunately, the limited collecting areas of the Asiago telescopes are not suitable to perform measurements on weak targets, and the separation of the telescopes is not adequate to resolve sources on a mas scale. Nonetheless, the Asiago experiment allowed us to carry out a preparatory activity for potential implementations of SII on long-baseline arrays of Cherenkov telescopes. As a matter of fact, future Cherenkov installations will have both large collecting areas and a large number of baselines, suitable for performing SII measurements and image reconstruction with an unprecedented spatial resolution (Le Bohec & Holder 2006; Nuñez et al. 2012a, b; Dravins et al. 2013; Rou et al. 2013; Kieda et al. 2019).

On the other hand, further progress needs to be made in order to set up a multibaseline photon counting intensity interferometer on an array of Cherenkov telescopes capable of performing imaging at 10–100 microarcsec scales. First of all, a relative photon timing accuracy among different telescopes of  $\sim 1$  ns is needed to correlate the signals over short time bins  $dt$  or high sampling frequencies (see equation 4), thus keeping the observing time within reasonable limits ( $\sim$ hours). In Asiago, we achieve this goal using independent acquisition and timing systems at the two telescopes, each made of a Rubidium clock

disciplined with a GPS receiver, that allow us a synchronization with UTC with an accuracy of  $\sim 1\text{--}2$  ns (Barbieri et al. 2009; Naletto et al. 2009). Nowadays, alternative solutions based on synchronization signals distributed through ethernet networks are available, but our approach retains the required reliability and accuracy, and could still be competitive for very long (several km or more) baselines. More challenging is the effective utilization of narrow band filters. While this is a common problem also for other SII implementations, it is particularly constraining for a single photon counting approach like ours because photon rates must be limited to affordable values without reducing the signal (i.e. without significantly attenuating the photon flux). For the very small  $f$ /numbers (i.e.  $\sim f/1$ ) of the Cherenkov telescopes, the angle of incidence of the rays coming on the interferometric filter from the outer portion of the mirror is very large (tens of degrees). Consequently, the transmitted wavelength of such rays is significantly smaller than that of those coming at normal incidence (Kieda et al. 2019). This broadening of the transmitted bandpass  $\Delta\lambda$  for a given photon rate reduces the  $S/N$  ratio of a measurement. To narrow the filter bandpass while maintaining a good transmission efficiency, an appropriate solution is installing a (removable) optical module at the telescope focal plane, suitably designed to reduce the angle of incidence.

A further aspect to consider for the implementation of SII on large area telescopes is handling the very high expected photon rates. The detectors must sustain more than  $10^8$  events/s and the acquisition electronics must be capable of coping with very high data rates (up to a few Gbit/s). In this respect, a number of selected components (SiPM detectors, Time-to-Digital Converters or Digitizer Cards with Field Programmable Gate Arrays and data compression, Computers with fast motherboards) with the required performance are presently available on the market. In addition, significant storage space and computational power are needed for saving and processing the large amount of acquired data. A post-processing approach similar to that adopted in Asiago can be applied to Small-Size Cherenkov Telescopes (SSCTs) of the 4-m class or to larger area telescopes for weaker targets. We estimate that a  $\sim 1$  h observation at a maximum rate of  $\approx 100$  Mcounts/s will produce a few Terabytes of raw data at each telescope. While these are significant but manageable numbers, the requirement in terms of computational time is rather demanding. Scaling from the processing time required for the data of the Asiago experiment, a  $\sim 1$  h measurement of  $g^{(2)}$  performed at the maximum rate, sufficient to reach an  $S/N \sim 5$  with a filter having a bandpass of several nanometers, will require 14 h for 8 baselines on a machine with 2000 CPU cores. For the typical effective area of an SSCT, the maximum rate is reached for the brightest stars ( $V \sim 0$ ), while for a Large Size Cherenkov Telescope (20-m class) for a star with  $V \sim 4$ .

To illustrate the potential of the technique with the upgrades outlined above and with the resolving capabilities of a km baseline Cherenkov telescope array, we consider the hypothesis of a hotspot on the surface of a star like Vega and intensity interferometry observations carried out with the SSCTs. A detailed simulation of surface features reconstruction for an array of Cherenkov telescopes was already presented by Nuñez et al. (2012b). Here, we describe only a specific example, providing details for a photon counting implementation within the framework discussed above. Fig. 6 shows a simulated measurement at zero baseline plus 7 additional measurements on projected baselines from  $\sim 100$  m up to  $\sim 1$  km, assuming a time resolution of  $\sim 1$  ns, a bandpass of  $\sim 5$  nm and a count rate of  $\sim 100$  Mcounts/s. The total acquisition time per measurement is 4 h. Simulated data are drawn from the expected theoretical value of  $g^{(2)}$  for a bright-spot of  $130 \mu\text{as}$  emitting 30 per cent of the source photon flux, overimposed on a disc of  $3.3$  mas emitting the remaining



**Figure 6.** Simulated spatial correlation ( $\langle g^{(2)}(0, d) \rangle - 1$ ) for Cherenkov telescope observations. The orange solid line represents the theoretical  $g^{(2)}$  for a uniform brightness disc of  $3.3$  mas emitting 70 per cent of the source photon flux. The other lines are the theoretical  $g^{(2)}$  for a bright-spot emitting 30 per cent of the source photon flux, overimposed on the  $3.3$  mas disc. Spot size:  $130 \mu\text{as}$  (orange dotted line),  $430 \mu\text{as}$  (orange dashed line).

70 per cent. The best match is obtained for the same theoretical curve (reduced  $\chi^2 = 1.0$  for 8 degrees of freedom). The other curves are not consistent with the simulated data (reduced  $\chi^2 > 3.7$  for 8 degrees of freedom). We emphasize the importance of having an SII implementation capable of at least one simultaneous measurement at zero baseline, which permits to calibrate the contribution of the stellar component and reduce the uncertainty on the parameters estimation. The simulated measurements are consistent with the presence of a hotspot with a size 25 times smaller than that of the star. For thermal emission, the temperature of the spot would be significantly higher than that of the star. While the optical-UV spectrum would show evidence for such an additional hot component, its actual morphology and structure could only be investigated through interferometric observations. A km baseline interferometric observation has thus the potential to place a direct constraint on surface features as small as tens of  $\mu\text{as}$  on the surface of a star, and hence to probe magnetic phenomena, such as those inferred from the observation of rotation modulations and flaring activity in the Kepler light curves of numerous A-type stars (Balona 2017; Van Doorselaere, Shariati & Debosscher 2017). Larger effective collecting areas such as those obtained combining Small Size with Medium/Large Size Cherenkov Telescopes would provide the required photon flux even for weaker targets or lower-contrast spots/features. With SII on km projected baselines one is then moving into novel and previously unexplored parameter domains in stellar Astrophysics, with the possibility to achieve imaging capabilities and angular resolutions in the optical band close to those attained at mm wavelengths with the Event Horizon Telescope.

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## DATA AVAILABILITY

Original event lists are stored in the Aqueye+Iqueye Public Data Archive, reachable from the Aqueye+Iqueye project page: <https://web.oapd.inaf.it/zampieri/aqueye-iqueye/> and are available upon request. All analysed data needed to evaluate the conclusions in the paper are present in the paper.

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